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RESEARCH LETTER

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Kev Points:

- · Lahar is monitored for the first time using infrasound array
- Advancement of lahar was 38 m/s over 10 km section: detected flow lasted more than 2 h
- Use of infrasound surveillance has potential for future lahar study and hazard mitigation

Supporting Information:

- Readme
- Movie S1

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Lahar infrasound associated with Volcán Villarrica's 3 March 2015 eruption

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Abstract The paroxysmal 2015 eruption of Volcán Villarrica (Chile) produced a 2.5 h long lahar, which descended more than 20 km within the Rio Correntoso/Turbio drainage and destroyed two small bridges. A three-element infrasound array 10 km from the summit, and 4 km from the lahar's closest approach, was used to study the flow's progression. Array processing using cross-correlation lag times and semblance places constraints on the lahar's dynamics, including detection of an initial flow pulse that traveled from 2 to 12 km at an average speed of 38 m/s. Subsequently, the lahar signal evolved to a relatively stationary infrasonic tremor located 10 to 12 km from the vent and adjacent to a topographic notch, through which sound may have preferentially diffracted toward the recording site. This study demonstrates the powerful capabilities of infrasound arrays for lahar study and suggests their potential application for future hazard monitoring.

1. Introduction

Lahars are one of the principal hazards at volcanoes. The most deadly historic lahar occurred in 1985 at Nevado del Ruiz (Colombia) when eruption-induced glacial melting produced flows that traveled further than 100 km and killed more than 25,000 people [Lowe et al., 1986]. Lahars, such as those at Nevado del Ruiz, may be generated coincidentally with volcanic eruptions or can initiate as secondary flows following rain events on ash-covered slopes, failure of crater lake impoundments, or spontaneous erosion or collapse of volcanic slopes [Vallance, 2000]. Efforts to mitigate lahar hazards focus on the timely upstream identification of flows and the relay of warnings to downstream authorities and the public. Such monitoring currently entails a wide spectrum of techniques, including radio-equipped human observers (e.g., Tungurahua, Ecuador), webcams (e.g., at Sakurajima, Japan), and networks of telemetered geophones, stream gauges, or "acoustic flow monitors" (e.g., at Merapi, Indonesia [Lavigne et al., 2000]). Geophone lahar detection, termed "acoustic flow monitoring," relies upon identification of high-frequency, high-amplitude tremor using duration threshold criteria [Hadley and LaHusen, 1995]. Our study presents a lahar case study from Volcan Villarrica and introduces "infrasound flow monitoring" as a potential complementary monitoring technique.

Low-frequency sound monitoring, typically in the infrasound (<20 Hz) band, is utilized in volcanology as both an eruption surveillance tool and as an instrument to improve understanding of eruption dynamics and flow phenomena [e.g., Johnson and Ripepe, 2011; Fee and Matoza, 2013]. Dynamics of volcanic pyroclastic flows, for instance, have been investigated at Soufrière Hills, Montserrat [Ripepe et al., 2009], and Unzen, Japan [Yamasato, 1997], using arrays and networks of infrasound sensors, respectively. Nonvolcanic gravity-driven flows, such as snow avalanches, have also been studied using infrasound array processing techniques [e.g., Havens et al., 2014]. Gravity-driven flows, such as pyroclastic currents, snow avalanches, lahars, and other types of debris flows [Kogelnig et al., 2014], produce inherently complex signal because the radiation source is moving and is often noncompact with respect to radiated acoustic energy. Arrays of acoustic sensors provide important beam-forming constraints that permit the tracking of moving, and/or distributed, low signal-to-noise sources.

2. Volcán Villarrica Background

Villarrica is Chile's most regular active volcano and typically hosts an open-vent lava lake with a surface located some few hundred meters beneath the summit crater rim [Palma et al., 2008]. Infrequent paroxysmal eruptive periods, punctuated by volcanic explosivity index (VEI) 2 events, occur with repeat intervals of every few decades [Van Daele et al., 2014]. Periods of heightened activity typically last months to years, such as the

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Figure 1. (a) A 6 March photo from Rio Turbio Bridge (17.2 km LFD from summit) looking upstream and showing fresh lahar deposits. (b) A 5 April photo from Correntoso at 8 km LFD looking downstream. The lahar flowed through the deep canyon to the left of the prominent hill.

most recent elevated activity in 1971 and 1984–85, when lahars cut bridges on both southern and northern sides of the volcano [*Siebert and Simkin*, 2002]. Lahar records from lake core sediment indicate similar activity for at least 22 eruptions occurring during the last 600 years [*Van Daele et al.*, 2014].

Paroxysmal eruptions and eruptioninduced laharic activity had been absent at Villarrica for 30 years, from 1985 until the 2015 activity featured in this study. Starting in early February of 2015, high levels of seismicity, increasing vent infrasound, and observations of ash venting and ballistics ejection prompted an elevation in volcanic alert (reports at www.onemi.cl). On 2 March, the Chilean monitoring agency Servicio Nacional de Geología y Minería issued a timely red alert and the Chilean security ministry Oficina Nacional de Emergencia del Ministerio del Interior extended the exclusion zone to 9 km.

On the morning of 3 March vigorous strombolian activity preceded a paroxysmal 1500 m high lava fountain that grew starting at ~3:00 A.M. (local time) and terminated about a half an hour later. This brief but violent VEI 2

paroxysm produced heavy tephra fall to the east and incandescent scoria flows predominantly on the north and east flanks, which were well observed from the city of Pucon at 17 km distance. These flows appeared as rolling blocks and slurries of incandescent material descending atop frozen surfaces and reaching distances of at least 1 km. Explosive lava fountaining, which coincided with vent-sourced infrasound, tapered quickly and terminated by about 3:30 A.M. Ensuing activity consisted of the collapse of unstable blocks on the slopes and laharic activity in drainages to the NNW and a larger lahar, which descended to the NNE.

We refer to this NNE flow path as the Correntoso/Turbio (CT), noting that although the Correntoso appears on many maps, some sources refer to the upper tributary as the Pedgregoso. The CT flow destroyed two small bridges with earthen abutments, located at 13.5 and 14.5 km longitudinal flow distances (LFD) from the summit and just upstream of the confluence of the Correntoso and Turbio Rivers (at 15.5 km LFD). The much larger steel-girdered bridge over the Turbio at 17.2 km LFD was not damaged despite evidence of high-energy flow, including deposition of meter-sized blocks at this distance (see Figure 1a).

3. Study

Acquisition of the 3 March lahar infrasound signal was serendipitous in that a network of infrasound sensors had recently been deployed around Villarrica in January and February with the intent to understand atmospheric propagation phenomena. These stations complemented a permanent six-element infrasound array (VIX) located 8 km from the vent, which is used to continuously monitor variations in volcanic unrest. The temporary 5 month deployment consisted of 30 infrasonic microphones deployed as 10 three-element infrasound arrays at a range of azimuths and distances (from 22 km to the summit itself, where sensors were destroyed on 3 March). The objectives of both the short-term and permanent installations were to better understand the



-8000 -6000 -4000 -2000 0 2000 4000 6000 8000 10000 easting (m)

Figure 2. (a) Longitudinal flow profile of the CT. Diamonds indicate 1 km LFD ticks. Cerduo profile corresponds to the relative height of the intervening topography between Array VIH and the CT drainage. Locations of bridges and significant waterfalls are indicated. (b) Slant distance and back azimuth between flow profile and Array VIH. (c) Advanced Spaceborne Thermal Emission and Reflection Radiometer (ASTER) Global Digital Elevation Map (GDEM) topography-derived 100 m contours draped on NASA EO-1 ALI image acquired on 9 March. Inset shows relative locations of infrasound sensors.

continuous and especially intense infrasound produced by Villarrica's open vent [*Ripepe et al.*, 2009; *Goto and Johnson*, 2011; *Richardson et al.*, 2014] and to characterize the effects of dynamic atmospheric structure on infrasound propagation [e.g., *Johnson et al.*, 2012]. The location of six infrasound arrays is indicated on the map of Figure 2, and example infrasound records from these stations are provided in Figure 3. Array VIH recorded the CT lahar signal with the greatest fidelity and is featured in this work.

Infrasonic microphones at all stations were composed of infraBSU Microelectromechanical systems based differential pressure transducers with an operation similar to that described in Marcillo et al. [2012]. Sensor corner frequency (3 dB down) was at 0.045 Hz (22 s), and intrinsic RMS noise levels in the 1-10 Hz band were at ~2 mPa. Microphone arrays consisted of a spatial distribution of sensors connected to a central datalogger with signal and power cable. Array aperture of VIH was ~25 m, and nodal locations were surveyed to an accuracy of ~50 cm using compass and measuring tape (Figure 2 inset). Data at VIH were acquired continuously at 100 Hz using DataCube 24 bit, three-channel digitizers with GPS time synchronization.

Infrasound records from the six mapped arrays reveal a combination of common and more local signal source generation (Figure 3). Gross waveform features that are shared across the network, and which possess similar waveform envelope and reduced pressure amplitudes, are relatable to summit or vent activity. Coherent sound that is only evident on individual arrays suggests that a source is preferentially located either closer to or within line of sight of that array. Generally, high-pass-filtered infrasound (>10 Hz) appears to accentuate signal differences leading us to conclude that high frequencies predominate for potential lahar sources. The most striking example of coherent infrasound that is pronounced on a single array is the more than 2 h long rapidly rising and slowly decaying tremor beginning 03:25 A.M. on Array VIH. Other arrays, including VIC, VIX, and VIY, also recorded high-frequency moving source signals, but these records were significantly lower in intensity and possessed inferior signal-to-noise quality compared to that of VIH.

3.1. Lahar Source Tracking

Lahar signal contains comparatively high-frequency energy relative to the infrasound from Villarrica vent activity, which is manifested by strombolian and lava fountaining, as well as passive ~1 Hz degassing signal [e.g., *Ripepe et al.*, 2009; *Goto and Johnson*, 2011; *Richardson et al.*, 2014]. The spectral evolution of the lahar recorded by the VIH array shows a broadband character that begins with prominent high-frequency energy



Figure 3. Infrasound records from six arrays filtered in the 0.25–5 Hz (black) and 10–50 Hz (red) bands. Records are displayed with their recorded pressures but are scaled to a common reduced pressure using the distances shown in parentheses. Labels of strombolian, paroxysm, and lahar correspond to periods of discrete explosive pulses, culminating lava fountain, and CT lahar periods, respectively.

extending at least to the Nyquist frequency (50 Hz for VIH data) and with peak frequency at 2–3 Hz. A centroid frequency, calculated as the weighted power amplitude spectrum, indicates an evolution from ~20 Hz to ~10 Hz during the first 15 min of the lahar (Figure 4b). Considering the generally broad spectral nature of the lahar infrasound, we perform source localization using broadly filtered data from 0.25 to 50 Hz, which serves to avoid potential spatial aliasing.

Evolving cross-correlation lag times for three unique station pairs are plotted as "correlograms" for 5 s windows with 1 s time steps (Figures 4c-4e). The correlogram lag times were resampled from 100 Hz to 1000 Hz through cubic interpolation to provide more detailed timing precision for source localization. Peak correlation lag times are considered consistent when the lag time sum of the three station pairs is less than the original digitization sample rate of 10 ms. Consistent windows for which mean normalized cross-correlation values are greater than 0.25 are considered as signal in this study.

Signal interarray lag times are compared with expected array lag times for candidate sources restricted to Villarrica's summit and/or to the CT flow path (mapped from NASA Advanced Land Imager (ALI) imagery and ground reconnaissance). A root-mean-square timing residual *R* is

calculated for each candidate source location (*x*, *y*, and *z* as a function of LFD) and for each overlapping 5 s time window centered at time *t*:

$$R(x, y, z, t) = \sqrt{(\Delta\phi_{2-1} - \Delta\tau_{2-1})^2 + (\Delta\phi_{3-2} - \Delta\tau_{3-2})^2 + (\Delta\phi_{1-3} - \Delta\tau_{1-3})^2}$$
(1)

where $\Delta \tau_{i-j}$ is the measured time lag between channels *i* and *j* and $\Delta \phi_{i-j}$ is the calculated time lag for sound propagating at 340 m/s and is a function of source position.

Low residual values can be mapped over time (see Figures 4f and 5b and Movie S1 in the supporting information) and indicate dynamic acoustic source locations. LFD uncertainty increases for candidate source locations with shared common back azimuths (see Figure 2b). Conversely, best locations are obtained when the flow path is perpendicular to the source-receiver direction, e.g., at LFD of ~9 km, where a residual error of 10 ms corresponds to LFD location uncertainty of 800 m. At further distances along the CT, beyond ~16 km, potential source locations cannot be resolved using Array VIH.

The locations determined by minimizing equation (1) determines a point location of the most intense sound signal recorded by the array for that time window. Sound source detection is potentially biased by source proximity, such that more distant sources are underrepresented. Moreover, the lahar acoustic source is most

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Figure 4. Analysis of 3 h time series encompassing summit eruptive activity and ensuing lahar. (a) Acoustic intensity recorded at Array VIH for two primary bands. (b) Broadband acoustic waveform (0.25–50 Hz) and corresponding spectrogram with centroid frequency shown as black line. (c–e) Correlograms showing intersensor-normalized cross-correlation values as a function of signal time (*x* axis) and phase lag (*y* axis). Highest correlation color values correspond to principal correlation time lags (in seconds) between the three sensor pairs. (f) Inferred source LFD tracked over time according to residual equation (1) and semblance equation (2) source localization. Residual timing uncertainty of 0.01 s is indicated with vertical gray lines. Black dashed line corresponds to inferred trailing edge of active flow. Distances of bridges and significant waterfalls in the CT are indicated. All calculations, including cross correlation, spectrogram, and flow locations, are made for 5 s windows with 4 s overlap.

likely a noncompact region. We speculate that active lahars flow over a longitudinal extent, which likely radiate sound as a complex superposition of sources, yet only one (prominent) source position is determined using cross correlation.

An alternate and complementary technique to map evolving acoustic source distributions uses semblance, which is a measure of signal to noise of the array beam stack [*Neidell and Taner*, 1971]. Expected interelement time shifts are calculated for each point along the flow path, and the recorded acoustic signals ∂p_i are accordingly shifted, stacked, and normalized.

$$S(x, y, z, t) = \frac{(\partial p_1(t) + \partial p_2(t + \Delta \phi_{2-1}) + \partial p_3(t + \Delta \phi_{3-1}))^2}{3\partial p_1^2(t)\partial p_2^2(t + \Delta \phi_{2-1})\partial p_3^2(t + \Delta \phi_{3-1})}$$
(2)

As with lag time residual analysis, the average semblance value is computed for 5 s windows overlapping by 4 s where *x*, *y*, and *z* are functions of LFD.



Figure 5. Fifteen minute detail of advancing lahar. (a) Captions and colormap values are the same as for Figure 4b. (b) Captions and colormap values are the same as for Figure 4f. Linear regression $(38 \pm 1 \text{ m/s})$ is calculated for indicated 270 s. Animation of the corresponding source movement is provided in supporting information materials.

3.2. Lahar Dynamics Inferred From Infrasound

The source of sound signal prior to 03:25 local time on 3 March is synchronous and principally colocated with Villarrica's summit activity. Starting at 03:26.0, however, lag-based locations appear to migrate systematically downslope toward the north. The earliest detected CT lahar source thus occurs at ~03:25.5 given a ~30 s propagation time. Notably, the summit eruptive activity diminishes between 03:25 and 03:28 coinciding with the approximate onset of the lahar.

From 03:26.5 to 03:31.0 the lag-based source moves rapidly from ~2 km to 12 km at an average speed of 38 ± 1 m/s, or 137 ± 3 km/h (95% confidence interval). The moving source appears to maintain a relatively constant speed despite a decrease in slope from 20° to 4° over this distance. If this movement corresponds to the translation of a flow surge downslope,

it represents the high end of previously measured lahar velocities but is within the bounds of lahars flowing close to a volcano and on steep slopes. Though it is higher than the averaged speeds of the 1985 Nevado del Ruiz lahars (5–15 m/s [*Lowe et al.*, 1986]), as well as lahars measured at Ruapehu in 2007 (less than 16 m/s [*Lube et al.*, 2012]) and those inferred at Popocatepetl, Mexico (1–14 m/s [*Munoz-Salinas et al.*, 2007]), it is consistent with proximal lahar velocities (30–40 m/s) determined at Mount St. Helens [*Pierson*, 1985]. We propose that Villarrica lahar tracking during the initial 5 min could correspond to the energetic bow wave and/or head, which contains the bulk of the kinetic flow power [*Lube et al.*, 2012]. After 03:31.0 the mapped lag-time sound source locations cease to advance rapidly and remain relatively fixed within a LFD range of ~10–13 km.

After 03:31 until approximately 05:30 coherent sound remains detectable and appears to originate from a LFD range of ~10 to 12 km and also at >16 km, where precise location is ambiguous due to the distal LFD uncertainty discussed previously. The source distribution at 10–12 km is close to, but not precisely coincident with, two substantial CT waterfalls (with drops of more than 10 m) located at 9.2 and 10.3 km LFD. Notably, this source range also coincides with a topographic saddle in the intervening Cerduo cordillera (see Figure 2a). We speculate that substantial lahar sound may be generated at the waterfalls and throughout the canyon between 10 and 12 km but that it preferentially diffracts around the 11.1 km LFD saddle. Toward 05:00 the sources appear to shift slightly downstream and cluster between 11.5 and 12.0 km and near the terminus of the CT canyon, from where sound is able to propagate near line of sight to Array VIH.

Throughout this period, when sources remain between 10 and 12 km, the flow tremor intensity diminishes while the centroid frequency remains fixed at about 10 Hz. This is suggestive of a stable source dimension but potentially diminished flow discharge. Notably, the last detections at ~11 km are at about 04:30 and the last detections at ~12 km are at ~05:00, whereas detections further downstream at 16 km continue until at least 05:30. This, together with semblance-inferred source localization, suggests the gradual downstream translation of the sound-generating lahar.

Semblance-inferred sources yield crude spatial resolution but may give a sense of the (broad) distribution of potential sources along the CT flow channel. Following the flow initiation (from 03:26 to 03:31), we observe distributed regions of high semblance values suggestive of sound that is produced along an extended LFD.

Starting at ~03:40 semblance remains highly along the entire active flow length (out to more than 16 km), but by around ~04:00 semblance diminishes in the upper CT as the bulk of the active lahar migrates downstream. By ~04:30 high semblance values indicate sources primarily at 10 km or further downstream.

4. Discussion: Potential for Infrasound Flow Monitoring

Villarrica's 3 March lahar in the CT drainage has a clear acoustic fingerprint that could be used as part of an early warning system. Both the spectral character of the lahar and, more significantly, the changing interarray-correlated time lags distinguish its genesis from that of summit eruptive activity and point to a moving source. The envelope of the lahar signal, and its evolving frequency content, is reminiscent of non-volcanic debris flows studied in the European Alps using a single infrasonic microphone and geophone [Kogelnig et al., 2014]; that study demonstrated a clear correlation between distinct flow surges and infrasonic tremor intensity. In the case of the CT an infrasound warning of a propagating lahar might be generated some 30–60 min prior to, or 12–15 km above, the flow's impact with the critical international highway bridge over the Turbio River. The 3 March event did not damage this bridge, but larger events would put this bridge, as well as residential developments further downstream, in jeopardy.

The 3 March lahar signal was well detected by a single three-element acoustic array for a range of distances (2 to 16 km LFD) and despite significant intervening topography (from 6.5 to 13 km LFD). These results attest to the remote sensing potential of this technology; however, we conclude that proper localization of an acoustic surveillance array, or arrays, is critical. A limitation of the Array VIH site was its inability to resolve source locations beyond ~16 km. Future source tracking ambiguity could be ameliorated by more selective location of the array (or arrays). Notably, other nearby Villarrica infrasound arrays, which were located further from the distal portions of the CT and behind significant topography, failed to clearly identify the CT event. These observations argue for implementation of infrasound array monitoring in multiple drainages where hazards might be expected.

Further work relating empirical observations of lahar flow to acoustic radiation is necessary and might also lead to real-time assessments of flow size and hazard. Future study should also include acoustic monitoring that extends above the traditional band of volcano infrasound used for eruption detection [*Johnson and Ripepe*, 2011]. This will require higher sampling rates and experimentation with potentially smaller array apertures to optimize signal coherence, and avoid aliasing, for higher frequency recordings.

5. Conclusions

The 3 March lahar of the CT drainage was tracked acoustically from near source to more than 13 km flow distance. Important constraints on initial flow speed ($38 \pm 1 \text{ m/s}$) were afforded by a single 25 m aperture, three-element array. The moderate-sized CT lahar remained detectable for more than 2 h despite the fact that the lahar flow path was 4–10 km from Array VIH and much of its length, from 6.5 to 13 km LFD, was not directly within line of sight. Lahar intensity and frequency content is greatest during the initial lahar advance. The abundance of coherent high-frequency energy argues for the usage of both infrasound and low-frequency audio band monitoring.

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