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Thad B. Welch Boise State University

Cameron H.G. Wright *University of Wyoming*

Michael G. Morrow University of Wisconsin, Madison

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What is the Derivative of Music?

Dr. Thad B. Welch, Boise State University

Thad B. Welch, Ph.D., P.E. received the B.E.E., M.S.E.E., E.E., and Ph.D. degrees from the Georgia Institute of Technology, Naval Postgraduate School, Naval Postgraduate School, and the University of Colorado in 1979, 1989, 1989, and 1997, respectively. He was commissioned in the U.S. Navy in 1979 and has been assigned to three submarines and a submarine repair tender. He has deployed in the Atlantic Ocean, Mediterranean Sea, and the Arctic Ocean.

From 1994-1997 he was an Instructor and Assistant Professor teaching in the Electrical Engineering Department at the U.S. Air Force Academy, Colorado Springs, CO. During 1996-1997 he was recognized as the Outstanding Academy Educator for the Electrical Engineering Department.

From 1997-2007 he was an Assistant Professor, Associate Professor, and Permanent Military Professor teaching in the Electrical Engineering Department at the U.S. Naval Academy, Annapolis, MD. During 2000-2001 he was recognized as the Outstanding Academy Educator for the Electrical Engineering Department. During 2001-2002 he received the Raouf outstanding engineering educator award. During 2002-2003 he was recognized as the Outstanding Researcher for the Electrical Engineering Department. He was an invited scholar at the University of Wyoming, fall 2004, where he was recognized as an eminent engineer and inducted into tau beta pi. In 2006 he co-authored "Real-time Digital Signal Processing, from MATLAB to C with the TMS320C6x DSK" which was translated into Chinese in 2011. The second edition of this text was published in 2012 and the third edition was published in 2017.

From 2007-2010 he was Professor and Chair of the Electrical and Computer Engineering Department at Boise State University, Boise, ID. From 2011-2012 he was the inaugural Signal Processing Education Network (SPEN) Fellow. From 2012-2014 he and his wife lived with 20 engineering students in the engineering residential college (ERC) on the Boise State campus.

His research interests include real-time digital signal processing (DSP), the implementation of DSP-based systems, and sustainable energy systems.

Dr. Cameron H. G. Wright P.E., University of Wyoming

Cameron H. G. Wright, Ph.D., P.E., is Interim Dean of the College of Engineering and Applied Science, and Professor of Electrical and Computer Engineering at the University of Wyoming, Laramie, WY. He was previously Professor and Deputy Department Head in the Department of Electrical Engineering at the United States Air Force Academy, and served as an R&D engineering officer in the U.S. Air Force for over 20 years. He received the B.S.E.E. (summa cum laude) from Louisiana Tech University in 1983, the M.S.E.E. from Purdue University in 1988, and the Ph.D. from the University of Texas at Austin in 1996. Cam's research interests include signal and image processing, real-time embedded computer systems, biomedical instrumentation, and engineering education. He is a member of ASEE, IEEE, SPIE, BMES, NSPE, Tau Beta Pi, and Eta Kappa Nu. His teaching awards include the University of Wyoming Ellbogen Meritorious Classroom Teaching Award (2012), the Tau Beta Pi WY-A Undergraduate Teaching Award (2011), the IEEE UW Student Branch's Outstanding Professor of the Year (2005 and 2008), the UW Mortar Board "Top Prof" award (2005, 2007, and 2015), the Outstanding Teaching Award from the ASEE Rocky Mountain Section (2007), the John A. Curtis Lecture Award from the Computers in Education Division of ASEE (1998, 2005, and 2010), and the Brigadier General Roland E. Thomas Award for outstanding contribution to cadet education (both 1992 and 1993) at the U.S. Air Force Academy. He is an active ABET evaluator and an NCEES PE exam committee member.

Mr. Michael G. Morrow, University of Wisconsin, Madison

Michael G. Morrow, M.Eng.E.E., P.E., is an Emeritus Faculty Associate in the Department of Electrical and Computer Engineering at the University of Wisconsin, Madison, WI. He previously taught at Boise State University and the U.S. Naval Academy. He is a senior member of IEEE.

What is the Derivative of Music?

Abstract

In our continuing effort to prove to students that *Signals & Systems* is not just another mathematics course taught by the ECE Department, we ask the question, "What is the Derivative of Music?"

The first-order difference (or first-difference) is an incredibly simple algorithm that very accurately approximates the numeric derivative operator, especially for oversampled signals. Its inverse also accurately approximates the numeric integration operator, but not without numeric difficulty.

Given a real-time demonstration using winDSK8, we can now show students that these mathematical operators provide powerful signal processing filtering tools for real-world signals.

During this ASEE session, we will include the demonstration that the derivative operator is more than a symbolic mathematical operator and much more than just another academic exercise.

We have successfully used winDSK, winDSK6, and the latest version, winDSK8, to provide demonstrations of any number of concepts during outreach (K-12 events), at freshman motivational events, and in junior, senior, and even graduate ECE courses.

Introduction

For years, students have struggled with learning the significance of the impulse response. This is especially true given that there is no piece of test and measurement equipment (T&ME) in our teaching laboratories that is capable of producing a true impulse. Many educators have written about the benefits of demonstrations to aid student learning, especially for some of these more difficult topics [1-15].

The discrete-time equivalent of the impulse response, the unit sample response, can be just as onerous for students to understand, since it's regularly viewed as "just a computer simulation" and not related to anything that's practical or happening in the real-world.

To illustrate this point, for several years, the authors have presented to students a question similar to, "In your own words, define the term, *impulse response*." The average score on this question was routinely the lowest of any of the questions on the *Signals & Systems* final examination. This improved significantly when real-time demonstrations, other hardware demonstrations, and laboratory exercises were introduced in the class.

Background

During outreach (K-12 events), at freshman motivational events, and in junior, senior, and even graduate ECE courses, we have used real-time systems to demonstrate the utility of user-programmable devices.

During the freshman or early ECE course events, where the derivative operator is (hopefully) well understood, we ask the question, "What is the Derivative of Music?" The typical student response is, "Give me the equation of the music and I can calculate its derivative." Our reply is usually along the lines of, "If you only want to listen to sinusoids or other simple periodic waveforms, I can give you an equation. But can *you* write the equation for your favorite song?"

This allows a seamless transition to the fact that while not all signals are *born digital*, we regularly process our signals in their digital or discrete form.

Returning our discussion to the derivative operator, a student who has learned the fundamentals of the Laplace transform should recognize the derivative, d/dt as the Laplace independent variable s. In most texts, $s = \sigma + j\omega$, and for a discussion of the frequency response, setting $\sigma = 0$ results in the classic result, $s = j\omega$. At this point, a *Signals & Systems* student should be able to recreate Figure 1. This should be recognized as the magnitude only display of a Bode plot for the response of an ideal integrator, 1/s, and an ideal differentiator, s.

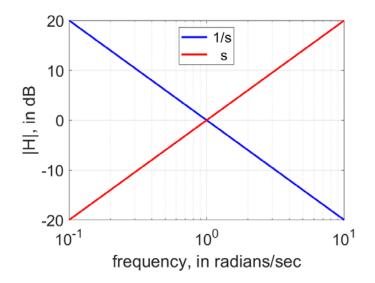


Figure 1. The frequency response (magnitude only) of an ideal integrator, 1/s, and an ideal differentiator, s. This is a portion of a Bode plot; phase is not shown.

In the sampled world, the result of the first-order difference, y[n] = x[n] - x[n - 1], is shown in Figure 2. The first-order difference or first difference, is just the difference

between the current and previous sample values. Figure 2 doesn't look much like the plot of a differentiator that we saw in Figure 1. But after shifting to logarithmic axes, shown in Figure 3, this now looks very similar to the associated plot in Figure 1. This provides a wonderful opportunity to discuss with students a number of related topics, including sampling, aliasing, use of the decibel (dB), and filtering.

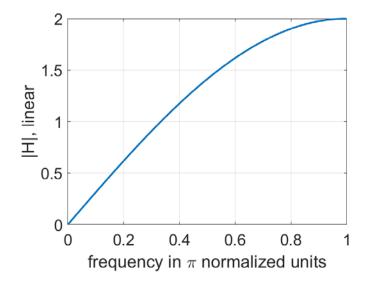


Figure 2. The frequency response (magnitude only) of the first-order difference, using linear axes.

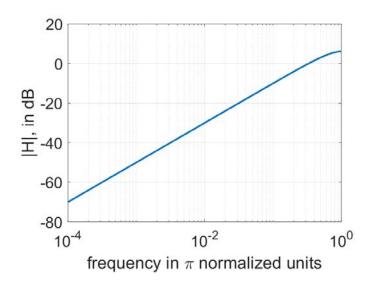


Figure 3. The frequency response (magnitude only) of the first-order difference, using logarithmic axes.

In MATLAB, the difference operator is implemented using the **diff** command. MATLAB can also calculate higher-order differences using this same **diff** command.

While s plots as a perfectly straight line in Figure 1, the first-order difference is incredibly close to a straight line for oversampled signals and only diverges from a straight line near the very upper end of the frequency axis, approaching the maximum frequency, Fs/2. It is easy to shift the magnitude value up or down, by simply applying a scale factor or gain. Similar observations can be made regarding the discrete-time version of 1/s, as shown in Figure 4.

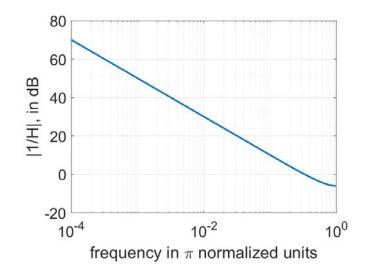


Figure 4. The frequency response (magnitude only) of the reciprocal of the first-order difference, using logarithmic axes.

Now that the frequency responses for s and 1/s (i.e., the first-order difference and its reciprocal) have been determined, the straightforward observation can be made that these actually represent filters. Specifically, s and the first-order difference are highpass filters and 1/s, the reciprocal of the first-order difference, are lowpass filters.

It must be noted that the pure reciprocal of the first-order difference becomes y[n] = y[n-1] + x[n], which is actually an ideal accumulator, and this form will cause stability issues.

This observation then leads naturally to a discussion with students of what is sometimes called the *leaky integrator*, y[n] = gain*y[n-1] + x[n], where gain is a value between 0 and 1, but usually very close to 1, e.g., 0.99. The gain value pulls the system's pole off of the unit circle, reducing the DC gain to a finite value, and resulting in a stable system. All of these topics can be stimulated by the simple question, "What is the Derivative of Music?"

Real-time demonstrations

The discussions with students are all accompanied by real-time demonstrations using winDSK8. This program, designed specifically for educators, and freely available to educators, has evolved and improved over the years [11-16]. A complete description of what is needed and how to connect both the hardware and software necessary to perform these and other demonstrations is provided in [16].

ừ winDSK8 ver 3.0.0.0		×	
Audio Demo Apps		DSP Board Configuration	
Talk-Thru	Vocoder	DSP: LCDK (OMAP-L138) V	
Audio Effects	Graphic Equalizer	Codec: AIC3106_16bit_McASP0 \lor	
K-P String		Sample Rate: 48.0 kHz \vee	
Guitar Synthesizer		Input Source: Line In \sim	
Filters (Communications		Host Interface Configuration	
Filters/Communications	0.00%	COM Port: COM4: ~	
FIR Filter	CommDSK	Baud: 921600 ~	
IIR (SOS)	CommFSK	Rescan COM Ports	
IIR (DF2)	Notch Filter	System Functions	
Filters/Communications		Get Board Version	
Oscope/Analyzer	Arbitrary Waveform	Load Program	
	Arbitrary wavelorm	Reset DSP	
DTMF Generator		Host Interface Test	
		Confidence Test	
Help	Quit without Saving	Save Settings and Exit	

Figure 5. The winDSK8 program main graphical user interface screen.

winDSK8 is designed to work with the TI LCDK (low cost development board). The GUI (graphical user interface) for winDSK8 allows for hundreds of different demonstrations, including everything that we have discussed in this paper. For the topics we are discussing here, the ability to quickly implement and demonstrate both FIR (shown in Figure 6) and IIR (shown in Figure 7) digital filters is a major benefit for the professor and the students.

FIR Filter (LCDK (OMAP-L138)) :: AIC3106_16bit_McASP0	×
Filter Coefficients $h[000] = +1.000000$	Quit
$ \begin{array}{l} h[000] &= \pm 1.000000 \\ h[001] &= \pm 0.000000 \\ h[002] &= \pm 0.000000 \end{array} $	Codec Settings
$ \begin{array}{l} h[003] &= +0.000000 \\ h[004] &= +0.000000 \\ h[005] &= +0.000000 \\ h[005] &= 0.000000 \\ h[005] &= 0.00000 \\ h[0$	Import
$\begin{array}{l} h[005] &= +0.000000 \\ h[006] &= +0.000000 \\ h[007] &= +0.000000 \end{array}$	Unity Gain
h[008] = +0.000000 h[009] = +0.000000	ilter Operating Mode
$ \begin{array}{l} h[010] &= +0.000000 \\ h[011] &= +0.000000 \\ h[012] &= +0.000000 \end{array} $	loating-point <
h[013] = +0.000000	Bypass Filters
+1.000000 Update	

Figure 6. The winDSK8 program graphical user interface screen for defining and demonstrating FIR digital filters.

IIR Filter (DF2) (LCDK (OMAP-L138	×	
Filter Coefficients Numerator (B) B[000] = ± 1.000000 B[001] = ± 0.000000 B[002] = ± 0.000000 B[003] = ± 0.000000 B[005] = ± 0.000000 B[006] = ± 0.000000 B[007] = ± 0.000000 B[008] = ± 0.000000 B[009] = ± 0.000000 B[010] = ± 0.000000 B[011] = ± 0.000000 B[011] = ± 0.000000 Left Zero All	$\begin{array}{c c} & & & & \\ \hline & & & \\ A[000] = +0.000000 & & \\ A[001] = +0.000000 & & \\ A[002] = +0.000000 & & \\ A[003] = +0.000000 & & \\ A[005] = +0.000000 & & \\ A[005] = +0.000000 & & \\ A[006] = +0.000000 & & \\ A[008] = +0.000000 & & \\ A[009] = +0.000000 & & \\ A[010] = +0.000000 & & \\ A[011] = +0.000000 & & \\ \hline \hline & & \\ \hline \hline & & \\ \hline \hline & & \\ \hline & & \\ \hline \hline & & \\ \hline \hline \\ \hline & & \\ \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \\ \hline \\ \hline $	Bypass Filters

Figure 7. The winDSK8 program graphical user interface screen for defining and demonstrating IIR digital filters.

Conclusions

After this quick demonstration, all of the current *Signals & Systems* students were correctly able to identify the derivative of music as a highpass filtered version of the original music signal. Similar success was demonstrated with the integrator, a lowpass filter, and with varying the magnitude of the unit impulse response, a volume control.

Real-world signals and the real-time processing of these signals, especially using studentprovided music for the signals, is remarkably motivational to our students. It has led to a much better understanding of what had been previously viewed by almost all *Signals & Systems* students as "just another math class."

During a requested guest lecture opportunity during this past academic year, 24 of 25 students felt that this demonstration helped them better understand *Signals & Systems* and all students wanted additional demonstrations and applications to be included in the class.

We encourage all professors to consider using real-world signals in all of their classes. The authors have repeatedly offered a three-credit, semester long, elective course in realtime signal processing. While our preference is to process these signals in real-time, offline processing can be almost as effective.

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