# AN INVESTIGATION OF CARRIER TRANSPORT IN HAFNIUM OXIDE/SILICON DIOXIDE MOS GATE DIELECTRIC STACKS FROM 5.6-400K

By

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A dissertation

submitted in partial fulfillment

of the requirements for the degree of

Doctor of Philosophy in Electrical and Computer Engineering

Boise State University

December 2010

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### BOISE STATE UNIVERSITY GRADUATE COLLEGE

## **DEFENSE COMMITTEE AND FINAL READING APPROVALS**

of the dissertation submitted by

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Date of Final Oral Examination: 13 August 2010

The following individuals read and discussed the dissertation submitted by student Richard G. Southwick III, and they also evaluated his presentation and response to questions during the final oral examination. They found that the student passed the final oral examination, and that the dissertation was satisfactory for a doctoral degree and ready for any final modifications that they explicitly required.



The final reading approval of the dissertation was granted by William B. Knowlton, Ph.D., Chair of the Supervisory Committee. The dissertation was approved for the Graduate College by John R. Pelton, Ph.D., Dean of the Graduate College.

#### ACKNOWLEDGEMENTS

<span id="page-3-0"></span>The completion of this dissertation would not be possible without the encouragement, support, and help of many individuals. I would like to thank my advisor Dr. William Knowlton for taking me on as an undergraduate in his research group. Dr. Knowlton graciously allowed me to continue my graduate studies working in his lab offering countless avenues to learn and grow. I have had the privilege of benefiting from Dr. Knowlton's mentorship and his encouragement has been valued and edifying during this undertaking. My appreciation is extended to Dr. Gennadi Bersuker, who has provided samples for this study, been very supportive of this work, and provided excellent discussions and feedback. I am grateful to Dr. Wan Kuang, Dr. R. Jacob Baker, Dr. Maria Mitkova, Dr. Elton Graugnard, Dr. Bernard Yurke, Dr. William Hughes, and Dr. Eric Vogel for all the support amidst the many demands on their time.

I am thankful to the many fellow students that I have had the privilege to work with. In particular, I would like to thank Ross Butler and Justin Reed. I am also grateful for Hieu Bui, Chris Buu, Shem Purnell, Blake Rapp, and Ryan Thompson who have helped with the measurement process.

To my family, whom I cherish the most, your support is most needed and appreciated. In addition, I recognize and honor the Almighty who sustains us all.

### ABSTRACT

<span id="page-4-0"></span>Hafnium oxide (HfO<sub>2</sub>) is replacing silicon dioxide (SiO<sub>2</sub>) as the gate dielectric in metal oxide semiconductor (MOS) structures driven mainly by need to reduce high leakage currents observed in sub-2nm  $SiO_2$ . The high dielectric constant of HfO<sub>2</sub> (~25) compared to  $SiO<sub>2</sub>$  (3.9 bulk) allows a thicker HfO<sub>2</sub> layer to be used in place of the thinner  $SiO<sub>2</sub>$  layer thereby reducing the gate leakage current in MOS devices while maintaining the same capacitive coupling provided by the thinner  $SiO<sub>2</sub>$ . However, incorporating HfO<sub>2</sub> into MOS devices produces a  $SiO<sub>2</sub>$  interfacial layer between the Si substrate and HfO<sub>2</sub> interface. The increased complexity of the multilayer dielectric gate stack and introduction of new materials requires knowledge of the carrier transport mechanisms for accurate modeling and process improvement.

A large temperature dependence of the leakage current in  $HfO<sub>2</sub>$  gate dielectrics are observed compared to  $SiO<sub>2</sub>$ , indicating temperature dependent leakage current measurements maybe well suited to understand the transport mechanism of  $HfO<sub>2</sub>$ -based gate dielectrics. The leakage currents are measured for two different titanium nitride (TiN) metal gate stacks composed of either 3nm or 5nm  $HfO<sub>2</sub>$  on 1.1nm SiO<sub>2</sub> interfacial layer over temperatures ranging from 6K to 400K. For gate biases that yield equivalent electron energy barriers for the 3nm and 5nm  $HfO<sub>2</sub>$  gate stacks, the 5nm stack shows orders of magnitude less current and an order of magnitude larger increase in the gate leakage current with respect to temperature from 5.6K to 400K.

Knowledge of the energy band structure is crucial in determining what carrier transport mechanisms are plausible in multilayer dielectric stacks. Important parameters, necessary for modeling different transport mechanisms, can be extracted from accurately constructed energy band diagrams such as electric fields and barrier heights. An existing program developed by the author is further modified to incorporate image charge effects, multilayer dielectrics, and transmission coefficient calculations for use in this study.

Results indicate that the widely used Poole-Frenkel and Schottky conduction mechanisms for  $HfO<sub>2</sub>$  dielectrics can only explain a narrow electric field and temperature range and fail to explain the observed thickness dependence. Modeling the temperature dependence of 3nm and 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub> n/pMOSFETs$  with a combination of a temperature independent term, variable range hopping conduction, and Arrhenius expression (e.g., nearest neighbor hopping) describes the entire measured temperature range (6K to 400K). Additionally,  $HfO<sub>2</sub>$  defect densities can be extracted using the proposed model and provide densities in the range of  $\sim 10^{19}$  to  $\sim 10^{21}$  cm<sup>-3</sup>eV<sup>-1</sup>, which correlate well with defect densities reported in the literature. Defects in the  $HfO<sub>2</sub>$  are likely a result of oxygen vacancies.

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#### CHAPTER 1: INTRODUCTION

<span id="page-18-0"></span>Hafnium oxide (HfO<sub>2</sub>) is replacing silicon dioxide (SiO<sub>2</sub>) as the gate dielectric of choice in metal oxide semiconductor (MOS) structures [1] due to the high dielectric constant (high-*k*) value of HfO<sub>2</sub> ( $\sim$ 25) compared to SiO<sub>2</sub> (3.9 bulk). The dielectric constant of  $HfO<sub>2</sub>$  has reduced the gate leakage current in MOS devices by replacing thinner  $SiO_2$  with thicker  $HfO_2$  while retaining desired device performance. However, the growth of HfO<sub>2</sub> on silicon (Si) generates a sub-nanometer thick  $SiO<sub>2</sub>$  interfacial layer (IL) leading to a dielectric bilayer (i.e.,  $HfO<sub>2</sub>-IL-Si$ ) [2] that increases 1) the complexity of the energy bands, and 2) the electrically active point defect concentration as compared to  $SiO<sub>2</sub> MOS$  devices. Due to the increased complexity of MOS devices incorporating HfO<sub>2</sub>, new questions arise. One of these fundamental questions is: what are the carrier transport mechanisms through the gate stack? This question does not only apply to  $HfO<sub>2</sub>$  but also to other dielectric materials that are quickly being integrated into other novel devices, such as multilayer dielectrics [3] and non-volatile memory [4-6]. The answer to this question could result in lower gate leakage current, providing: cooler devices, lower power consumption, longer battery life, and increased portability.

For the case of transport properties in  $HfO<sub>2</sub>$ , a strong temperature dependence has been observed [7-9]. [Figure 1.1](#page-19-0) shows the temperature dependence of a  $HfO<sub>2</sub>$  gate stack (red data) compared to that composed of only  $SiO<sub>2</sub>$  (black data) as the gate dielectric [10]. Increased temperature dependence of the gate leakage current in the  $HfO<sub>2</sub>$  device is observed as compared to the  $SiO<sub>2</sub>$  device [\(Figure 1.1\)](#page-19-0). Comprehending the conduction

mechanism in high-*k* materials has become of interest to the scientific community not only to understand the materials performance, but to understand the underlying physics and thus the material's limitations [9, 11-13]. Conduction or transport mechanisms (i.e., the kinetics) in materials are generally thermally activated, thus temperature dependent studies remain a key tool to understanding transport mechanisms.



<span id="page-19-0"></span>Figure 1.1: Gate leakage current for nMOSFETs composed of a  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate dielectric stack and a  $SiO<sub>2</sub>$  gate dielectric for various temperatures ranging from 6 - 300K. The  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate dielectric shows larger temperature dependence (red) than  $SiO<sub>2</sub>$  (black) at both positive and negative gate biases. Similar to [10].

For the general case of current transport in high-*k* dielectrics, many temperature dependent studies have been performed on silicon nitride [14, 15], titanium oxide [16], aluminum oxide [17], europium oxide [18], zirconium oxide [19], hafnium oxide [9, 11, 20-22], and others to determine the transport mechanism. Traditional temperature dependent transport mechanisms in high-*k* dielectrics have focused primarily on Poole-Frenkel emission [23-26], Schottky emission [7, 23], ohmic, and ionic conduction [27]. Since high permittivity materials are being used as a gate dielectric replacement material, it has been suggested by theory that polarons, electron-phonon interactions, could play a significant role in current conduction [28, 29]. As electron-phonon interactions are thermally activated, temperature dependent measurements are appropriate for examining potential polaron mediated transport. For more information regarding polarons, see Appendix A.

Despite the large amount of temperature dependent work performed to understand carrier transport in  $HfO<sub>2</sub>$  (the high- $k$  material that has received the most attention), the majority of the work has focused on above room temperature measurements with few studies analyzing transport below room temperature and even fewer at cryogenic temperatures below 77K. This leaves a significant portion of temperatures from near 0K to room temperature that has yet to be thoroughly examined and utilized in determining the carrier transport mechanism. Measurements performed near 0K have the added benefit of reduced thermal smearing of the Fermi energy level  $(E_f)$  relative to room temperature or even 77K, providing an appreciably sharper energy probe [\(Figure 1.2\)](#page-21-0).

For work performed on  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate dielectrics, many transport mechanisms have been suggested and include: Poole-Frenkel transport [7, 30-32], Schottky emission [7, 33, 34], polaron transport [35-37], quantum mechanical tunneling [30], and trap assisted tunneling [30, 38] among others. These studies highlight the lack of consensus in the field. It is evident that a comprehensive study has yet to be performed that has identified carrier transport regimes over large temperature and voltage regimes. The aim of this study is to identify carrier transport mechanisms over a broad temperature and voltage regime.



<span id="page-21-0"></span>Figure 1.2: Thermal broadening function [39],  $F_T(E) = \partial_E f(E)$ , as a function of *E-E<sub>f</sub>* at 5.6K, 77K, and 300K. The energy distribution at 5.6K is significantly narrower allowing the  $E_f$  position to be known much more accurately.

Employing a variable temperature probe station, the carrier transport in 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> and 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> MOS dielectric stacks from 5.6-400K is investigated. Results reveal regimes where carrier transport is dominated by either carrier-limited transport or conduction path-limited transport. For conduction pathlimited transport, an approach suggested by the most common mechanisms used in the literature to explain the temperature dependence of the gate leakage current is taken to analyze the wide temperature and voltage range data measured in this study. First Poole-Frenkel analysis is performed followed by Schottky analysis. Results indicate that Poole-Frenkel transport is capable of describing the data in a limited voltage and temperature range and Schottky emission does not describe the temperature and voltage dependence of the gate leakage current. Using mechanisms suggested by temperature dependent carrier transport studies of disordered materials by the physics community, hopping

analysis is performed. Results indicate that the full temperature and voltage regime for conduction path-limited transport can be described using a variable range hopping term, Arrhenius term, and temperature independent term. Inconsistencies in the fit parameters of the variable range hopping term and the Arrhenius term are identified and proposed as further areas of research.

This study is presented in nine chapters. In the following chapter, an introduction to various transport mechanisms is presented. Chapter 3 details the instrumentation, software, test devices, and experimental procedures used to measure and analyze carrier transport. Chapter 4 describes the development of an energy band simulation tool useful in analyzing multilayer dielectric stacks in metal-insulator-metal and MOS stacks. Chapter 5 gives experimental results and observations to the behavior of the temperature dependence of the gate leakage current. Chapters 6, 7, and 8 explore three transport mechanisms (Poole-Frenkel, Schottky, and hopping conduction) as possible explanations of the gate leakage current and its temperature dependence. Finally, Chapter 9 summarizes important points and offers some directions for future work.

#### CHAPTER 2: TRANSPORT MECHANISMS

<span id="page-23-0"></span>There are many carrier transport mechanisms all of which are influenced by temperature to some degree. The following subsections address the most common transport mechanisms.

#### <span id="page-23-1"></span>**2.1: Direct Tunneling (DT) and Fowler-Nordheim Tunneling (FNT)**

The most basic carrier transport mechanisms, which account for the majority of the leakage current in  $SiO<sub>2</sub>$  based dielectrics, are purely quantum mechanical in nature and include direct tunneling (DT) and Fowler-Nordheim tunneling (FNT). [Figure 1.1](#page-19-0) shows the energy band diagrams for a  $SiO<sub>2</sub> MOSFET$  at flat-band (a), in DT (b), and in  $FNT(c)$ .

Tunneling through the full width of the dielectric (i.e., trapezoidal barrier) is DT [\(Figure 2.1b](#page-24-0)), while tunneling through a triangular barrier is FNT [\(Figure 2.1c](#page-24-0)). Although quantum mechanical tunneling is not temperature dependent to first order, higher order temperature dependent factors do exist. These parameters include 1) the effective mass in the gate electrode, dielectric, and semiconductor; 2) the number of minority and majority carriers in the semiconductor; and 3) the energy of the minority and majority carriers. These parameters result in weakly temperature dependent carrier transport via quantum mechanical tunneling.



<span id="page-24-0"></span>through the gate dielectric takes place at the full width of the gate dielectric compared to (c) FNT – tunneling through a triangular barrier, which reduces the tunneling distance, created using [40].

For a single barrier, the mathematical description of FNT can be simplified as [41,

42]:

<span id="page-24-1"></span>
$$
J_{FN} = B_{FN} E_{ox}^2 \exp\left(-\frac{C_{FN}}{E_{ox}}\right) \tag{2.1}
$$

where

<span id="page-24-2"></span>
$$
B_{FN} = \frac{q^3}{16\pi^2 \hbar \phi_B} \left(\frac{m^*}{m_e}\right), \ C_{FN} = \frac{4\sqrt{2m^* \phi_B^3}}{3q\hbar}, \tag{2.2}
$$

and *q*,  $\hbar$ ,  $\phi_B$ ,  $E_{ox}$ , and  $m^*$  are the charge of an electron, reduced Planck's constant, barrier height between the oxide and semiconductor, the electric field in the oxide, and the effective mass of the electron in the oxide. Examining the simplified FNT equation in

<span id="page-25-0"></span>[\(2.1\)](#page-24-1) and [\(2.2\)](#page-24-2), no direct temperature term is observed. However,  $E_{ox}$ ,  $m^*$ , and  $\phi_B$  all are slightly temperature dependent.

#### **2.2: Variable-Range and Nearest-Neighbor Hopping Conduction**

If defects exist in the oxide, carriers can move from one defect to another using the defects as "stepping stones" to pass through the oxide. If a carrier tunnels through the oxide using just one defect "step", the transport mechanism is typically called trap assisted tunneling [\(Figure 2.2\)](#page-25-1) and it is considered a two-step tunneling process [43].



<span id="page-25-1"></span>Figure 2.2: Energy band diagram [40] showing trap-assisted tunneling, using the presence of a defect in the oxide as a "stepping stone" for tunneling.

Conversely, if many defect traps exist, an impurity defect band is formed within the oxide and conduction takes place similar to transport in the conduction band (i.e., unbound or delocalized states) with an effective mass associated with the impurity band. Between these two carrier transport extremes exists the regime known as hopping conduction, which was first described by P.W. Anderson [44]. At electronic energy states near the Fermi energy, thermally activated electrons hop from one localized state to another. The probability of an electron hopping from a state below the Fermi energy to a state above the Fermi energy level depends on three factors [45]:

- a. The Boltzmann's factor  $\exp(-\Delta E_{trap}/k_bT)$ , where  $\Delta E_{trap}$  is the energy difference between the two states,  $k_b$  is Boltzmann's constant, and  $T$  is temperature.
- b. The probability of absorbing a phonon,  $v_{ph}$ , of the proper energy, which depends on the phonon spectrum.
- c. A probability factor that depends on the overlap of the wave functions of the two states,  $exp(-2\alpha R)$ , where *R* is the distance between the states and  $\alpha$  is the inverse decay length of the localized state.

The distance to which the carrier must hop increases as the temperature decreases. This conduction mechanism is also referred to as phonon-assisted hopping and the probability of hopping is given as [45, 46]:

<span id="page-26-0"></span>
$$
v_{ph} \exp\left(-2\alpha R - \frac{\Delta E_{trap}}{k_b T}\right).
$$
 (2.3)

At high temperatures, the temperature term dominates and carriers jump to the nearest localized state since the  $exp(-2\alpha R)$  term falls off quickly. This type of hopping conduction is called nearest neighbor hopping (NNH) conduction [47, 48] [\(Figure 2.3a](#page-27-0)). As the temperature decreases, insufficient energy is present to cause a transition from a lower to a higher energy state. Known as variable range hopping (VRH) conduction, carriers can then only hop to energy states of similar energies [\(Figure 2.3b](#page-27-0)).



<span id="page-27-0"></span>Figure 2.3: Energy band diagram<sup>[1](#page-27-1)</sup> showing localized states around the Fermi energy,  $E_f$ . The energy of the conduction band,  $E_c$ , and the valance band energy level,  $E_v$ , are also shown. Nearest neighbor hopping conduction is shown in part (a) while variable range hopping conduction is shown in part (b).

The distance to which the carrier must hop increases as the temperature decreases.

An increase in hopping distance as a function of decreasing temperature was first identified by Mott [47, 48]. Mott's treatment of identifying the optimal hopping distance resulted in a  $T^{1/4}$  dependence [45]. Many other approaches have been considered in modeling hopping conduction, including the application of percolation theory and for the three dimensional case all predict a  $T^{1/4}$  temperature dependence [45, 49]. It has been suggested that an arbitrary *d*-dimensional case for variable range hopping conductivity exists and is given by [46]:

$$
\sigma = \sigma_{hop} \exp\left(-\left(\frac{T_0}{T}\right)^{\frac{1}{d+1}}\right) \tag{2.4}
$$

<span id="page-27-2"></span>where  $T_0$ , the characteristic temperature, is given by:

<span id="page-27-1"></span><sup>&</sup>lt;sup>1</sup> In crystalline materials, the density of states for valence electrons (valance band) and excited electrons (conduction band) are sharply defined. The energy difference between the top of the valance band and the bottom of the conduction band is defined as the band gap. In highly disordered semiconductors and insulators (i.e., amorphous or poly-crystalline), the density of states for valence electrons and excited electrons are not well defined (due to disorder in the bonding) and result in localized tail states. Rather than band edges and gaps, highly disordered materials use the analogy of mobility edges and a mobility gap. [Figure 2.3,](#page-27-0) depicting hopping conduction, has been draw as a crystalline insulator for simplicity but is also applicable to highly disordered insulators.

11

$$
T_0 = \frac{Ad}{2\alpha k_b N(E_F)} \left(2\alpha \left(\frac{d+1}{d}\right)\right)^{d+1} \tag{2.5}
$$

and *A* and  $\sigma_{hop}$  are constants with  $N(E_F)$  the density of states about the Fermi energy. For two dimensional hopping conduction, the temperature dependence would be  $T^{1/3}$ .

Hopping conduction can occur in both crystalline materials (as shown in [Figure](#page-27-0)  [2.3](#page-27-0) for simplicity) and highly disordered materials. In crystalline materials, defects are introduced into the band gap by impurities or structural defects in the lattice. In addition to impurities, amorphous materials have defects in the mobility gap (analogous to band gap in crystalline materials), due to the random orientation of the atoms and unsatisfied bonds. Much of the work leading to descriptions of variable range hopping conduction and nearest neighbor hopping conduction was done on amorphous materials. Variable range hopping and nearest neighbor hopping are especially applicable to the system of dielectrics studied here  $(SiO<sub>2</sub>$  and  $HfO<sub>2</sub>)$  as they are both disordered systems.

#### **2.3: Poole-Frenkel Conduction**

<span id="page-28-0"></span>Poole-Frenkel (P-F) conduction or emission [24-26] acts to modify the potential well of trapped carriers. This modification is a result of high electric fields, which lowers the ionization energy [45] or the energy for thermal stimulation of electrons into the conduction band [27]. Frenkel, building on the previous work of Poole [24-26], showed that the trap barrier height  $(\phi_{PF})$  is lowered by [50]:

<span id="page-28-1"></span>
$$
\Delta \phi_{PF} = \beta_{PF} E_{ox}^{1/2} \tag{2.6}
$$

where

$$
\beta_{PF} = \left(\frac{q^3}{\pi \varepsilon_0 \varepsilon_r}\right)^{1/2},\tag{2.7}
$$

 $\varepsilon_0$  is the permittivity of free space, and  $\varepsilon_r$  and is the high frequency (i.e., dynamic) dielectric constant [51, 52]. [Figure 2.4](#page-30-0) shows a diagram illustrating the reduction in the potential well of a trap in the presence of an electric field.

The derivation of the energy potential lowering effect [\(2.6\)](#page-28-1) depends on the hydrogenic potential. That is, the standard P-F mechanism incorporates the concept of a hydrogenic impurity for which the ionization energy potential is determined using the effective mass approximation [53-55]. The hydrogenic impurity includes both a charged ion impurity and a charged trapped carrier, which interact with each other. In his model, Frenkel only considered electrons and donor traps [24]. However, in the effective mass approximation, the difference between the hydrogenic ionization energy potential for an electron and hole is simply the effective mass of the respective carriers. Hence, there is no reason why the P-F model cannot be applied to holes as it is applied to electrons. A widely accepted mathematical expression for the standard P-F conduction  $(J_{PF})$  can be written as:

$$
J_{PF} = CE_{ox}e^{-\frac{q\phi_{PF} - \beta_{PF}\sqrt{E_{ox}}}{\xi k_b T}},
$$
\n(2.8)

where  $C$ ,  $k_b$ ,  $T$ , and  $\xi$ , are a constant, Boltzmann's constant, temperature, and a factor that depends on acceptor compensation [52, 56], respectively. The value of *ξ* is usually between 1 and 2. In Frenkel's original paper,  $\zeta = 2$ . In much of the literature,  $\zeta = 1$  (e.g., [20, 23, 33, 38, 41, 57-59]), which corresponds to heavily compensated traps [52].



<span id="page-30-0"></span>Figure 2.4: Energy band diagram showing Poole-Frenkel emission. As the electric field in the dielectric increases, the trap barrier is lowered. As the temperature increases, the trapped carrier has more energy and can more easily overcome the barrier. Created using [40].

The potential lowering effect of Poole-Frenkel emission has been applied to variable range hopping conduction by adding the  $E_{ox}$ <sup>1/2</sup> dependence in the exponential [45, 46]. Poole-Frenkel conduction dominates at high temperatures, where enough thermal energy is available to stimulate the carrier over the barrier, and high fields, where the barrier is significantly lowered [27]. At extremely high electric fields, the electron can hop downward without thermal activation yielding [45, 60]:

$$
\sigma \propto \sigma_{hop2} \exp\left(-B/E_{ox}^{1/4}\right) \tag{2.9}
$$

where  $\sigma_{hop2}$  and *B* are constants.

#### **2.4: Schottky Emission**

<span id="page-31-0"></span>Emission of the carrier over the dielectric barrier ( $\phi_B$ ) and into the dielectric conduction band is known as thermionic emission. The barrier the charged carrier overcomes is lowered in the presence of an electric field due to the image charge theorem (discussed in Section [4.1.4\)](#page-49-0). Thermionic emission over an electric field assisted lower barrier is known as Schottky emission. [Figure 2.5](#page-32-1) shows an energy band diagram of Schottky emission in a MOS gate stack composed of a single dielectric. The dashed line in [Figure 2.5](#page-32-1) represents the barrier to electrons without considering image charge effects while the solid line considers image charge effects due to the metal gate.

Schottky emission can be modeled using the following equation [27, 41]:

<span id="page-31-1"></span>
$$
J_{SE} = A * T^2 \exp\left(\frac{-q(\phi_B - \sqrt{qE_{ox}/4\pi\varepsilon_0 \varepsilon_r})}{k_b T}\right)
$$
(2.10)

where  $\varepsilon_r$  is the high frequency dielectric constant and  $A^*$  is the effective Richardson constant given by [41]:

$$
A^* = \frac{4\pi q m^* k_b^2}{h^3} \tag{2.11}
$$

The parameters *h* and  $\phi_B$  are Planck's constant and the barrier height between the semiconductor conduction band and the dielectric conduction band, respectively.



<span id="page-32-1"></span>Figure 2.5: Energy band diagram depicting Schottky emission of an electron moving from the metal gate to the  $SiO<sub>2</sub>$  $SiO<sub>2</sub>$  $SiO<sub>2</sub>$  conduction band.<sup>2</sup> The Schottky emission process is similar to thermionic emission with the charged carrier barrier lowered by the presence of an electric field and the image charge theorem. Created using [40].

#### **2.5: Determining the Conduction Mechanism**

<span id="page-32-0"></span>Determining which conduction mechanism is present in a dielectric is primarily determined by fitting experimental data to the various conduction mechanism equations shown above. Establishing which transport mechanisms are present is difficult as several transport mechanisms can occur simultaneously, which can distort experimental results. To deconvolute multiple transport mechanisms, it becomes necessary to characterize the dielectric under a wide variety of conditions where one transport mechanism can dominate over the others thereby simplifying the identification of the dominant mechanism.

<span id="page-32-2"></span> $2$  As will be shown later in Section [4.1.4](#page-49-0) and Chapter 7, the effects of image charge from both dielectric interfaces (not shown in [Figure 2.5\)](#page-32-1) should be considered in ultra thin dielectrics.

The simplest method for measuring the conduction current is via a current-voltage (I-V) sweep. There is a wide array of equipment available to perform such a measurement and the measurement is relatively quick. Many of the conduction mechanisms discussed have a voltage or electric field dependence. These transport mechanisms include: FNT, Poole-Frenkel, and Schottky conduction. Understanding the behavior of the conduction current as a function of voltage is crucial to identifying which transport mechanism is responsible. Many transport mechanisms dominate under certain voltage conditions. For example, FNT dominates DT at high electric fields.

In addition to a voltage dependence, most of the transport mechanisms discussed have a temperature dependence (i.e., *T* in [\(2.3\)](#page-26-0), [\(2.4\)](#page-27-2), and [\(2.10\)](#page-31-1)). Hence, most carrier transport studies are performed at room temperatures and above (e.g., [7, 22, 23, 61]). This study focuses on deconvoluting multiple transport mechanisms in a complex dielectric system by incorporating 1) a temperature range from cryogenic to above room temperature, and 2) a broad range of voltages.

#### CHAPTER 3: EXPERIMENTAL PROCEDURE

<span id="page-34-0"></span>In this section, the software and instrumentation used in this study are described. Briefly discussed are: 1) an analytical software package in which significant scripts were coded to analyze large experimental data sets, and 2) the development of a onedimensional multilayer: metal/oxide/semiconductor simulation software to understand the underlying physics of multilayer dielectric MOS structures. The latter will be described in greater detail in Chapter 4. Additionally, various hardware components used are presented as well as the test devices. Finally, the experimental procedure is discussed.

#### **3.1: Software**

<span id="page-34-1"></span>Analysis, manipulation, and visualization of the experimental results primarily occurred using OriginPro  $8.0^3$  $8.0^3$ . Custom fitting routines using OriginPro's non-linear curve fitting toolbox were written to compare experimental results to various transport mechanisms described in Chapter 2. Custom data manipulation code was also written to minimize human error and increase the amount of data that can be examined. The amount of custom code written, leveraging the power of OriginPro, results in over 14,000 lines of code, 80% of which has been written by the author.

A primary means of understanding and explaining the various transport mechanisms that can occur in advanced devices is facilitated through energy band diagrams (e.g., [Figure 2.1](#page-24-0) - [Figure 2.5\)](#page-32-1). Calculating the energy band diagram as a result

<span id="page-34-2"></span><sup>&</sup>lt;sup>3</sup> OriginPro is a registered trademark of OriginLab.

of various gate voltages requires extensive knowledge of device physics. Even using simple analytical solutions for modeling MOS capacitor operation requires the simultaneous solution of many interdependent equations. The complexity of the energy band diagram increases as additional dielectric layers are added to the gate stack of MOS devices. To address these needs, a program was developed capable of constructing a gate stack with multiple dielectric layers and identifying 1) tunneling mechanisms, 2) voltage drops, 3) electric fields, 4) charge distributions, 5) potential, 6) image charge effects, and 7) quantum mechanical tunneling transmission coefficients among other physical parameters (discussed in Chapter 4), expanding on a previous version of the program also written by the author [40].

#### **3.2: Instrumentation**

#### <span id="page-35-1"></span><span id="page-35-0"></span>3.2.1: Electrical Measurement Instrumentation

Electrical characterization of the high-*k* gate MOSFETs were performed with the Keithley 4200 Semiconductor Characterization System (SCS) shown in [Figure 3.1.](#page-36-1) The Keithley 4200SCS is a precision DC voltage-current source and measurement unit capable of either 1) sourcing voltage and measuring current, or 2) sourcing current and measuring voltage. Four medium power source monitoring units (SMU) are included in the Keithley 4200 capable of sourcing up to 20V with 100mA of current. Four pre-amps are attached to the SMUs for additional current sensitivity down to 100aA resolution with 10fA accuracy. The four SMUs allow all four MOSFET terminals (gate, drain, source, well/substrate) to be measured simultaneously. For capacitance-voltage (C-V) measurements, the Agilent 4284 LCR meter was used.


Figure 3.1: Keithley 4200 Semiconductor Characterization System used to measure device characteristics in this study.

## 3.2.2: Probe Station

A Janis Research custom built variable temperature probe station (5.6-450K) with four actively cooled (to limit heat injection into the devices) triaxial Kelvin probes was used for all measurements. The probe station is designed for low current sensitivity with a noise floor ~10fA. The low noise floor of the station is ideally suited for measuring the low current levels of gate leakage currents. The excellent DC characteristics have tradeoffs with the AC characteristics of the system, which has a 3dB roll-off at ~10MHz. Experiments were performed under vacuum, necessary to reach the temperatures studied here, and under light tight conditions. The variable temperature probe station with supporting electrical instrumentation, including the Keithley 4200SCS, is shown in [Figure 3.2.](#page-37-0) The small 5 cm sample chuck [\(Figure 3.2](#page-37-0) inset) required that the wafer containing the MOS devices to be cleaved. Select devices were tested on a room temperature probe station (Micromanipulater Model 6200) before and after wafer cleaving to verify that the cleaving process did not damage the devices. Grounding mats

and electro-static discharge (ESD) boots straps were worn to protect the devices from

ESD damage.



<span id="page-37-2"></span><span id="page-37-0"></span>Figure 3.2: Variable temperature probe station and supporting equipment. Inset shows where the samples are placed and probed.

# **3.3: Devices**

The MOSFET test devices used in this study were fabricated by SEMATECH<sup>[4](#page-37-1)</sup> using a standard self-align process on epitaxial Si-substrate. A chemical  $SiO<sub>2</sub>$  IL was grown by treating Si with  $O_3$ . Hf $O_2$  was deposited using atomic layer deposition for thicknesses of 3 and 5nm. Using chemical vapor deposition, 10nm of titanium nitride

<span id="page-37-1"></span> $\frac{1}{4}$ <sup>4</sup>SEMATECH is an international semiconductor manufacturing consortium which performs advanced research and development on semiconductor devices based in Austin, TX, USA.

(TiN) was used as a metal gate capped by 150nm of amorphous Si. Source/drain junctions were activated using temperatures of 1000ºC for 10 seconds followed by a post metal forming gas anneal for 30 minutes at 480ºC [62].

A SiO2 control wafer was also fabricated using the exact same wafer processing described above with the exception of the dielectric stack, which is composed of a 2.0nm thermal  $SiO<sub>2</sub>$  *in situ* steam generated oxide at 950 $^{\circ}$ C. The control wafer was used to establish gate leakage current comparisons between high- $k$  and  $SiO<sub>2</sub>$ , as well as associated temperature dependencies. [Table](#page-38-0) 3.1 shows wafer split information.

Split	Interfacial Layer Material	High- $k$ Material	Gate Material
	1.1nm chemical $SiO2$	$3$ nm HfO <sub>2</sub>	TiN
	1.1nm chemical $SiO2$	$5$ nm HfO <sub>2</sub>	TiN
	2.0nm thermal $SiO2$	-	TiN

<span id="page-38-0"></span>**Table 3.1: Wafer Split Information**

In addition to wafer fabrication, SEMATECH has performed some characterization tests to quantify the dielectric constant of the  $HfO<sub>2</sub>$  and IL using high resolution-electron transmission microscopy (HR-TEM) micrographs and C-V tests. Flatband and EOT were extracted using the North Carolina State University (NCSU) methodology [63]. The data (shown in [64]) gives the extracted EOT from the capacitance-voltage tests for each  $HfO<sub>2</sub>$  layer thickness. The equivalent oxide thickness  $(EOT)^5$  $(EOT)^5$  of the dual layer dielectric can be described by:

$$
EOT_{HfO_2/SiO_2} = \frac{3.9}{\varepsilon_{r,HfO_2}} t_{ox,HfO_2} + EOT_{SiO_2}
$$
 (3.1)

<span id="page-38-2"></span><span id="page-38-1"></span> $<sup>5</sup>$  Equivalent oxide thickness, or EOT, is a normalized thickness value based on the capacitance of the</sup> dielectric(s). The EOT normalizes the thickness of the dielectric(s) to that of bulk  $SiO<sub>2</sub>$ , which has a relative dielectric constant of 3.9.

where  $\varepsilon_{r,HfO2}$  is the relative dielectric constant of the HfO<sub>2</sub> high-*k* layer,  $t_{ox,HfO2}$  is the physical thickness of the HfO<sub>2</sub> layer (extracted using HR-TEM), and  $EOT<sub>SiO2</sub>$  is the EOT of the  $SiO<sub>2</sub>$  IL. From [\(3.1\)](#page-38-2), the y-axis intercept and the slope can be used to determine the EOT of the IL and the dielectric constant of the  $HfO<sub>2</sub>$ , respectively. For the devices used in this study, a 0.7nm EOT of the IL and a dielectric constant of 20 for the  $HfO<sub>2</sub>$  layer were obtained. HR-TEM micrographs show the  $SiO<sub>2</sub>$  IL to be between 0.9nm and 1.1nm [\(Figure 3.3\)](#page-39-0). Using the EOT of 0.7nm and the physical thickness of 1.1nm, a relative static dielectric constant ( $\varepsilon$ <sub>*r,SiO2*</sub>) of 6.13 is extracted using equation [\(3.2\)](#page-39-1), where  $t_{ox}$  is the physical oxide thickness. The increased value of the static relative dielectric constant of the interfacial layer  $(6.13)$  compared to bulk  $(3.9)$  is attributed to oxygen deficiencies related to HfO<sub>2</sub> deposition and related processing [64]. Table 4.3 shows a compiled list of the different material parameters for each layer.

$$
\varepsilon_r = \frac{3.9t_{ox}}{EOT}
$$
\n(3.2)

<span id="page-39-1"></span>

<span id="page-39-0"></span>Figure 3.3: High resolution transmission electron microscope (HR-TEM) micrograph showing the interfacial layer thickness ranging from 0.9nm to 1.1nm. The darker top material is the HfO<sub>2</sub> high- $k$  layer and the lower layer the crystalline Si substrate. HR-TEM micrograph courtesy of Dr. Du Li of Micron Technology.

	Gate (TiN)	HfO <sub>2</sub>	SiO <sub>2</sub>	Si
Work Function (eV)	4.45		-	
Electron Affinity (eV)		2.65	0.95	4.15
Dielectric Constant		20	6.13	11.7
Band Gap (eV)		5.7	8.9	1.11
Thickness (nm)		3 and 5	1.1	
Doping $\text{cm}^3$ )		-		$1x10^{18}$ (n-type) $2x10^{15}$ (p-type)

**Table 3.2: Materials Properties**

Although each wafer die contains many devices, the devices used in this study were large area devices in order to increase the signal to noise ratio of the gate leakage current to system noise, which is around 10fA. The largest n/pMOSFETs available for this study had widths and lengths (*W*/*L*) of 30μm/30μm and 50μm/50μm.

# **3.4: Measurement Procedure**

As was discussed in Section [2.5,](#page-32-0) a simple method to study carrier transport mechanisms is to analyze the DC I-V characteristics of the gate leakage current at various temperatures. Developing analytical techniques for DC I-V characteristics of multi-layer stacks leverages existing common measurement techniques that are routinely performed for single layer dielectric gate stacks. DC I-V techniques are also well suited for use in the variable range probe station where the excellent low-noise DC characteristics can be utilized and the frequency response limitations of the system can be avoided.

For the I-V sweep of the gate leakage current  $(I_G-V_G)$ , a technique called carrier separation [65-67] was used whereby all four MOSFET terminals are monitored, which allows the carrier type that is transported through the dielectric stack to be identified. To measure the inversion charge density, a slight bias on the drain current is applied during one of the tests. A 60s hold time was integrated into all tests to allow the device to reach steady state. A sweep delay of 1s was also used to allow the device to reach steady state

during the measurement sweep. Small sweep steps of 0.01V provide fine resolution of the gate leakage current with respect to the gate voltage, which is especially useful for large changes in the current with respect to voltage. Measurements were performed using the Keithely 4200's "*quiet*" setting to minimize noise. A single I-V sweep results in a test time of about 20mins. [Table 3.3](#page-41-0) describes the voltage range used and the resulting current measurement range for the various tests discussed. The voltage source range for all four terminals was set to "*best fixed*" where the Keithley 4200SCS determines what source range to use for the entire voltage sweep (i.e., the source range is not changed during the test).

Test	$V_{Gate}$		$V_{Drain}$ $V_{Source. Sub/Well}$	$I_{Gate}$	$I_{Drain,Source, Sub/Well}$	Temperature $(K)$
$1^{\dagger}$	-1 $V^*$ to 1V	0V	0V	Auto	Not Monitored	5.6, 7, 8, 9, 10, 15, 20 to
	$0.01V$ steps					300 in 10K increments
$2^{\dagger}$	-1 $V^*$ to 1V	$3K_bT^*$	0V	100pA	100pA Limited Auto	5.6, 7, 8, 9, 10, 15, 20 to
	$0.01V$ steps			Limited Auto		300 in 10K increments
	$-2V$ to $2V$				100pA Limited Auto	6, 10, 15, 20 to 100 in
$3^{\ddagger}$	$0.01V$ steps	0V	0V	Auto		10K increments 100 to
						400 in 20K increments
$4^{\ddagger}$	$-1V$ to 2.5V <sup>**</sup>	0V	0V	Auto	100pA Limited Auto	300
	0.01V steps					

<span id="page-41-0"></span>**Table 3.3: I-V sweep parameters**

\*pMOSFETs: bias is negative polarity. for 5nm HfO<sub>2</sub> devices stop voltage was 3V. \*\*\* start voltage of high-*k* devices was -1.25V. <sup>†</sup> not performed on 5nm HfO<sub>2</sub> devices. <sup>‡</sup>only performed on high-*k* devices

The temperatures at which measurements were performed are also shown in [Table](#page-41-0)  [3.3.](#page-41-0) Very fine temperature steps were used to accurately track the gate leakage current with respect to temperature. This study resulted in the one of the lowest temperature

studies conducted to date on  $HfO<sub>2</sub>$  and the most finely-spaced-temperature characterization of  $HfO<sub>2</sub>$  to date according to the author's knowledge. For the temperature range examined (5.6-400K), measurements began at the lowest temperature and increased until the entire temperature range of interest was covered. The station was allowed to sit for a minimum of 20 minutes between temperatures to allow the probe station to reach a thermal steady state.

A limited number of devices were used in taking measurements described in [Table 3.3,](#page-41-0) they are:

- a. for  $2 \text{nm } \text{SiO}_2$ , there were 4 devices:  $2 \text{nm } \text{MS}$  and  $2 \text{pm } \text{MS}$ ,
- b. for 3nm HfO<sub>2</sub>, there were 7 devices: 3 nMOS and 4 pMOS, and
- c. for 5nm  $HfO<sub>2</sub>$ , there were 4 devices: 2 nMOS and 2 pMOS

A total 15 devices were used in creating the finely-spaced-in-temperature results discussed this study. Results correspond to trends observed in the temperature dependence of the gate leakage current in many other MOSFETs of the same gate stack, which were performed either using a larger temperature step size or differently sized MOSFETs.

Subsequent C-V measurements were also performed to determine the freeze-out behavior of carriers in n/pMOSFETs. A select number n/pMOSFETs composed of 3nm  $HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>$ , 5nm  $HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>$ , and 2nm  $SiO<sub>2</sub>$  devices were used to perform C-V using the Agilent 4284. For the C-V measurements, an AC probe frequency of 100kHz and amplitude of  $45 \text{mV}_{\text{rms}}$  was used. The C-V measurements were taken over a temperature range of 5.6K to 300K.

## CHAPTER 4: ENERGY BAND SIMULATION TOOL

As is demonstrated in [Figure 2.1](#page-24-0)[-Figure 2.5,](#page-32-1) energy band diagrams are useful tools to explain solid state principles and to understand device behavior including metaloxide-semiconductor (MOS) structures. Many device parameters can also be extracted from accurately constructed energy band diagrams. The parameters include the flatband voltage  $(V_{FB})$ , threshold voltage  $(V_t)$ , and electric field. The latter is required for calculating the current from Fowler-Nordhiem tunneling [68, 69], Poole-Frenkel transport [70, 71], and Schottky emission [69, 72]. Accurate construction of energy band diagrams is time consuming and tedious, which can limit their usefulness. Quick hand sketches can lead to over exaggeration of features, which 1) limits analysis or 2) leads to incorrect assumptions. Accurate construction of energy band diagrams in modern MOS devices is further complicated by the recent introduction of multilayer dielectrics. MOS multilayer dielectric devices include high-*k* oxides in MOS devices [73] and trap-based flash nonvolatile memory devices (NVM) [74], such as SONOS [75] and TANOS [76], that incorporate trapped charge within the multilayer dielectric stack.

Device structure parameter calculations can be performed by hand, using spreadsheets, mathematical programs (e.g., Matlab, Mathematica) or with Poisson-Schrodinger equation solvers (PSES), which utilize finite-element approaches. Hand calculations can be quick and useful but typically employ simplifying assumptions, which limit their effectiveness. A quick visual method to understand these devices is not available. Although an improvement over hand calculations, employing spreadsheets or

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mathematical programs for complex modeling can be challenging and time consuming. Assuming spreadsheets or mathematical programs accurately calculate device parameters for a MOS structure, changing the existing calculations from a single dielectric system to a more complex system (e.g., a three dielectric layer system) requires additional nontrivial programming. Conversely, extremely powerful finite element PSES are available to perform many device parameter calculations and to graphically represent a variety of device structures. The cost of software licenses and the effort required to learn the program interface is substantial. These barriers leave many without the ability to easily and quickly calculate the energy band diagram and associated parameters of multilayer dielectric device structures.

To address this dilemma, software was developed that quickly allows visualization of diagrams, including energy bands, potentials, and electric fields for dual layer high-*k* dielectrics on semiconductors with the ability to calculate and display voltages, electric fields, and capacitances as a function of applied voltages [77]. The approach is unique in that it does not rely on purely numerical techniques, such as finiteelement PSES, but rather an iterative approach based on the underlying physics. The software is freely available to the public [78] and has received positive reviews from individual scientists and engineers at institutions and companies, including Penn State University, National Institute of Standards and Technology (NIST), Oregon State University, University of Florida, SEMATECH, Intel, Texas Instruments, ST Microelectronics, Freescale, IBM, and others. The author knows of no other software with equivalent capabilities, simplicity, speed, and cost (free).

A new version of the program is discussed here where the previous version developed by the author is expanded to support an unlimited number of dielectric layers with the added capability of adding metal layers between dielectric layers. The software is also expanded to display the potential through the dielectric stack, charge distributions, as well as the effects trap charge in the dielectric play on the energy band diagram and various device parameters. The improvements to the program minimize both the setup time and the learning curve compared to finite-element PSES. Parameter calculations and the representation of energy, electric field, or charge distributions are nearly instantaneous, and easier to initiate and execute than either spreadsheets, mathematical programs, or finite element PSES approaches.

# **4.1: Model**

Accurate construction of an energy band diagram requires solving Poisson's equation:

$$
\frac{d^2\phi}{dx^2} = -\frac{dE_{Field}}{dx} = -\frac{\rho}{\varepsilon},\tag{4.1}
$$

<span id="page-45-0"></span>where *x* is distance,  $\phi$  is potential,  $E_{Field}$  is electric field,  $\rho$  is charge density, and  $\varepsilon$  is the permittivity. The simulation program uses a modular approach to calculate the charge, electric field, potential, and energy of a structure composed of metals, dielectrics, and a semiconductor. In this approach, Poisson's equation, [\(4.1\)](#page-45-0), is solved for each material independently when given a starting charge and potential. Using the individual solutions to [\(4.1\)](#page-45-0), the entire structure is then solved. Due to the modular approach, an arbitrary number of materials may be used in any combination limited by the following rules.

Metals may be placed at any location in the gate stack as long as they are separated by dielectrics. The structure must have a metal as a starting material and end with either a metal or semiconductor material. A semiconductor can only be placed as an end material since an infinite thickness is assumed when solving the model. These few constraints leave a large number of structures that can be analyzed in one-dimension using the simulation tool, making it extremely useful in analyzing multilayer novel dielectrics, which are being used in advanced metal-insulator-semiconductor devices, such as trapbased non-volatile memory.

The next three subsections describe the model used for each material type in determining the solution to the entire structure. Following these models, additions to the simulation tool are described.

# 4.1.1: Metal Model

Metals in the model are assumed to be perfect conductors. This implies the electric field in the metal is zero or:

$$
E_{\text{metal}} = 0, \tag{4.2}
$$

which also implies that the potential drop in the metal is also zero or:

$$
\Delta \phi_{metal} = 0. \tag{4.3}
$$

Hence, the potential in the metal is equal to the potential in the previous material at the boundary. For the first metal in the structure (i.e., considered at the top of a stack of multilayers of materials), the starting charge is applied as an infinitely thin line charge to the bottom of the metal. For a metal inside the structure, the negative of the sum of the charges above the metal (*ρtotal*) are placed on the top of the metal (*ρmetal,top*) as an infinitely thin line charge (due to charge neutrality), and the sum of the charges plus any trapped

charge assigned to the metal (*ρmetal,trapped*) are placed on the bottom part of the metal as an infinitely thin line charge. These relationships are described by the following equations:

$$
\rho_{\text{metal,top}} = -\rho_{\text{total}} \qquad \text{and} \tag{4.4}
$$

$$
\rho_{\text{metal}, bottom} = \rho_{\text{total}} + \rho_{\text{metal}, trapped} \,. \tag{4.5}
$$

For a metal that is placed as an end material (the bottom of the stack of materials), the sum of the charges above the metal are placed on the top of the metal as an infinitely thin line charge. Regardless of the thickness of the metal material, charge in the metal is modeled using infinitely thin line charges and does not consider quantum mechanical effects.

## 4.1.2: Dielectric Model

For each dielectric, an arbitrary number of line charges can be inserted within the material. Following Poisson's equation, the electric field (*E*) in the dielectric at a given line charge (*j*) is given by:

<span id="page-47-0"></span>
$$
E_j = \frac{1}{\varepsilon} \left( \rho_{\text{total}} + \sum_{0}^{j} \rho_j \right), \tag{4.6}
$$

where  $\rho_{total}$  is the sum of the charge in the structure up to the interface of the dielectric of interest and  $\rho_i$  is the *j*th line charge in the said dielectric. After the electric field is calculated, the potential  $(\phi)$  can then be calculated at a given line charge by:

<span id="page-47-1"></span>
$$
\phi_j = \phi_{boundary} + \sum_{1}^{j} -E_{j-1} (x_j - x_{j-1})
$$
\n(4.7)

where  $\phi_{boundary}$  is the potential at the boundary of the dielectric of interest and  $x_j$  is the location of the *j*th line charge. Using the potential, the energy band is easily calculated by applying the appropriate electron affinities and band gaps.

Equations [\(4.6\)](#page-47-0) and [\(4.7\)](#page-47-1) are applicable at any location inside the dielectric and are not limited to a specified line charge.

#### 4.1.3: Semiconductor Model

As mentioned above, a semiconductor can be placed at the bottom of the stack and the equations used for solving the charge, electric field, and potential of the semiconductor are taken from [79]. Using [79], the potential drop in the semiconductor (surface potential,  $\psi_s$ ) for a given charge is given by:

<span id="page-48-0"></span>
$$
Q'_{C} = \pm \sqrt{2q\varepsilon_{s}N_{A}}\sqrt{\phi_{t}e^{-\psi_{s}/\phi_{t}} + \psi_{s} - \phi_{t} + e^{-2\phi_{F}/\phi_{t}}\left(\phi_{t}e^{\psi_{s}/\phi_{t}} - \psi_{s} - \phi_{t}\right)}
$$
(4.8)

where  $Q'_{c}$ ,  $q$ ,  $N_A$ ,  $\varepsilon_s$ ,  $\phi_t$ , and  $\phi_F$  are the semiconductor charge per unit area, electron charge, doping concentration, semiconductor dielectric constant, thermal voltage, and semiconductor body doping potential, respectively. To obtain the potential drop in the semiconductor as a function of distance  $(x)$ , the integral of the inverse of the electric field yields the distance as follows [79],

$$
\int_{\psi(x)}^{\psi_s} \frac{1}{E(\hat{\psi})} d\hat{\psi} = x - x_{\text{surface}}
$$
\n(4.9)

where  $E(\psi)$  is the electric field of the semiconductor as a function of potential and is calculated by [79]:

<span id="page-48-1"></span>
$$
E(\psi) = \pm \frac{\sqrt{2q\varepsilon_s N_A}}{\kappa_s} \sqrt{\phi_t e^{-\psi(x)/\phi_t} + \psi(x) - \phi_t + e^{-2\phi_F/\phi_t} \left(\phi_t e^{\psi(x)/\phi_t} - \psi(x) - \phi_t\right)}.
$$
(4.10)

Using [\(4.8\)](#page-48-0)-[\(4.10\)](#page-48-1), the potential, charge, and electric field in the semiconductor can be calculated. The potential of the entire stack is solved by choosing a starting gate charge and determining if the resultant potential matches the desired input voltage. A solution is obtained using this iterative approach. The result of the analytical algorithm built into the program and the assumptions described in [Table 4.1](#page-49-0) provides quick calculation speeds.

Fermi-Dirac approximated with Maxwell-Boltzmann statistics
Semiconductor doping >> intrinsic carrier concentration
Complete ionization of dopant atoms (Temperature $> 100K$ )
Non-degeneracy in the semiconductor
Uniformly doped Si
Charge sheet approximation
Metal gate
Infinitely thin line charges
Quantum mechanical effects not considered
Device in equilibrium/no current flow

<span id="page-49-0"></span>**Table 4.1: Simulation Tool Assumptions**

#### 4.1.4: Image Charge Model

A charged particle at distance *x* from a perfect conductor plate will have its electric field lines terminate perpendicular to the interface between a conductor and nonconductor plate as shown in [Figure 4.1.](#page-50-0) Opposite charged particles at a distance of 2*x* will have their electric fields perpendicular to an imaginary plane exactly half way (or distance *x*) and normal to the two charged particles. The force between a charged particle and conductor plate at a distance *x* from one another is therefore equal to the force between two oppositely charged particles at distance 2*x*; this is known as the *image charge theorem*.



<span id="page-50-0"></span>Figure 4.1: Diagram demonstrating the image charge theorem. A charged particle at distance *x* from a conductor experiences a force equal to the force between two opposite charged particles at distance 2*x*.

The potential energy for two oppositely charged particles with electric charge *q* (the charge of an electron) at a distance  $2x$  in units of  $eV$  is given by Coulomb's potential:

$$
PE(x) = \frac{-q}{16\pi\epsilon x} \tag{4.11}
$$

<span id="page-50-1"></span>where *q* is the charge of an electron and  $\varepsilon$  is the high frequency dielectric constant of the medium surrounding the electron. The potential energy of an electron<sup>[6](#page-50-2)</sup> at a distance x from a conductor can also be described by ([4.11](#page-50-1)). The potential energy of an electron in the dielectric of a MOS device modifies the barrier it sees due to its own charge interacting with the nearby conductor. If an electron is placed between parallel conductor plates (as is the case in metal-insulator-metal structures), image charges are formed across both conductor plates. The image charges are imaged again across each conductor plate and the pattern repeats itself infinitely. The potential of each of these image charges acting on the electron is summed using the superposition principle to give the potential energy of the electron acting with the two conductor plates. An example of how this

<span id="page-50-2"></span> <sup>6</sup> An analogous case can also be made for holes.

occurs for the first three sets of image charges is shown in [Figure 4.2.](#page-51-0) The infinite sum of these charges acting on the electron at *x* is given by:

<span id="page-51-1"></span>
$$
PE(x) = \frac{q}{16\pi\varepsilon} \sum_{n=0}^{\infty} \left( -\frac{1}{nd+x} - \frac{1}{(n+1)d-x} + \frac{2}{(n+1)d} \right)
$$
(4.12)

where  $n$  a variable of the summation, which takes on integer values,  $x$  is the distance to one conductor, and *d* is the distance between conductors.



<span id="page-51-0"></span>Figure 4.2: Image charges due to an electron between two conductors. Each imaged charge is imaged again across the other conductor resulting in an infinite series of image charges. The first three image charge sets are shown here (top, middle, and bottom) along with the resulting potential.

For multiple dielectrics, the image potential at the dielectric-dielectric interface must also be considered. The potential energy of image charge due to the dielectricdielectric interface (a charge free interface) is given in units of eV as [80, 81]:

<span id="page-52-0"></span>
$$
PE(x) = \frac{-q}{16\pi\epsilon x}k\tag{4.13}
$$

<span id="page-52-1"></span>where

$$
k = \frac{\varepsilon_a - \varepsilon}{\varepsilon_a + \varepsilon},\tag{4.14}
$$

*ε* is the high frequency dielectric constant where the charge is located, and *ε<sup>a</sup>* is the high frequency dielectric constant of the adjacent dielectric. Examining [\(4.13\)](#page-52-0) and [\(4.14\)](#page-52-1) indicate that if  $\varepsilon > \varepsilon_a$ , then the charge is repelled from the boundary, and if  $\varepsilon < \varepsilon_a$ , the charge is attracted to the boundary. For thin multilayer dielectrics, the effects of boundary to the right and left of the dielectric must be considered. The solution to the image charge potential of a thin dielectric with a dielectric on either side (similar to [Figure 4.2](#page-51-0) where the metals are replaced with dielectrics) was solved by Kleefstra and Herman and is given as [81]:

<span id="page-52-2"></span>
$$
PE(x) = \frac{q}{16\pi\epsilon x} \sum_{n=0}^{\infty} (k_i k_r)^n \left( \frac{k_i}{nd + x} + \frac{k_r}{d(n+1) - x} + \frac{2k_i k_r}{(n+1)d} \right)
$$
(4.15)

<span id="page-52-3"></span>where

$$
k_{i} = \frac{\varepsilon - \varepsilon_{i}}{\varepsilon + \varepsilon_{i}}, \quad k_{r} = \frac{\varepsilon - \varepsilon_{r}}{\varepsilon + \varepsilon_{r}}, \tag{4.16}
$$

*ε* is the high-frequency dielectric constant of the material for which the potential is solved,  $\varepsilon_l$  is the high-frequency dielectric constant of the material to the left, and  $\varepsilon_r$  is the high-frequency dielectric constant of the material to the right. The potential in  $(4.15)$  can

also be used if either material to the side of the dielectric is a metal by setting  $k_l$  or  $k_r$  to -1. For the case in which the dielectric has a metal to the left and right (i.e., *kl* and *kr* equal -1), [\(4.15\)](#page-52-2) reduces to [\(4.13\)](#page-52-0). Within atomic distances of the interface, the potential image charge which is based on classical theory no longer applies [81]. The failure of classical theory within atomic distances of the interface is also observed by examining the potential in [\(4.11\)](#page-50-1), [\(4.12\)](#page-51-1), [\(4.13\)](#page-52-0), and [\(4.15\)](#page-52-2) as *x* goes to zero, which results in a potential energy the moves toward infinity.

Using [\(4.15\)](#page-52-2) and [\(4.16\)](#page-52-3), the image potential of the electron can be applied to the energy band diagram by subtracting the image potential from the potential calculated in Sections 4.1.1-4.1.2. Both metals and semiconductors can be considered as perfect conductors in the simulation tool and have the effects of the image charge potential applied to the energy band diagrams. An example showing the image barrier lowering for electrons due to the metal gate and Si substrate is shown in [Figure 4.3.](#page-54-0) The incorporation of image charge effects is important in considering Schottky emission as was shown in Section [2.4.](#page-31-0) The extrapolation of image charge effects to multiple dielectrics is important in this study in which the bidielectric  $HfO_2/SiO_2$  is studied. This model will be used when carrier transport due to image charge effects is considered in Chapter 7.



<span id="page-54-0"></span>Figure 4.3: An example of a TiN/HfO<sub>2</sub>/SiO<sub>2</sub>/Si nMOS stack energy band diagram with image charge effects (solid lines) and without image charge effects (dotted lines) for electrons and holes.

# 4.1.5: Tunneling Distance

The simulation program also supports a geometrically calculated tunneling distance through the dielectrics. The tunneling distance, useful for determining the Fowler-Nordheim tunneling (FNT) distance or direct tunneling (DT) distance for a specified applied bias and the transition from DT to FNT as a function of applied bias, is calculated using the resultant energy barriers. The approach to determine tunneling distance is only a first-order approximation; however, it is of practical value. The tunneling distance is calculated through a given dielectric layer from an adjacent layer's conduction band (CB) or valence band (VB) into its own CB or VB or into another adjacent layer's CB or VB. Shown in [Figure 4.4](#page-55-0) is an example of the calculated tunneling distance in each dielectric layer for the nMOS device shown in [Figure 4.3](#page-54-0) without image charge effects.



<span id="page-55-0"></span>Figure 4.4: Tunneling distance calculations versus gate voltage using the simulation program for a TiN/3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>/Si nMOS device. Tunneling distance for the  $HfO<sub>2</sub>$  and  $SiO<sub>2</sub>$  layers are shown in red and green, respectively. The right side of the plot (dashed lines) corresponds to substrate electron injection and the left side to gate electron injection (solid lines). The direct tunneling, Fowler-Nordheim tunneling, and hot injection regimes are labeled.

## 4.1.6: Quantum Mechanical Transmission Coefficient

The simulation tool supports the calculation of the quantum mechanical transmission coefficient through multilayer dielectrics in the gate stack. To determine the transmission coefficient, the time-independent Schrödinger wave equation must be solved for the stack potential. The one-dimensional time-independent wave equation is given as:

<span id="page-55-1"></span>
$$
-\frac{\hbar^2}{2m}\frac{d^2\psi}{dx^2} + \phi\psi = E\psi\tag{4.17}
$$

where  $\hbar$  is the reduced Planck's constant,  $m$  is the mass of the particle,  $x$  is distance,  $E$  is energy of the particle,  $\phi$  is the potential, and  $\psi$  is the wave function. The potential to solve is the trapezoidal potential [\(Figure 4.5\)](#page-56-0), which represents the energy band diagram of the dielectric. Upon finding a solution to the trapezoidal potential, solutions to an arbitrary number of trapezoidal barriers can be determined using transfer matrices.



<span id="page-56-0"></span>

To find a solution to the wave equation shown in [Figure 4.5,](#page-56-0) [\(4.17\)](#page-55-1) must be solved for each region shown. The general solutions for region I and III are the same since they have the same potential [i.e.,  $\phi$ <sub>I,III</sub>(*x*) = 0] and take the form of:

$$
\psi_{I}(x) = A_{r}e^{jkx} + A_{l}e^{-jkx}, \qquad (4.18)
$$

$$
\psi_{III}(x) = C_r e^{jkx} + C_l e^{-jkx}, \qquad (4.19)
$$

where the subscripts *r* and *l* of the constants *A* and *C* denote a right and left traveling wave respectively, *j* is the imaginary number, and

$$
k = \frac{\sqrt{2mE}}{\hbar} \,. \tag{4.20}
$$

For region II, [\(4.17\)](#page-55-1) must be solved for the potential:

$$
\phi_{II}(x) = \frac{\phi_2 - \phi_1}{l} x + \phi_1, \qquad (4.21)
$$

where  $\phi_1$  and  $\phi_2$  are the left potential and right potential of the trapizodial barrier respectively and *l* is the barrier length [\(Figure 4.5\)](#page-56-0). The general solution to the wave equation for region II is in the form of Airy functions [82]:

40

$$
\psi_{II}(x) = B_1 AiryAi(\gamma + x\eta) + B_2 AiryBi(\gamma + x\eta) \,. \tag{4.22}
$$

where

$$
\gamma = \frac{\beta(\phi_1 - E)}{\left(\frac{\beta(\phi_2 - \phi_1)}{l}\right)^{2/3}},\tag{4.23}
$$

$$
\eta = \left(\frac{\beta(\phi_2 - \phi_1)}{l}\right)^{1/3},\tag{4.24}
$$

and

$$
\beta = \frac{2m}{\hbar^2} \,. \tag{4.25}
$$

The solution to the wave equation for all three regions can now be determined by solving the boundary equations, which states the wave function is continuous and smooth at the boundaries, which is mathematically expressed as:

$$
\psi_{I}(0) = \psi_{II}(0) \n\psi_{I}^{\dagger}(0) = \psi_{II}^{\dagger}(0) \n\psi_{II}(l) = \psi_{III}(l) \n\psi_{II}^{\dagger}(l) = \psi_{III}^{\dagger}(l)
$$
\n(4.26)

Solving the boundary equations and formulating the result in transmission matrix (*T*) form [83, 84] yields:

<span id="page-57-0"></span>
$$
\begin{bmatrix} C_r \\ C_l \end{bmatrix} = \begin{bmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{bmatrix} \begin{bmatrix} A_r \\ A_l \end{bmatrix},
$$
(4.27)

where

$$
T_{11} = e^{-jkl} \{ \alpha_1 \alpha_2 + \alpha_3 \alpha_4 + \alpha_5 \alpha_6 \} / \alpha_7
$$
  
\n
$$
T_{12} = e^{j2kd} e^{-jkl} \{ \alpha_1 \alpha_8 + \alpha_3 \alpha_9 + \alpha_{10} \alpha_6 \} / \alpha_7
$$
  
\n
$$
T_{21} = e^{-j2kd} e^{jkl} \{ \alpha_1 \alpha_2 - \alpha_3 \alpha_4 + \alpha_5 \alpha_{11} \} / \alpha_7
$$
  
\n
$$
T_{22} = e^{jkl} \{ \alpha_1 \alpha_8 + \alpha_3 \alpha_9 + \alpha_{10} \alpha_{11} \} / \alpha_7
$$
\n(4.28)

$$
\alpha_{1} = k \cdot AiryAi(\gamma + l\eta)
$$
\n
$$
\alpha_{2} = jk \cdot AiryBi(\gamma) - \eta \cdot AiryBi'(\gamma)
$$
\n
$$
\alpha_{3} = \eta \cdot AiryAi'(\gamma + l\eta)
$$
\n
$$
\alpha_{4} = k \cdot AiryBi(\gamma) + j\eta \cdot AiryBi'(\gamma)
$$
\n
$$
\alpha_{5} = -jk \cdot AiryAi(\gamma) + \eta \cdot AiryAi'(\gamma)
$$
\n
$$
\alpha_{6} = k \cdot AiryBi(\gamma + l\eta) - j\eta \cdot AiryBi'(\gamma + l\eta)
$$
\n
$$
\alpha_{7} = 2k\eta[AiryAi'(\gamma)AiryBi(\gamma) - AiryAi(\gamma)AiryBi'(\gamma)]
$$
\n
$$
\alpha_{8} = -jk \cdot AiryBi(\gamma) - \eta \cdot AiryBi'(\gamma)
$$
\n
$$
\alpha_{9} = -k \cdot AiryBi(\gamma) + j\eta \cdot AiryBi'(\gamma)
$$
\n
$$
\alpha_{10} = jk \cdot AiryAi(\gamma) + \eta \cdot AiryAi'(\gamma)
$$
\n
$$
\alpha_{11} = k \cdot AiryBi(\gamma + l\eta) + j\eta \cdot AiryBi'(\gamma + l\eta)
$$

and *d* is a lateral distance shift in the barrier. The transmission matrix for multiple barriers at various distances *d* can be found by using [\(4.27\)](#page-57-0). The transmission matrix through the entire stack of barriers is found by matrix multiplication of the individual barrier transmission matrices. The quantum mechanical transmission coeffecient (*T*) is found by:

$$
T = \left| \frac{T_{11} T_{22} - T_{12} T_{21}}{T_{22}} \right|^2.
$$
 (4.30)

An example of calculating the transmission coefficient for a TiN/3nm  $HfO_2/1.1$ nm SiO<sub>2</sub>/p-type Si stack at  $V_{Gate} = 2V$  is shown in [Figure 4.6.](#page-59-0)



<span id="page-59-0"></span>Figure 4.6: Transmission coefficient calculation for electron substrate injection. The transmission coefficient is shown for  $V_{Gate} = 2V$  at various energy levels above the conduction band  $(E_c)$  of the Si (gate stack in inset).

## **4.2: Capabilities**

The simulation tool provides the user with the ability to change any of the materials parameters used in the model to increase accuracy. Interfacial layers, common in high-*k* dielectrics, can be simulated by adding additional layers permitting further refinement to the simulation. An unlimited amount of fixed sheet charge can be added to any dielectric to simulate trapped fixed charge. The simulation tool also supports temperature dependent energy band gaps and intrinsic carrier concentrations of semiconductors. An electric field dependent dielectric constant is also supported for potential use in MOS ferroelectric devices [85] and multilayer ferroelectric materials [86, 87]. Image charge effects and the quantum mechanical transmission coefficient through multilayer dielectrics are also modeled.

With these capabilities, complex metal-insulator semiconductor devices whose configurations can include  $m-I_i-X$ ,  $M-I_i-M-I_i-X$ , and  $M-I_i-(M-I_i-X)$  where  $m$  and  $I$  signify metal and insulator, *i* and *j* are integer numbers, and *X* denotes a metal or a semiconductor, can be readily examined and exported for further investigation. The current version of the program contains over 18,000 lines of code.

# **4.3: Validation of the Model**

Because of the advanced capabilities of finite-element PSES programs, the PSES program SILVACO [88] was used to assess the accuracy of the simulation tool. The energy band diagram and electric field generated by the simulation tool described in the previous section is directly compared to the output of SILVACO. A gate stack composed of TiN/5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>/p-Si is used for the comparison. This stack corresponds to one of the stack types described in Section [3.3](#page-37-2) and is of interest in this study. The input parameters used in the SILVACO simulations are given in Appendix B.

The energy band diagram calculated by the simulation tool and SILVACO with and without quantum mechanical (QM) correction is shown in [Figure 4.7](#page-61-0) for a gate bias of 2V and in [Figure 4.8](#page-61-1) for a gate bias of -2V. Both [Figure 4.7](#page-61-0) and [Figure 4.8](#page-61-1) show the simulation tool produces nearly identical results to the energy bands calculated by SILVACO without quantum mechanical effects. Appling quantum mechanical correction factors to the Si semiconductor using SILVACO results in a slight modification to the energy band diagram that is well approximated by the simulation tool. In particular, the  $SiO<sub>2</sub>$  IL should change the most with QM corrections as it is adjacent to the Si, yet the change is insignificant.



<span id="page-61-0"></span>Figure 4.7: Energy band diagram of a TiN/5nm  $HfO_2/1.1$ nm Si $O_2/p$ -Si stack calculated using the simulation tool, SILVACO, and SILVACO with quantum mechanical (QM) corrections for a gate bias of 2V. Minimal differences are observed.



<span id="page-61-1"></span>Figure 4.8: Energy band diagram of a TiN/5nm  $HfO_2/1.1$ nm Si $O_2/p$ -Si stack calculated using the simulation tool, SILVACO, and SILVACO with quantum mechanical corrections for a gate bias of -2V. Minimal differences are observed.

A comparison of the calculated electric field for the dielectrics in the TiN/HfO<sub>2</sub>/SiO<sub>2</sub>/p-Si stack is shown in [Figure 4.9](#page-63-0) as the gate voltage is stepped from  $-2V$ to 2V. The data are generated three different ways as were the energy band diagrams discussed above: 1) using the simulation tool, 2) using SILVACO without QM corrections, and 3) using SILVACO with QM corrections. The data symbols in [Figure 4.9](#page-63-0) are spaced in such a manner as to aid in the comparison. All three calculation methods yield similar results. The electric field calculated using the simulation tool (solid lines) and SILVACO without QM corrections (symbols) correspond nearly exactly. Comparing the output of the simulation tool to that of SILVACO with QM corrections (dashed lines) produces very similar results. Hence, [Figure 4.9](#page-63-0) demonstrates that the electric field of the dielectric layers changes very little with the quantum corrections performed by SILVACO. The electric field calculated using SILVACO with QM correction is slightly lower compared to the simulation tool due to an increase in the potential drop in the semiconductor. The simulation tool therefore overestimates the electric field of the dielectrics and underestimates the potential drop in the semiconductor. Additionally, this simulation tool over estimates the capacitance<sup>[7](#page-62-0)</sup>.

<span id="page-62-0"></span> $<sup>7</sup>$  Note that this discussion only applies when the material is a semiconductor and not a perfect metal.</sup>



<span id="page-63-0"></span>Figure 4.9: Electric field in the  $SiO<sub>2</sub>$  and  $HfO<sub>2</sub>$  layer as a function of gate voltage calculated by the simulation tool and SILVACO with and without quantum mechanical corrections.

These calculations and comparisons demonstrate that the simulation program provides results that are reasonable and very similar to much more sophisticated calculations. The time required to learn and then use the freeware program is considerably less thereby increasing the accessibility for those that are not accustomed to involved simulations on complex multilayer dielectric structures.

## CHAPTER 5: EXPERIMENTAL RESULTS AND DISCUSSION

Representative gate leakage current measurements for the 3 different gate stacks investigated (3nm HfO<sub>2</sub>/1.1nm HfO<sub>2</sub>, 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>, and 2nm SiO<sub>2</sub>) as a function of gate voltage and temperature are shown in [Figure 5.1](#page-64-0) and [Figure 5.2](#page-65-0) for nMOSFETs and pMOSFETs, respectively. As was shown in [Figure 1.1,](#page-19-0) [Figure 5.1](#page-64-0) and [Figure 5.2](#page-65-0) indicate that the temperature dependence of the gate leakage current for both n- and pMOSFET devices is much larger for the high- $k$  devices compared to the  $SiO<sub>2</sub>$ control device.



<span id="page-64-0"></span>Figure 5.1: Gate leakage current for nMOSFETs composed of a 3nm or 5nm  $HfO<sub>2</sub>/1.1$  $SiO<sub>2</sub>$  gate dielectric and a 2nm  $SiO<sub>2</sub>$  gate dielectric for temperatures ranging from 6K to 300K.

For positive gate biases of 1V, the 3nm  $HfO<sub>2</sub>$  nMOSFETs show an order of magnitude increase in gate leakage current with the pMOSFETs showing over three

orders of magnitude increase. The 5nm  $HfO<sub>2</sub>$  stack shows over an order of magnitude increase in the gate leakage current at a gate bias of 1V for both n- and pMOSFETs. Meanwhile, the  $SiO<sub>2</sub>$  control device displays less than an order of magnitude increase in the gate leakage current. For gate leakage currents near -1V, the temperature dependence of the gate leakage current is in general small compared to  $+1V$ . At  $-1V$ , the 3nm HfO<sub>2</sub> nMOSFET device shown in [Figure 5.1](#page-64-0) displays a large increase in the gate leakage current with respect to temperature similar to  $3nm$  HfO<sub>2</sub> pMOSFET device at  $+1V$  shown in [Figure 5.2.](#page-65-0) While the increase in gate leakage current for -1V gate biases is lower than 1V gate biases for the high- $k$  devices, it is nonetheless higher than  $SiO<sub>2</sub>$ .



<span id="page-65-0"></span>Figure 5.2: Gate leakage current for pMOSFETs composed of a 3nm or 5nm  $HfO<sub>2</sub>/1.1$  $SiO<sub>2</sub>$  gate dielectric and a 2nm  $SiO<sub>2</sub>$  gate dielectric for temperatures ranging from 6K to 300K.

Since the EOTs for the 5nm  $HfO<sub>2</sub>$  and 2nm  $SiO<sub>2</sub>$  devices are relatively similar

 $\text{[EOT}_{5nm\text{ HfO2/1.1nm\text{ SiO2}}}=1.7$ nm and  $\text{EOT}_{\text{SiO2}}=2$ nm), the  $\text{HfO}_2/\text{SiO}_2$  temperature

dependence of the gate leakage current data differ from the  $SiO<sub>2</sub>$  data most likely because

of the presence of  $HfO<sub>2</sub>$  defects, phonon modes, and perhaps carrier transport modes.

There is also a significant difference in the gate leakage current of the  $5<sub>nm</sub>$  HfO<sub>2</sub> devices compared to the 3nm  $HfO<sub>2</sub>$  device. While the magnitude of the gate leakage current of the 5nm HfO<sub>2</sub> device is much smaller than the 3nm HfO<sub>2</sub>, the temperature dependence is larger. The exception to the previous statement is the large increase in the gate leakage current observed a +1V for the 3nm  $HfO<sub>2</sub>$  nMOSFET devices and -1V for the 3nm  $HfO<sub>2</sub>$ pMOSFET devices. The majority of the gate leakage current increase occurs at low temperatures  $T < 50K$  and the incremental increase in the gate leakage current at higher temperature  $T > 100K$  is larger in the 5nm HfO<sub>2</sub> device compared the 3nm HfO<sub>2</sub> device. This signifies strong thickness dependence in the transport mechanism in the  $HfO<sub>2</sub>$  layer or a transition between bulk transport and thin layer transport.

#### **5.1: General Temperature Observations**

The gate current versus gate voltage  $(I_G - V_G)$  temperature dependent curves for both n- and pMOSFETs show similar trends in three different regimes. These regimes are: 1) weak inversion (labeled Region 1 in [Figure 5.1](#page-64-0) and [Figure 5.2](#page-65-0) and the encircled regions in [Figure 5.3\)](#page-67-0), 2) relatively large positive gate biases (0.7V to 1V, labeled Region 2 in [Figure 5.1](#page-64-0) and [Figure 5.2\)](#page-65-0), and 3) relatively large negative biases (~ -1V labeled Region 3 in [Figure 5.1](#page-64-0) and [Figure 5.2\)](#page-65-0). The following subsections propose qualitative explanations for the temperature increases for the three regimes [10].

## 5.1.1: Weak Inversion – Region 1

For both n- and pMOSFETs composed of  $HfO<sub>2</sub>/SiO<sub>2</sub>$  and  $SiO<sub>2</sub>$  gate dielectrics, a large increase in the gate leakage current density,  $J_{Gate}$ , versus gate voltage is observed (the encircled regions in [Figure 5.3\)](#page-67-0) during weak inversion of the MOSFET channel. As the temperature increases, the slope of *JGate* vs *VGate* decreases following temperature dependent trends in sub-threshold slope [89]. Applying a  $3k_BT$  bias (i.e., large enough that thermal noise is not a factor) between the source and drain [89] to measure the presence of inversion charge (Test 2 in [Table 3.3\)](#page-41-0), reveals the sudden increase in *JGate* (encircled regions in [Figure 5.3\)](#page-67-0) corresponds to the sudden increase of minority carriers in the channel (steep slope region of  $I_{Source}$  in [Figure 5.4\)](#page-68-0).



<span id="page-67-0"></span>Figure 5.3: Gate leakage current density of (a) pMOSFETs and (b) nMOSFETs composed of 2nm  $SiO_2$ , 3nm  $HfO_2/1.1$ nm  $SiO_2$ , and 5nm  $HfO_2/1.1$ nm  $SiO_2$  for temperatures ranging from  $6K - 300K$ . The encircled regions indicate a common temperature response in the gate leakage current, which occurs in the weak inversion region.



<span id="page-68-0"></span>Figure 5.4: A comparison of source current, (also a measure of the inversion charge) to the gate leakage current. Current is transport path-limited above the threshold voltage  $(V_{TH})$  and carrier rate limited below  $\sim V_{TH}$  at low temperatures. Thick red arrows indicate source to gate overlap transport. Only select temperatures are shown for clarity.

The data of [Figure 5.4](#page-68-0) suggest *carrier-limited* and *transport path-limited* regimes. Consider [Figure 5.5](#page-70-0) where the currents from all four MOSFET terminals are plotted. In [Figure 5.5,](#page-70-0) the drain and source current are asymmetric across the voltage axis. At voltages near -1.05V, the gate current is nearly symmetric with both the drain and source currents. In the perfect scenario, the drain current comes from the source current and hence the source and drain current would be symmetric across the voltage axis. The asymmetry in the drain current with respect to the source current and the symmetry in the gate current with respect to both the drain and source current near the threshold voltage indicate that the first carriers that enter the channel from the source and drain do not flow from the source to the drain (i.e., source and drain current are asymmetric across the voltage axis), but flow from the source and drain through the gate dielectric to the metal gate (i.e., the gate and drain/source currents are symmetric near the threshold voltage).

The increase in *IGate* at the threshold voltage is therefore due to minority carriers from the source and drain terminals entering the channel during inversion formation. Hence, prior to the threshold voltage (i.e., depletion/weak inversion), the gate leakage current is *carrier-limited,* labeled in [Figure 5.4,](#page-68-0) due to the absence of minority carriers. The slope of the gate leakage current matches the sub-threshold slope of the source current (labeled "Matching slopes" in [Figure 5.4\)](#page-68-0), which indicates that the gate leakage current follows the number of carriers in the channel and is therefore carrier-limited in this regime. It appears that *IGate* then saturates even as the inversion charge continues to increase exponentially (as indicated by the exponential increase in the source current) before losing its exponential dependence with the gate bias. The continued exponential increases in the carrier concentration while the gate leakage current saturates as a function of gate voltage indicates a *transport path-limited* mechanism, labeled in [Figure 5.4.](#page-68-0) As the temperature increases, the transition between *carrier-limited* and *transport path-limited* conduction occurs at lower voltages due to the increased number of minority carriers as temperatures increase. Above the threshold voltage however, a sufficient amount of minority carriers are present so that the leakage current is *transport path-limited* over the temperature range investigated.



<span id="page-70-0"></span>Figure 5.5: A plot of all four terminal currents at 10K, 20K, and 30K in a 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> pMOSFET. Tunneling current (i.e., gate current) is carrier starved as observed by the increase in the gate leakage current corresponding to the presence of minority carriers flowing from the source and drain to the gate.

Similar slopes for both the gate leakage and source currents with respect to gate voltage are observed in  $2nm$  SiO<sub>2</sub> devices prior to channel inversion (region of interest is indicated by thick red arrows in [Figure 5.4\)](#page-68-0). The similar slopes between the gate and source currents in  $2nm$  SiO<sub>2</sub> devices indicates that, in that regime (prior to weak inversion), the gate leakage current corresponds to the gate to source/drain overlap region. This suggestion is further confirmed by analyzing the gate leakage currents of two differently sized MOSFETs.

Information concerning the physical location of carrier transport through the gate dielectric stack can be obtained by examining the gate leakage currents of differently sized MOSFETs. If carrier transport is dominated by the conduction mechanisms of the gate dielectric stack, the gate leakage current is expected to scale with the area of the MOSFET (*W*x*L*). If the gate leakage current is dominated by interface effects at the edge of the channel area, then the gate leakage current is expected to scale with the length of the leaky edge. So, if interface effects of the entire edge of the MOSFET channel area dominate the gate leakage current, then the gate leakage current is expected to scale with the perimeter of the device  $(2L+2W)$ . Hence, determining how the gate leakage current scales can indicate the location of where the dominate current transport is occurring.

To access the physical location of the gate leakage current, the gate leakage current density (scaled by area,  $J_{Gate}$ ) of  $30 \mu m/30 \mu m$  and  $50 \mu m/50 \mu m$  2nm  $SiO_2$  devices is plotted in [Figure 5.6.](#page-71-0) The gate leakage current densities scaled by *area* for the two differently sized devices are the same in the *transport path-limited* regime indicating that the leakage current is dominated by transport from the Si channel, which is *area* dependent.



<span id="page-71-0"></span>Figure 5.6: Comparison of the gate leakage current densities of two different area 2nm  $SiO<sub>2</sub>$  nMOSFETs,  $30 \mu m/30 \mu m$  and  $50 \mu m/50 \mu m$ . Areas of device operation where the gate leakage current densities are the same and differ are indicated. Inset shows the depletion/weak inversion regime.
An exception to the preceding argument is made in the *carrier-limited* regime and in accumulation where the 50μm/50μm device shows a lower gate leakage current density than the  $30\mu m/30\mu m$  device [\(Figure 5.6\)](#page-71-0). This may be explained by scaling the gate leakage current according to the MOSFET's *width* (*W*), *WGate* = *IGate*/*W* (since the gate to source/drain overlap region scales with device width<sup>[8](#page-72-0)</sup>), rather than the MOSFET's *area* as shown in Figure 5.7. The gate leakage current scaled by width  $(W_{Gate})$  for the 30μm/30μm device and the 50μm/50μm device is the same (i.e., superimposed) in the accumulation and depletion regimes, indicating that the gate leakage current scales according to *width* in these regimes. Current transport in the accumulation and depletion regimes is therefore dominated by the area overlap of the gate and the source/drain junctions, which scales by *width*. Note that this only applies to the  $2nm$  SiO<sub>2</sub> control devices. For the 3nm  $HfO<sub>2</sub>$  and 5nm  $HfO<sub>2</sub>$  devices, the gate leakage current scales well with area in all operating regimes, as indicated by the overlap of both  $J_{Gate}$ 's of the 30μm/30μm and 50μm/50μm devices in [Figure 5.8.](#page-73-1)

<span id="page-72-0"></span><sup>&</sup>lt;sup>8</sup> The area of the gate to drain/source overlap region is the length of the gate to drain/source overlap region multiplied by the MOSFETs width. The length of the gate to drain/source region is controlled by the manufacturing process in a self-aligned process and can be assumed constant between various MOSFET sizes. The width of the MOSFET is primarily controlled by the device layout and to a much lesser extent by the manufacturing process (especially in large width devices). The gate to drain/source overlap region therefore scales with the MOSFET's width.



<span id="page-73-0"></span>Figure 5.7: Comparison of the gate leakage current of  $2nm$  Si $O<sub>2</sub>$  nMOSFETs when scaled by the MOSFETs width. Overlap of currents in the accumulation and depletion regions indicate that current transport is occurring in the gate to source/drain overlap regions. Inset shows the depletion/weak inversion regime.



<span id="page-73-1"></span>Figure 5.8: Gate leakage current density for 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  devices having areas 30μm/30μm and 50μm/50μm. The gate leakage current scales well with area, indicating current transport is dominated in the channel area of the device.

#### 5.1.2: Relatively Large Positive Gate Biases – Region 2

For relatively large positive gate biases, gate biases above the threshold voltage in nMOS devices, the temperature dependence of the gate leakage current differs significantly between the three gate stacks examined. [Figure 5.9](#page-74-0) shows the gate leakage current density for nMOSFETs [\(Figure 5.9a](#page-74-0)) and pMOSFETs [\(Figure 5.9b](#page-74-0)) for the three gate stacks examined. The temperature range shown in [Figure 5.9](#page-74-0) extends from 6K to 300K except for the 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> pMOSFET device, where the temperature range is from 50K to 300K. Data for temperatures below 50K are not shown for the 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub> pMOSFETs$  because another temperature dependent transport regime dominates in the accumulation regime [\(Figure 5.2\)](#page-65-0). An explanation of the temperature dependent transport regime for *T* < 50K for devices in accumulation is discussed below in Section [5.3.](#page-83-0)



<span id="page-74-0"></span>Figure 5.9: Gate leakage current density plots for (a) nMOS and (b) pMOS devices composed 2nm  $SiO<sub>2</sub>$ , 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$ , and 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$ . Currents are shown for positive gate biases and for temperatures ranging from 6K to 300K except for the 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> pMOSFET where only temperatures ranging from 50K to 300K are shown.

Trends in the gate leakage current are consistent for n- and pMOSFET devices as shown in [Figure 5.9](#page-74-0) except for the depletion/weak inversion regime as was discussed in the section above. The gate leakage current increase with temperature of the  $2nm$   $SiO<sub>2</sub>$ control devices show relatively little increase in contrast with the large change in the gate leakage current of  $HfO<sub>2</sub>$  based gate stacks with temperature. The 5nm  $HfO<sub>2</sub>$  device has a greater temperature dependence in the gate leakage current compared to the  $3nm$  HfO<sub>2</sub> devices. The greater temperature dependence of  $J_{Gate}$  in the thicker 5nm  $HfO<sub>2</sub>$  devices, compared to the 3nm  $HfO<sub>2</sub>$  devices, suggests that the temperature dependence of the gate leakage current is dominated by the HfO<sub>2</sub> layer and not the HfO<sub>2</sub>/SiO<sub>2</sub> interface since the interface remains unchanged between the 3nm and 5nm  $HfO<sub>2</sub>$  devices.

A bulge in *JGate* over the large temperature range investigated is seen in the 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  devices in [Figure 5.9](#page-74-0) and has maximum at a gate voltage of ~1.1V. The temperature dependence of the gate leakage current increases until a gate voltage of  $\sim$ 1.1V (i.e., the maximum) is reached after which the temperature dependence of the gate leakage current decreases. This trend is observed in both n- and p-MOSFET devices but not in the 5nm  $HfO_2/1.1$ nm  $SiO_2$  devices suggesting a  $SiO_2$  effect.

A possible qualitative argument for the bulge seen in [Figure 5.9](#page-74-0) is as the gate bias increases, the Fermi energy level in the Si moves closer to the conduction band of the HfO2. Nevertheless, at low temperatures (i.e., minimal thermal broadening [–Figure 1.2\)](#page-21-0) and low voltages, the Fermi level is not close enough to access defect states in the  $SiO<sub>2</sub>$ layer located in energy above the Si conduction band. As the temperature increases, the thermal energy distribution broadens [\(Figure 1.2\)](#page-21-0), allowing electrons to occupy higher energy levels in the Si that have a greater probability to coincide with defect levels in the

 $SiO<sub>2</sub>$ . The combined qualitative result is the temperature dependence of the gate leakage current increases as the gate voltage increases. As the gate bias continues to increase beyond ~1.1V, less temperature is required (resonance conditions are met between the defects and the Si Fermi level by further band bending) to promote electrons to energy levels in resonance with defects in  $SiO<sub>2</sub>$  layer, resulting in a decrease in the temperature dependence of  $J_{Gate}$  for  $V_{Gate} = \sim 1.1 \text{V} - 2 \text{V}$ .

The suggestion that electrons from the Si contribute to the bulge in the gate leakage current [\(Figure 5.9\)](#page-74-0) may be substantiated by examining the energy band diagram of an nMOS device for gate biases of 0V, 1V, and 2V shown in [Figure 5.10.](#page-77-0) As the gate voltage increases, the barrier for electrons is reduced while the barrier for holes remains large for all three biases. The energy band diagram suggests an electron substrate dominated transport mechanism for the relatively large positive gate bias regime. This suggestion is confirmed using carrier separation analysis below in Section [5.2.1.](#page-81-0)



<span id="page-77-0"></span>Figure 5.10: Energy band diagram of a TiN/5nm  $HfO_2/1.1$ nm Si $O_2/p-Si$  nMOS gate stack at gate biases of 0V, 1V, and 2V. The barrier for substrate electrons decreases as the gate voltage increases. The barrier for holes remains appreciably large for all three gate voltages shown.

5.1.3: Relatively Large Negative Gate Biases – Region 3

[Figure 5.11](#page-78-0) shows the gate leakage current density for nMOSFETs [\(Figure 5.11a](#page-78-0)) and pMOSFETs [\(Figure 5.11b](#page-78-0)) for the three gate stacks examined at negative gate biases. The temperature range shown in [Figure 5.11](#page-78-0) ranges from 6K to 300K, except for the 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  nMOSFET device, where the temperature range is from 50K to 300K. Similar to 3nm HfO<sub>2</sub> pMOSFETs in accumulation, temperatures below 50K are not plotted for the 3nm  $HfO<sub>2</sub>$  nMOSFET due to another temperature dependent mechanism dominating in the accumulation regime for  $T < 50$ K. An explanation of the preceding mechanism is discussed below in Section [5.3.](#page-83-0)



<span id="page-78-0"></span>Figure 5.11: Gate leakage current density plots for (a) nMOS and (b) pMOS devices composed 2nm  $SiO<sub>2</sub>$ , 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$ , and 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$ . Currents are shown for negative gate biases and for temperatures ranging from 6K to 300K, except for the 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  nMOSFET, where only temperatures ranging from 50K to 300K are shown.

Trends in the gate leakage current are consistent for n- and pMOSFET devices as shown in [Figure 5.11,](#page-78-0) except for the depletion/weak inversion regime as was discussed in Section [5.1.1.](#page-66-0) The difference in the temperature dependence of the three gate stacks examined in the negative gate voltage regime is not large, which includes the temperature dependence difference of the 2nm  $SiO<sub>2</sub>$  control devices. The 5nm HfO<sub>2</sub> devices have a slightly stronger temperature dependence of  $J_{Gate}$  than the 3nm  $HfO<sub>2</sub>$  devices. The temperature dependence of *JGate* decreases as *VGate* approaches -2V, which may suggest an electric field dependence. A bulge is not seen in the  $3nm$  HfO<sub>2</sub> temperature dependence of *JGate* in the negative bias regime as was observed at positive gate voltages in [Figure 5.9.](#page-74-0)

As was done for positive gate biases in [Figure 5.10,](#page-77-0) the energy band diagram of a TiN/5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>/p-Si nMOS device biased at 0V,  $-1V$ , and  $-2V$  is shown in

[Figure 5.12](#page-79-0) for completeness. [Figure 5.12](#page-79-0) indicates the barrier to gate electrons and substrate holes is large over the negative gate voltage regime of interest.



<span id="page-79-0"></span>Figure 5.12: Energy band diagram of a TiN/5nm  $HfO_2/1.1$ nm Si $O_2/p-Si$  nMOS gate stack at gate biases of 0V, -1V, and -2V. While the barrier to metal electrons decreases, the barrier remains formidable. The barrier for holes remains appreciably large for all three gate voltages shown.

## **5.2: Carrier Separation: Results and Discussion**

<span id="page-79-1"></span>An important element in determining the carrier transport mechanism(s) is determining the carrier type. Knowing the carrier type of the gate leakage current can eliminate consideration of various transport mechanisms as the cause of the gate leakage current. Identifying the type of carrier (i.e., electron or hole) that is contributing to the gate leakage current can be performed by carrier separation analysis [65-67]. Carrier separation analysis is performed by examining the currents in the source/drain and bulk terminals of the MOSFET, requiring the current through all four terminals of the MOSFET to be measured. In an nMOSFET device, the current through the source/drain

(n-type region) corresponds to electrons while the bulk current corresponds to holes (ptype region). The opposite is true in pMOSFETs where the source/drain corresponds to hole currents (p-type region) and the bulk current corresponds to electron current (n-type region). Carrier separation analysis is primarily performed with the MOSFET in inversion where recombination is minimal.

With the MOSFET in inversion, minority carriers from the gate are captured by the channel and collected by the source/drain terminals. Majority carriers from the gate quickly drift away from the channel to the bulk due to high electric fields in the semiconductor channel and are collected by the bulk terminal. With the MOSFET in accumulation, minority carriers from the gate are not collected by the inversion channel (an inversion channel is not present in accumulation) and diffuse to the drain/source terminals. Minority carrier diffusion to the source/drain may take considerable time, especially if the device is large (as is the case in this study). During diffusion, the minority carrier may recombine with majority carriers, giving rise to an increase in the bulk current rather than the source/drain. It therefore becomes difficult to know if the bulk current is due to majority carriers from the gate or from recombination with minority carriers. Thus, it is important to measure both n- and p-MOSFETs to characterize carrier transport for positive and negative voltages.

The terminal currents for the gate (black lines), source/drain (green lines, which have been added together mathematically to plot the total minority carrier current), and bulk (red lines) are shown for 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> n/pMOSFET devices in [Figure 5.13](#page-81-1) and 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> n/pMOSFETs devices in [Figure 5.14.](#page-82-0)

#### <span id="page-81-0"></span>5.2.1: Positive Gate Biases

For both 3nm and 5nm HfO<sub>2</sub> nMOSFET devices in inversion [\(Figure 5.13a](#page-81-1) and [Figure 5.14a](#page-82-0)), the gate current overlaps with to the source/drain (n-type regions) current implying the gate leakage current is due to substrate electron injection. Within the accumulation operating region of 3nm and 5nm pMOSFET devices [\(Figure 5.13b](#page-81-1) and [Figure 5.14b](#page-82-0)), where recombination is occurring, the gate and bulk current (n-type region) are superimposed, indicating electron substrate injection. Hence, the gate leakage current for both the pMOSFET and nMOSFET devices is due to substrate electron injection.



<span id="page-81-1"></span>Figure 5.13: Currents monitored from each terminal for (a) an nMOSFET and (b) pMOSFET composed of 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$ . Note that many of the currents are superimposed.



<span id="page-82-0"></span>Figure 5.14: Currents monitored from each terminal for an (a) nMOSFET and (b) pMOSFET composed of 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$ . Note that many of the currents are superimposed.

#### 5.2.2: Negative Gate Biases

The gate current and source/drain (p-type region) currents of 3nm and 5nm pMOSFETs in inversion [\(Figure 5.13b](#page-81-1) and [Figure 5.14b](#page-82-0)) correspond very well, indicating that substrate hole injection is occurring at negative gate biases. Analyzing the  $3$ nm HfO<sub>2</sub> nMOSFET currents in accumulation [\(Figure 5.13a](#page-81-1)), where electron-hole recombination is occurring, shows the gate and bulk (p-type region) currents are superimposed, suggesting substrate hole injection is occurring. For the 5nm  $HfO<sub>2</sub>$ nMOSFET device in accumulation [\(Figure 5.14a](#page-82-0)), the gate current is more equivalent to the bulk current than the source/drain current, which also suggests substrate hole injection. To a lesser extent in the 5nm  $HfO<sub>2</sub>$  nMOSFET [\(Figure 5.14a](#page-82-0)) but still noticeable is the large source/drain current in relation to the gate current, which indicates that perhaps electrons play a role in the gate leakage currents at negative gate biases in  $5$ nm HfO<sub>2</sub> devices. Some evidence of this is also observed in the  $5$ nm HfO<sub>2</sub> pMOSFET

[\(Figure 5.14b](#page-82-0)) in inversion, where the electron current (bulk current) is less than a decade smaller than the gate leakage current.

In summary, for positive gate biases of 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  and 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> n/pMOSFETs, the gate leakage current is dominated by substrate electron injection and for negative gate biases substrate hole injection. In the 5nm  $HfO<sub>2</sub>$ devices in the negative gate bias regime, the gate electron current begins to have an increasing role in the gate leakage current as evidenced by [Figure 5.14a](#page-82-0), where the electron current nearly corresponds to the gate current. This analysis differs from the work of Shaimeev *et al.*, on HfO<sub>2</sub>/SiO<sub>2</sub> gate stacks where carrier separation analysis results in electron current for both positive gate biases and negative gate biases [90]. It is important to note that the metal gate used by Shaimeev *et al.* was aluminum (Al), which has a work function of 4.1eV while the metal gate used in this study is TiN with a work function of 4.45eV. The smaller work function of Al reduces the conduction band offset of the metal gate with  $\text{HfO}_2$ , which would increase the access of metal electrons to defects near the  $HfO<sub>2</sub>$  conduction band edge or to the conduction band itself through FN tunneling. These two examples highlight the effect that the difference in the work function of the metal gate has on the gate leakage current and the type of carrier involved in the carrier transport.

#### **5.3: Arrhenius Results and Discussion**

<span id="page-83-0"></span>Many temperature dependent mechanisms follow an Arrhenius expression of the form (expressed here in terms of the gate current density):

<span id="page-83-1"></span>
$$
J_{Gate}(T) = Ae^{-E_A/k_B T},
$$
\n(5.1)

where  $A$  and  $E_A$  represent a constant and activation energy. Determining the activation energy from [\(5.1\)](#page-83-1) is performed by linearizing the equation (shown in the form of  $y = mx + b$ ) as:

<span id="page-84-0"></span>
$$
\ln(J_{\text{Gate}}(T)) = -\frac{E_A}{k_B} \frac{1}{T} + \ln(A) \,, \tag{5.2}
$$

Equation [\(5.2\)](#page-84-0) illustrates that the activation energy can be derived from the slope of the data plotted as the natural log of  $J_{Gate}$  versus  $1/T$ , which is called an Arrhenius plot. Arrhenius plots<sup>[9](#page-84-2)</sup> of the 3nm and 5nm  $HfO<sub>2</sub>$  devices for both nMOSFETs and pMOSFETs areshown in Figure 5.15 while Arrhenius plots of the  $2nm$   $SiO<sub>2</sub>$  control n/pMOSFETs are shown in [Figure 5.16.](#page-85-0)



<span id="page-84-1"></span>Figure 5.15: Arrhenius plot of the gate leakage current density at gate biases of -2V and 2V for (a) 3nm HfO $_2$ /1.1nm SiO<sub>2</sub> devices and (b) 5nm HfO $_2$ /1.1nm SiO<sub>2</sub> devices.

<span id="page-84-2"></span> $9$  Notice that the Arrhenius plots shown (e.g., [Figure 5.15\)](#page-84-1) are plotted on a log base 10 scale and not on a natural log scale as described in [\(5.2\)](#page-84-0). The log base 10 scale is used to better identify the gate current density values. Plotting the data on a log base 10 scale maintains the linearity of Arrhenius data but changes the offset and slope by a multiple of log(*e*). These differences are accounted for when extracting the activation energy.



<span id="page-85-0"></span>Figure 5.16: Arrhenius plot of the gate leakage current density of  $2nm$  SiO<sub>2</sub> control device for n/pMOSFETs for gate biases of -1V and 1V.

Observed in [Figure 5.15](#page-84-1) and [Figure 5.16](#page-85-0) are two regimes that appear linear at first: 1) a weak temperature dependent regime is observed for  $T < 50K$  with  $\mu$ eV activation energies, and 2) a strong temperature regime is observed to  $T > 150K$ . The presence of multiple slopes in an Arrhenius plot is an indication that multiple processes are occurring [45]. The Arrhenius behavior of *JGate* [\(Figure 5.15](#page-84-1) and [Figure 5.16\)](#page-85-0) reveals that the two ranges in temperature in which the slopes are significantly dissimilar suggests that two different transport regimes are present. This behavior is observed for all three gate stacks examined: 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>, 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub>, and SiO<sub>2</sub> MOSFETs. Two transport regimes were also observed by Compagnoni *et al*. [11] in which they examined transport over a temperature range of 77-300K in Al/5nm  $HfO<sub>2</sub>/0.87$ nm Si $O<sub>2</sub>/Si$  MOS capacitors. They report activation energies ~87meV for temperatures higher than 165K and 5meV for the lower temperature regime of 77-165K. In this study, a lower activation energy of  $\sim$ 1µeV is found, indicating a very weak

temperature dependence and most likely a non-Arrhenius behavior because the energy is unrealistically low. Of interest is to determine the activation energy in the low temperature range of Compagnoni *et al.* (77-165K). [Figure 5.17](#page-87-0) shows the 5nm HfO<sub>2</sub> data of this study in a temperature regime down to which Compagnoni *et al*. investigated (i.e., 77K). In this regime, an activation energy of 2.7meV is determined for the low temperature regime, which is consistent with the activation energy reported by Compagnoni *et al*. For the high temperature regime investigated by Compagnoni *et al.*, an activation energy of 66meV is obtain, similar to the 87meV reported by Compagnoni *et al*.. The much larger activation energy of 2.7meV is explained by realizing that the range of temperatures used down to 77K to calculate the activation energy is in a transition region, which is not linear (compare temperature regions of [Figure 5.15b](#page-84-1) and [Figure 5.17\)](#page-87-0).



<span id="page-87-0"></span>Figure 5.17: Arrhenius plot of the gate leakage current density for  $HfO<sub>2</sub>/SiO<sub>2</sub>$ nMOSFETs. For gate leakage currents from  $\sim$ 125K to 77K, which appear linear, the weak temperature regime has an activation energy of 2.7meV. As the temperature range in this work continue down to 5.6K, ~125K to 77K is in a transition region and not linear.

The increments of temperature used in the study by Compagnoni *et al*. for the wide transition regime are large, thereby leaving the temperature range not well defined. The data in [Figure 5.17](#page-87-0) suggests that room temperature is part of the transition regime as it has significant curvature. The derivative of  $\ln(J_{Gate})$  versus  $1/T$  shows an ever increasing slope as the temperature increases, which indicates that the data does not follow a strict Arrhenius law in the temperature regime  $T < 400K$ . The activation energy extracted from the Arrhenius plot therefore depends on the temperature range used. To illustrate this effect, [Figure 5.18](#page-88-0) shows the activation energy versus gate voltage calculated using four different temperature ranges for 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  and 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  n/pMOSFETs. Extracted activation energies in [Figure 5.18](#page-88-0) are only shown for large gate biases where MOSFET effects of depletion and weak inversion do not distort trends. The higher the temperature range used to extract the activation energy,

the larger the activation energy. The 5nm  $HfO<sub>2</sub>$  samples show a larger activation energy compared to the 3nm  $HfO<sub>2</sub>$  samples. In general, the activation energies of both n/pMOSFETs are similar for the various temperature ranges investigated [\(Figure 5.18\)](#page-88-0).



<span id="page-88-0"></span>Figure 5.18: Activation energy versus gate voltage for various n/pMOSFETs composed of a bilayer of 3nm or 5nm  $HfO<sub>2</sub>$  on 1.1nm  $SiO<sub>2</sub>$ . The activation energy is dependent on the temperature range used to extract it. The higher the temperature range used, the larger the calculated activation energy.

The Arrhenius plots of 3nm and 5nm  $HfO<sub>2</sub>$  devices in accumulation [\(Figure 5.15\)](#page-84-1) show additional slope changes and thus indicate additional processes are occurring for temperatures less than 50K [10]. The 3nm  $HfO<sub>2</sub>$  samples clearly show both n/pMOSFETs having nearly the same temperature dependence until temperatures fall below 50K where devices in accumulation have low leakage currents. It is believed that the lack of thermally generated majority carriers from the donor/acceptor energy levels at temperatures below ~50K limit the amount of carriers available for transport through the gate stack. This idea is similar to the *carrier-limited* and *transport path-limited* regimes discussed in Section [5.1.1.](#page-66-0) Note that for devices in accumulation, majority carriers are the

dominate contribution to *JGate*, according to carrier separation analysis (Section [5.2\)](#page-79-1), which indicates that substrate electrons dominate transport at positive gate biases (pMOSFETs in accumulation) and substrate holes dominate carrier transport at negative gate biases (nMOSFETs in accumulation). The largest change in the gate leakage current as temperature decreases below  $50K$  is observed for 3nm  $HfO<sub>2</sub>$  pMOSFETs in accumulation. C-V data on a 3nm  $HfO<sub>2</sub>$  pMOSFET to determine the response of majority carriers as a function of temperature are shown in [Figure 5.19.](#page-89-0) Similar to the gate leakage current [\(Figure 5.2\)](#page-65-0), the capacitance in accumulation decreases as the temperature decreases below 50K [\(Figure 5.19\)](#page-89-0). For the measured temperatures of 25K and 5.6K, a significant reduction in the capacitance signifies that the majority carriers are not responding to the capacitance AC probe frequency. The absence of a majority carrier response in the C-V measurements at temperatures below 50K further justifies the idea that a limited number of majority carriers in accumulation are limiting the gate leakage current in accumulation.



<span id="page-89-0"></span>Figure 5.19: Capacitance-Voltage response of a 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  pMOSFET for temperatures ranging from 5.6K to 300K. A large decrease in the capacitance is observed in the accumulation regime as temperature decreases below 50K.

In addition to the temperature dependence of extracted activation energies, the activation energy also varies with gate voltage for both the  $HfO<sub>2</sub>$  samples as well as the  $SiO<sub>2</sub>$  control samples; see [Figure 5.18](#page-88-0) and Figure 11 in [10]. The gate voltage dependence of the activation energy [\(Figure 5.18\)](#page-88-0) suggests an electric field dependence. Typical electric field correction factors to the activation energy are Poole-Frenkel and Schottky emission as was discussed in Chapter 2. Due to the extensive use of Pool-Frenkel and Schottky emission as explanations to the temperature dependence of the gate leakage current in high-*k* devices, Chapters 6 and 7 focus on examining the data using Poole-Frenkel and Schottky analysis.

#### CHAPTER 6: POOLE-FRENKEL ANALYSIS

<sup>[10](#page-91-0)</sup>Poole-Frenkel (P-F) conduction has been a popular explanation of the temperature dependence of the gate leakage current of  $HfO<sub>2</sub>$  in the literature for high temperature measurements (300K to  $\sim$  500K) [7, 21, 92, 93]. Through the use of P-F analysis, various trap energy barrier heights have been reported (e.g., 0.35eV [21], 0.68eV [20], 1.11-1.36eV [33], 1.5eV [7]) for  $HfO<sub>2</sub>$ . The reported trap barrier heights may differ due to a variety of reasons, which may include different growth methods, preand post-growth processing, and device technologies used. In this chapter, P-F analysis is applied to the gate leakage currents measured in the high temperature region  $(T > 150K)$ . Methods of extracting the electric field in the  $HfO<sub>2</sub>$  layer are discussed and the effect that various electric field calculation techniques have on the extracted trap barrier height are presented. Using the wide range of temperatures available and two different  $HfO<sub>2</sub>$ thicknesses, the standard P-F model is used to examine the trap barrier height versus both temperature range and  $HfO<sub>2</sub>$  thickness. In short, this chapter examines whether or not the standard P-F model can describe charge transport over a wide temperature range in  $HfO<sub>2</sub>$ - $SiO<sub>2</sub>$  bilayer dielectric stacks (6K – 400K).

### **6.1: Poole-Frenkel Analysis Techniques**

<span id="page-91-1"></span>The standard P-F conduction mechanism was described earlier in Section [2.3.](#page-28-0) P-F conduction does not describe the kinetics of carrier capture. It only considers carrier

<span id="page-91-0"></span> $10$  The main points and some content discussed in this chapter are taken from work published in [91].

emission. In order P-F conduction to dominate, thermal stimulation of the carrier over the reduced barrier height must be the limiting mechanism. Traps are usually considered to be filled through quantum mechanical tunneling [32]. P-F conduction also stipulates the nature of the traps involved in the conduction process due to its derivation of a hydrogenic-like state. That is, according to Frenkel, for trapping to occur, the impurity must be ionized in the non-trapped state and neutral in the trapped state [51]. P-F also assumes negligible interaction between traps, hence the trap concentration is considered low. An example depicting the P-F conduction path in 5nm HfO<sub>2</sub> with a 1.1nm SiO<sub>2</sub> interfacial layer is shown in [Figure 6.1.](#page-92-0)



<span id="page-92-0"></span>Figure 6.1: Energy band diagram of 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> nMOS device with (solid green line) and without (dotted green line) a hydrogenic trap. The diagram was created using [40], a  $\phi_{PF}$  of 0.45eV, and a relative high frequency dielectric constant of 7.8; both values were extract from the data**.** After [91].

A common method to determine if a model describes data is by linearizing the model. New input and output parameters are derived using the linearized model and plotted; if the result is linear, a case of the model can be made. This type of plot for P-F

transport is called a P-F plot where [\(2.8\)](#page-29-0) is linearized by plotting  $\ln(J/E_{ox})$  vs.  $E_{ox}^{-1/2}$ . The high frequency dielectric constant can be extracted from slope of the line, which yields  $\beta_{PF}/\zeta k_b T$  if  $\zeta$  is known; however, usually it is assumed to be 1. The trap barrier height is extracted from the *y*-intercept:

$$
\ln(C) - \frac{q\phi_{PF}}{\zeta k_b T} \,. \tag{6.1}
$$

To eliminate *C*, data from more than one temperature can be used. An alternative approach to extracting  $\phi_{PF}$  is achieved by following [20, 57] in which [\(2.8\)](#page-29-0) is linearized against the inverse of temperature instead of  $E_{ox}^{1/2}$  by:

<span id="page-93-0"></span>
$$
\ln\left(\frac{J_{PF}}{E_{ox}}\right) = -\frac{q\phi_{PF} - \beta_{PF}\sqrt{E_{ox}}}{\zeta k_b} \frac{1}{T} + \ln(C). \tag{6.2}
$$

Equation [\(6.2\)](#page-93-0) predicts Arrhenius behavior. The slope of the resulting line is proportional to the reduced trap barrier height ( $\phi_r$ ),  $q\phi_{PF}$ - $\beta_{PF}E_{ox}^{1/2}$ , which decreases as the electric field increases. The trap barrier height is found by extracting  $\phi_r$  at various electric field strengths and then extrapolating  $\phi_r$  to an electric field of zero, which yields  $\phi_{PF}$ . This latter approach to finding  $\phi_{PF}$  is the method used in this study.

# **6.2: Electric Field Calculation**

Both of the methods discussed above for calculating  $\phi_{PF}$  requires knowing the electric field. To extract the trap barrier height in the  $HfO_2^{-11}$  $HfO_2^{-11}$  $HfO_2^{-11}$ , the electric field in the  $HfO_2$  $(E_{ox, HfO2})$  should be used [10]. Various methods for calculating the electric field have been used in the literature (e.g., [16, 20, 32, 38, 41]). Simple methods used for calculating the

<span id="page-93-1"></span><sup>&</sup>lt;sup>11</sup> Assumes the traps are located in the HfO<sub>2</sub> layer which is a reasonable assumption.

electric field have the advantage of being quick and easy. However, simple approximations to the electric field compared to more accurate calculations using CV modeling programs, finite element analysis tools, or the energy band simulation tool discussed in Chapter 4, can lead to significant differences [10, 91]. The large differences in the calculated values of the electric field has a substantial impact on the calculated  $\phi_{PF}$ [91].

The electric field in a MOS device at a particular bias is not constant with temperature. The temperature dependence of the electric field depends on multiple factors, a primary one being the metal-semiconductor work function difference. However, for large doping concentrations<sup>[12](#page-94-0)</sup>, minimal variation in the electric field with temperature (10K to 400K) is observed in simulations [10]. This can be predominantly attributed to the negligible change in the semiconductor work function with temperature for large doping concentrations. Because the electric field remains nominally unchanged with respect to temperature, the temperature dependence of the electric field is assumed constant in this work.

As was mentioned above, a variety of methods exist to accurately calculate the electric field in the oxide of MOS devices. Many of these tools are proprietary, costly, and/or support only single layer dielectric oxides. The energy band simulation tool (Chapter 4) supports modeling the electric field in multiple dielectrics, is free [94], and is used in this study to extract the electric field versus gate bias. The energy band simulation tool was calibrated to the devices used in this study using the flatband voltage and materials parameters extracted by SEMATECH [64].

<span id="page-94-0"></span><sup>&</sup>lt;sup>12</sup> In this work, a doping concentration of  $1x10^{18}$  cm<sup>-3</sup> is used for all simulations

#### **6.3: Poole-Frenkel Analysis Results**

Following the second method for calculating  $\phi_{PF}$  described in Section [6.1,](#page-91-1) in which [\(6.2\)](#page-93-0) is used, the gate leakage current (e.g., [Figure 5.1](#page-64-0) and [Figure 5.2\)](#page-65-0) is examined for relatively large positive and negative gate biases to examine the gate leakage current in the transport-limited regime (see Section [5.1.1\)](#page-66-0). Recall from Section [5.2](#page-79-1) that the gate leakage current corresponds to substrate electron injection for positive gate biases and to substrate hole injection for negative gate biases. In the following subsections, P-F analysis is first applied to electron substrate injection and then to hole substrate injection. 6.3.1: Electron Substrate Injection (Positive Gate Biases)

A representative P-F plot for electron substrate injection is shown in [Figure 6.2.](#page-96-0) As was discussed in Section [6.1,](#page-91-1) [\(2.8\)](#page-29-0) predicts P-F data should be linear on a P-F plot,  $ln(J_{Gate}/E_{ox,HfO2})$  vs  $E_{ox,HfO2}^{1/2}$ . The plot of the data in [Figure 6.2](#page-96-0) is not linear over the entire electric field range shown as it has a slight curvature to it. The data in [Figure 6.2](#page-96-0) can approach linearity if a smaller electric field range is specified. However, by doing so, the range P-F emission can explain the temperature dependence of the gate leakage current is severely limited, which brings into question the validity of the P-F model.

One method to examine the deviation from linearity in [Figure 6.2](#page-96-0) (i.e., the soundness of the P-F model) is to evaluate approximations used to derive the classic P-F equation [\(2.8\)](#page-29-0). Classic P-F was derived by approximating Fermi-Dirac statistics with Boltzmann statistics. For large electric fields where the reduced trap barrier height is small, Boltzmann statistics fail to describe the thermal statistics causing non-linearities in the P-F plot; this occurs near the saturation voltage. A saturation P-F analysis approach

has been proposed in [95] and developed in [56, 96] in which Maxwell-Boltzmann statistics are replaced by Fermi-Dirac statistics to describe non-linear (e.g., saturated) P-F data. At the saturation voltage, the reduction of the barrier trap height is equal to the trap barrier height. Mathematically, this occurs when Δ*ϕPF* in [\(2.6\)](#page-28-1) equals *ϕPF*. When Δ*ϕPF* is less than  $\phi_{PF}$ , carriers are thermally ionized over the reduced trap barrier, which gives rise to a temperature dependence. When  $\Delta \phi_{PF} = \phi_{PF}$ , no barrier exists - thermal assistance is not needed for the carrier to leave the trap and the gate leakage current should not change with temperature at the saturation voltage. Saturation P-F therefore dominates when the conductivity (*JGate*/*Eox,HfO2*) for various temperatures approaches a crossing point. In this study, the conductivity data in [Figure 6.2](#page-96-0) is not observed to cross or approach crossing, indicating that the P-F saturation is not occurring. Therefore, saturation P-F analysis for the non-linear data observed in [Figure 6.2](#page-96-0) is not applicable.



<span id="page-96-0"></span>Figure 6.2: P-F plot of the gate leakage current of a 5nm  $HfO<sub>2</sub> 1.1nm SiO<sub>2</sub> pMOSFET for$ temperatures ranging from 6K to 400K. Most temperatures are not plotted to increase clarity of the data. A linear reference line has been added to the plot to demonstrate curvature in the data. Similar to [91].

The deviation from linearity could be due to the other temperature dependent mechanisms that do not dominate but influence the temperature dependence of the gate leakage current.<sup>[13](#page-97-0)</sup> P-F conduction has been cited many times in the literature as the follows the Arrhenius-type behavior predicted by ([6.2](#page-93-0)), the conductivity ( $J_{\text{Gate}}/E_{ox, HfO2}$ ) is reason for the temperature dependence of the gate leakage current (e.g., see Chapter 6 introduction) and merits an in-depth discussion of its application to the temperature data in this study. Therefore, continuing the analysis to verify whether or not the P-F transport plotted versus the inverse temperature at various electric fields as shown in [Figure 6.3.](#page-98-0) For three temperature ranges in the strong temperature dependent regime,  $\phi_r$  at various electric field strengths is extracted, assuming  $\xi = 1$ , and plotted against the square root of the electric field [\(Figure 6.4\)](#page-98-1) in order to extract  $\phi_{PF}$ . The data in [Figure 6.3](#page-98-0) are not completely linear and thus is another indication that the behavior is not standard P-F. The slope of the data is observed to increase with increasing temperature to the highest temperature (400K) for which measurements were performed. Therefore,  $\phi_r$  extracted from the data will be dependent on the temperature range used as demonstrated in [Figure](#page-98-1)  [6.4.](#page-98-1) Note that a nonlinear Arrhenius plot [\(Figure 5.17\)](#page-87-0) was observed and discussed in Section [5.3.](#page-83-0)

<span id="page-97-0"></span><sup>&</sup>lt;sup>13</sup> Other temperature dependent mechanisms might include Schottky emission, trap assisted tunneling, etc. As will be shown later, it turns out that the standard P-F mechanism does not adequately explain the data for reasons other than a non-linear P-F plot.



<span id="page-98-0"></span>Figure 6.3: Arrhenius P-F plot at various electric field strengths of a 5nm  $HfO<sub>2</sub> 1.1$ nm SiO2 pMOSFET for temperatures 200K to 400K. The data is nonlinear as demonstrated by the linear reference line. Similar to [91].



<span id="page-98-1"></span>Figure 6.4: Reduced trap barrier height  $(\phi_r)$  at various electric field strengths using three different temperature ranges from e.g. [Figure 6.3.](#page-98-0)  $\phi_r$  at flatband (vertical dashed line), or  $φ_{PF}$ , is determined by linear extrapolation, e.g. red (solid) and green (dashed) lines. Similar to [91].

Since the data in the Arrhenius P-F plot in [Figure 6.3](#page-98-0) show a slight curvature with the slope increasing as temperature increases, it is evident that [\(6.2\)](#page-93-0), obtained by linearizing [\(2.8\)](#page-29-0), cannot be applied to the data. Equation [\(2.8\)](#page-29-0) was derived assuming a single trap energy level; hence, the data does not exhibit single trap energy level behavior. The observed nonlinearity of the data may stem from several possibilities. One possibility is that several series of linear data with dissimilar slopes (i.e., various trap energy levels) may exist and combine to form non-linear data. Another possible explanation may be that the wave functions of the traps overlap due to a high defect density. Overlapping of the wave functions would lead to the potentials of the traps overlapping, which may broaden the distribution of trap energy barrier heights (*ϕPF*'s) [97]. An additional possibility might be attributed to the presence of charged traps (not considered in P-F conduction) taking part in carrier transport, which is indicative of multivalent traps, which is supported by theoretical calculations showing the five charge states of oxygen vacancies in  $HfO<sub>2</sub>$  [98].

Due to the curvature of the data, only a limited range of data can be analyzed and explained using the standard P-F model. This finding highlights two uncertainties with the P-F model. First, if the data are linear over only a narrow range of temperatures, the extracted *ϕPF* seems physically tenuous. Second, when a narrow range of temperatures is selected for analysis, then the temperatures outside the narrow temperature range are not being considered, thereby indicating that other *ϕPF's* exist.

Regardless of the cause, the curvature in the data in [Figure 6.3](#page-98-0) influences the extracted reduced trap energy barrier height  $(\phi_r)$  depending on the temperature range used to perform the linear fit. [Figure 6.4](#page-98-1) shows  $\phi_r$  extracted for a 5nm HfO<sub>2</sub> on 1.1nm SiO<sub>2</sub>

nMOSFET using three different temperature ranges. To obtain  $\phi_{PF}$ ,  $\phi_r$  is extrapolated to  $E_{\alpha x, HfO2} = 0$  shown by the dashed vertical line in [Figure 6.4.](#page-98-1) As depicted in [Figure 6.4,](#page-98-1) the temperature range used for calculating  $\phi_r$ , as well as the range of electric field strengths to perform the linear regression fit to extrapolate  $\phi_{PF}$ , yields significantly different results. The green (dashed) lines in [Figure 6.4](#page-98-1) correspond to extracting *ϕPF* using an electric field range of 900 to 1100  $(V/cm)^{1/2}$ . The red (solid) lines in [Figure 6.4](#page-98-1) correspond to a linear fit using electric field strengths ranging from 800 to 1480  $(V/cm)^{1/2}$ . Both red and green lines illustrate the wide distribution of *ϕPF*'s that can be extracted. The standard P-F model predicts a constant slope for data plotted in the manner of [Figure 6.4.](#page-98-1) The heterogeneity of the slope in [Figure 6.4](#page-98-1) suggests that P-F conduction is not an appropriate model or is limited to a small electric field range.

As was shown in [Figure 5.1](#page-64-0) and [Figure 5.2,](#page-65-0) the temperature dependence of the  $5$ nm HfO<sub>2</sub> devices differed considerably from the  $3$ nm HfO<sub>2</sub> devices. This temperature dependence difference is also observed in the P-F  $\phi_{PF}$  extraction [\(Figure 6.5\)](#page-101-0). [Figure 6.5](#page-101-0) shows the  $\phi_r$ 's for MOSFETs with 5nm HfO<sub>2</sub> and 3nm HfO<sub>2</sub>. The extracted  $\phi_{PF}$  for the n/pMOSFETs composed of 5nm HfO<sub>2</sub> is ~0.45eV below the HfO<sub>2</sub> conduction band for a low electric field fit and ~0.35eV below for a high electric field fit. The P-F analysis for n/pMOSFETs composed of 3nm HfO<sub>2</sub> results in a  $\phi_{PF}$  of ~0.23eV below the HfO<sub>2</sub> conduction band. Therefore, the HfO<sub>2</sub> thickness affects the measured  $\phi_{PF}$ . The similarly calculated  $\phi_{PF}$ 's for n and pMOSFETs verify the same traps in the HfO<sub>2</sub> are responsible for the gate leakage current whether in nMOS or pMOS configuration and thereby independent of the Si doping and related processing. However, the P-F model does not

incorporate a dielectric thickness dependence and therefore cannot explain the data in



[Figure 6.5.](#page-101-0)

<span id="page-101-0"></span>Figure 6.5: Electric field dependence of the  $\phi_r$  (extracted from temperatures ranging from  $320K$  to 400K) for 5nm HfO<sub>2</sub> and 3nm HfO<sub>2</sub> nMOSFETs. The thick grey lines represent linear fits to the data. For the 5nm  $HfO<sub>2</sub>$  devices, two linear regimes are observed and give different trap energy barriers. The thin black linear fit line for  $3$ nm HfO<sub>2</sub> devices show P-F conduction is not valid in the low field regime as  $\phi_r$  increases with the electric field instead of being reduced. Similar to [91].

A reason for the thickness dependence of calculated *ϕPF* may best be understood through [Figure 6.1. Figure 6.1](#page-92-0) shows the trap potential of a 0.45eV trap energy barrier with a relative high frequency dielectric constant of 7.8 (a high value) located in the 5nm  $HfO<sub>2</sub>$  layer. The value of the trap energy barrier was extrapolated from [Figure 6.5](#page-101-0) while the high frequency dielectric constant was extracted by calculating *β* from [Figure 6.2](#page-96-0) using 400K data and assuming  $\xi = 1$ . Because the P-F potential is based on the concept of a hydrogenic impurity, the Columbic potential between the electron and positive trap, shown in [Figure 6.1,](#page-92-0) extends over a large distance that is comparable to the  $HfO<sub>2</sub>$  layer thickness. Depending on the location of the trap and thickness of the  $HfO<sub>2</sub>$ , standard P-F

conduction may not dominate and the resulting transport mechanism becomes thickness dependent. P-F analysis, shown in [Figure 6.5,](#page-101-0) indicates that the 3nm  $HfO<sub>2</sub>$  layer contains traps with lower  $\phi_{PF}$ 's than the  $\phi_{PF}$ 's extracted for the 5nm HfO<sub>2</sub>. For the high field regime, the difference observed in  $\phi_{PF}$ 's between 3nm and 5nm HfO<sub>2</sub> may result from the large delocalized trap potential [\(Figure 6.1\)](#page-92-0) assumed by the P-F model via an effective mass approximation. A large delocalized trap potential similar in diameter to the thickness of the HfO<sub>2</sub> may reduce  $\phi_{PF}$  more than what is predicted in [\(2.6\)](#page-28-1). This supposition assumes that P-F conduction is prevalent. Conversely, the differences in observed  $\phi_{PF}$ 's between 3nm and 5nm HfO<sub>2</sub> may be due to the presence of another carrier transport mechanism. Regardless of the possible explanations to describe the observed differences, the P-F model does not consider a dielectric thickness dependence and thus is inadequate to explain the differences observed in [Figure 6.5.](#page-101-0)

For the 3nm HfO<sub>2</sub> devices shown in [Figure 6.4](#page-98-1) and [Figure 6.5,](#page-101-0)  $\phi_r$  for electric fields between ~700 and ~900 (V/cm)<sup>1/2</sup> increases with increasing field strength. If the governing carrier transport mechanism is P-F conduction,  $\phi_r$  should decrease rather than increase with increasing electric field according to  $(2.6)$ . Hence, for the 3nm HfO<sub>2</sub> devices in this study, it is evident that P-F transport does not explain the temperature dependence of the gate leakage current density for electric field strengths below ~900  $(V/cm)^{1/2}$  or gate voltages below 1V. Consequently, for typical MOSFET operation conditions,  $(V_{Gate} < -1V)$ , P-F transport is not dominant in 3nm HfO<sub>2</sub> and a different thermally activated carrier transport mechanism dominates.

Given the above analysis on electron substrate injection (positive gate biases), P-F conduction does not explain the temperature dependence of the gate leakage current.

#### 6.3.2: Hole Substrate Injection (Negative Gate Biases)

P-F analysis is performed on 3nm and 5nm  $HfO<sub>2</sub>$  n/pMOSFETs at negative gate biases in much the same way as it was performed for positive gate biases. The only difference is in nomenclature; for negative gate biases, the electric field has a minus sign to indicate the polarity. This minus sign is removed before taking the square root of the electric field in [\(6.2\)](#page-93-0) (i.e., no imaginary numbers are used) and replaced after calculating the square root, signifying the polarity (i.e., negative gate biases). This preservation of the polarity of the electric field is evident in the figures discussed below.

A P-F plot for negative gate biases is shown in [Figure 6.6](#page-104-0) that is typical for data obtained from 5nm  $HfO<sub>2</sub>/1.1$ nm pMOSFETs. The P-F plot for negative gate biases show more linearity (see linear reference line in [Figure 6.6\)](#page-104-0) than exhibited by PF plots for positive gate biases (e.g., [Figure 6.2\)](#page-96-0). However, the Arrhenius P-F plot [\(Figure 6.7\)](#page-105-0) is as nonlinear as the Arrhenius P-F plot for positive gate biases [\(Figure](#page-98-0) 6.3). The nonlinear Arrhenius P-F plot indicates that P-F conduction does not describe the temperature dependence of the gate leakage current over the temperature range investigated. Similar arguments given for the nonlinear Arrhenius P-F plot for positive gate biases can also be presented here (see discussion of [Figure 6.3\)](#page-98-0).



<span id="page-104-0"></span>Figure 6.6: P-F plot of a 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> pMOSFET for negative gate biases. The negative *Eox,HfO2* values on the *x*-axis indicate the polarity of the electric field. Most temperatures are not plotted to increase clarity of the data. A linear reference line has been added to the plot to demonstrate curvature in the data.

The curvature of the Arrhenius P-F plot [\(Figure 6.7\)](#page-105-0) leads to multiple  $\phi_{PF}$ 's depending on the temperature range used as was demonstrated for positive gate biases, shown in [Figure 6.4.](#page-98-1) [Figure 6.8](#page-106-0) shows  $\phi_r$  as a function of the square root of electric field for three temperature ranges: 320K to 400K, 280K to 360K, and 220K to 300K. The lower the temperature range used to extract  $\phi_r$  results in a lower calculated  $\phi_{PF}$ , as demonstrated by the linear extrapolation lines for the various temperature ranges shown in [Figure 6.8.](#page-106-0) The extraction of multiple  $\phi_{PF}$ 's depending on the temperature range used indicates that P-F does not describe the temperature dependence of the gate leakage current or at least does not dominate. The electric field range, over which the linear fit to extrapolate  $\phi_{PF}$  is performed, influences the result since  $\phi_r$  versus  $E_{ox,HfO2}^{1/2}$  is nonlinear. An interesting feature in [Figure 6.8](#page-106-0) is that as  $E_{ox,HfO2}^{1/2}$  increase above 1,000 (V/cm)<sup>1/2</sup> for the 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> devices,  $\phi_r$  increases rather than decreases as is predicted by P-

F conduction. The increase in  $\phi_r$  as  $E_{ox,HfO2}$  increases is another indication that P-F conduction does not describe the gate leakage current.



<span id="page-105-0"></span>Figure 6.7: Arrhenius P-F plot at select electric field strengths of a 5nm  $HfO_2/1.1$ nm Si $O_2$ pMOSFET for temperatures 50K to 400K. The data is nonlinear as demonstrated by the linear reference line. The negative *Eox,HfO2* values indicate the polarity of the electric field.

The extracted values for  $\phi_{PF}$  is ~0.11eV for the 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> devices extracted from a temperature range of 320K to 400K and ~50meV for the 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  devices over the same temperature range. The difference in the extracted  $\phi_{PF}$  between 5nm and 3nm HfO<sub>2</sub> devices illustrates a limitation with P-F conduction as an explanation of the gate leakage current that also occurred when analyzing positive gate voltage currents. That is, the standard P-F conduction mechanism does not predict a thickness dependence; it is independent of thickness.



<span id="page-106-0"></span>Figure 6.8: Electric field dependence of the  $\phi_r$  (extracted from three temperature ranges) for 5nm  $HfO<sub>2</sub>$  (open symbols) and 3nm  $HfO<sub>2</sub>$  (closed symbols) n/pMOSFETs. The thick grey represent linear extrapolations to  $E_{ox,HfO2}^{1/2} = 0$  for which  $\phi_{PF}$ 's are extracted. For high electric fields,  $\phi_r$  increases as  $E_{ox, HfO2}$  increases instead of decreasing, indicating that P-F conduction does not describe the gate leakage data.

Additional evidence that suggests the data does not conform to the framework of the P-F model concerns the magnitude of the extracted value  $\phi_{PF}$  (a maximum of  $\sim$ 0.11eV was extracted). Given the location of the trap ( $\sim$ 0.11eV above the HfO<sub>2</sub> valance band), it is unlikely that the trap is filled over the voltage range of interest  $(|V_{Gate}| < |-2V|)$ due to the energy difference between the Fermi energy level in the Si (source of the hole carriers) compared to the trap energy level extracted by the P-F analysis performed here. The smallest energy level difference occurs when  $V_{Gate} = -2V$  for which an energy band diagram is shown in [Figure 6.9.](#page-107-0) An energy level difference of ~2.5eV and ~1.9eV exists between the defects and Si Fermi level at the  $HfO_2/SiO_2$  and TiN/HfO<sub>2</sub> interface respectively at  $V_{Gate} = -2V$ , indicated by the arrows in [Figure 6.9.](#page-107-0) The large energy difference between the extract trap energy and Si Fermi energy level [\(Figure 6.9\)](#page-107-0)

indicates that capture of holes is unlikely for which thermal emission of the holes from the traps described by P-F is also unlikely. The large energy difference also calls into question whether thermal emission of holes from the trap (a small energy difference, [Figure 6.9\)](#page-107-0) is the limiting process for current conduction, which P-F conduction assumes. It would be more likely that hole capture by traps [\(Figure 6.9\)](#page-107-0) is the limiting process for such a scenario. This is another indication that P-F conduction does not explain the temperature dependence of the gate leakage current.



<span id="page-107-0"></span>Figure 6.9: Energy band diagram showing the deepest extracted defect level (dashed red line,  $0.11$ eV above the HfO<sub>2</sub> valance band) from the P-F analysis in comparison to the Fermi energy level in the Si (thick blue line). A large energy difference exists between the defect and Si Fermi energy level.

While P-F conduction has been used in the literature to explain the temperature dependence of the gate leakage current [7, 21, 92, 93], a thorough analysis of P-F conduction on the gate leakage temperature dependence indicates that for the devices and temperature range used, P-F conduction does not explain the gate leakage current for the
positive or negative gate bias regime. A variety of reasons were given for this conclusion, including:

- 1. For the positive gate bias regimes, the P-F plot is nonlinear over a large electric field range for positive gate biases [\(Figure 6.2\)](#page-96-0).
- 2. The Arrhenius P-F plots are nonlinear [\(Figure 6.3](#page-98-0) and [Figure 6.7\)](#page-105-0) for which many different trap barrier heights can be extracted depending on the temperature range examined. The standard P-F model was developed for mono-energetic defect levels for which a linear Arrhenius P-F plot is expected. The standard P-F model is therefore only able to describe a small temperature range.
- 3. Nonlinear  $\phi_r$ 's with respect to  $E_{ox,HfO2}^{1/2}$  were obtained for which different *ϕPF*'s can be extracted depending on the choice of electric field range used to perform the linear extrapolation [\(Figure 6.5\)](#page-101-0). The small electric field range (which can then be approximated as linear) is evidence that the P-F conduction mechanism provides an inappropriate explanation to the gate leakage dependence.
- 4. A thickness dependence exists between the 3nm and 5nm  $HfO<sub>2</sub>$  devices for which the P-F model does not predict.
- 5. For the negative gate bias regime, the extracted trap energy level is nonsensical, yielding a shallow defect energy requiring a large thermal emission of holes from the Si to populate the energy level. This would result in a defect filling-limited transport mechanism and not thermal emission from the defect (P-F) as the limiting mechanism.

6. For 5nm HfO<sub>2</sub> devices at large negative biases  $(|E_{ox,HfO2}|^2 > |-1000| (V/cm)^{1/2})$ and for 3nm HfO<sub>2</sub> devices in the positive biases regime at small negative biases ( $E_{ox,HfO2}$  < 700 (V/cm)<sup>1/2</sup>),  $\phi_r$  *increases* as the magnitude of the electric field increases. According to the P-F model *ϕ<sup>r</sup>* should *decrease* as the magnitude of the electric field increases not *increase*.

Based on reasons summarized above, P-F does not explain the temperature dependence of the gate leakage current and other temperature dependent mechanism should be explored.

### CHAPTER 7: SCHOTTKY ANALYSIS

Another popular carrier transport mechanism that may be used to explain the temperature dependence of the gate leakage current in  $HfO<sub>2</sub>$  devices is Schottky emission (e.g., [7, 23, 33, 34, 41, 61, 99]). However, Schottky emission discussed in the literature relative to  $HfO<sub>2</sub>$  only considers carrier emission into the  $HfO<sub>2</sub>$  dielectric conduction band from the gate electrode or substrate injection assuming an interfacial layer does not exists between the HfO<sub>2</sub> and substrate. For the devices used in this study, a 1.1nm  $SiO<sub>2</sub>$ interfacial layer is present between the  $HfO<sub>2</sub>$  and Si substrate, which must be considered when modeling thermionic charge injection from the substrate into the  $HfO<sub>2</sub>$  conduction band. In this chapter, a simple model taking into account the presence of the interfacial layer is developed. Application of the model is then applied to the gate leakage data of this study for both electron substrate injection and hole substrate injection.

#### **7.1: Image Charge in multilayer dielectrics**

An introduction to Schottky emission was given in Section [2.4](#page-31-0) for a single dielectric. Schottky emission is the process in which the carriers are thermally stimulated into the conduction band of the dielectric. The energy required to reach the conduction band of the dielectric is decreased (reduced barrier height,  $\phi_r$ ) in the presence of an electric field due to the image charge theorem. The derivation of Schottky emission can be performed following [100] where the potential energy (PE) of the barrier (in units of Joules) as a function of distance is written as:

$$
PE(x) = q\phi_B - qxE_{ox} - \frac{q^2}{16\pi\varepsilon_r\varepsilon_0 x}.
$$
\n(7.1)

<span id="page-111-0"></span>The first term in [\(7.1\)](#page-111-0) is the barrier height ( $\phi_B$ , in units of eV), which corresponds to the conduction band offset (for electrons) or valance band offset (for holes) if thermal stimulation is from a semiconductor. The first term could also refer to the metal work function dielectric conduction band offset (for electrons) or metal work function dielectric valance band offset (for holes) if thermal stimulation is from the Fermi energy of a metal. The second term considers the change in the potential energy in the presences of an electric field. The third term is the Coulomb potential due to the image charge theorem; see [\(4.11\)](#page-50-0). Identifying the reduced potential barrier height as a function of the electric field is determined by finding the distance where the maximum of [\(7.1\)](#page-111-0) occurs (denoted here as  $x_{max}$ ) and then solving  $PE(x_{max})$ . The value  $x_{max}$  is determined by setting the derivative of  $(7.1)$  to zero and solving for *x*, which yields:

$$
x_{\text{max}} = \frac{1}{4} \sqrt{\frac{q}{\pi \varepsilon_0 \varepsilon_r E_{\text{ox}}}} \,. \tag{7.2}
$$

<span id="page-111-3"></span>The reduced trap barrier height,  $PE(x_{max})$ , can then be written as:

<span id="page-111-2"></span>
$$
PE(x_{max}) = q(\phi_B - \sqrt{qE_{ox}/4\pi\varepsilon_r\varepsilon_0}).
$$
\n(7.3)

Carriers are stimulated over the barrier by thermionic emission described by the Richardson equation [101, 102]:

<span id="page-111-1"></span>
$$
J = A * T^2 \exp\left(\frac{-q\phi}{k_b T}\right),\tag{7.4}
$$

where  $A^*$  is the effective Richardson constant given in Section [2.4](#page-31-0) and  $\phi$  is the barrier height. The Schottky emission equation is found by replacing  $\phi$  in [\(7.4\)](#page-111-1) with the reduced barrier height [\(7.3\)](#page-111-2), written here again for convenience:

<span id="page-112-0"></span>
$$
J_{SE} = A^*T^2 \exp\left(\frac{-q(\phi_B - \sqrt{qE_{ox}/4\pi\varepsilon_r \varepsilon_0})}{k_b T}\right). \tag{7.5}
$$

For thick single layer dielectrics, [\(7.3\)](#page-111-2) is a good approximation to the barrier height. However, as the layer thickness decreases, the image charge effects of both conductors becomes more important. An example of a thin  $1.2$ nm SiO<sub>2</sub> barrier considering the image charge effects of only the semiconductor and both the semiconductor and metal is shown by the energy band diagram in [Figure 7.1](#page-113-0) using the Image Charge Model outlined in Section [4.1.4](#page-49-0) and a relative high frequency dielectric constant of 2.38 for the  $SiO<sub>2</sub>$  layer [103]. [Figure 7.1](#page-113-0) shows a noticeable decrease in the barrier height (~128meV) when image charge effects of both the metal and semiconductor are considered compared to only the semiconductor.



<span id="page-113-0"></span>Figure 7.1: Energy band diagram of a TiN/1.2nm  $SiO<sub>2</sub>/Si$  nMOSFET considering image charge effects of only the semiconductor and both the semiconductor and metal. A difference of ~128meV exists between the barrier heights of the two calculations. Created using [40].

Similar to ultra thin dielectrics, where the effects two conductors must be considered, multilayer dielectrics also present situations for which Schottky emission does not describe thermionic emission. For example, if another dielectric has a larger conduction band offset than the dielectric adjacent to the conductor from which carrier injection is occurring (e.g., metal-SiO<sub>2</sub> band offset is greater than that of metal-HfO<sub>2</sub>), [\(7.5\)](#page-112-0) may not apply. The maximum barrier height of the gate stack, for which thermionic conduction should be considered, may not be due to the image charge interaction with the first dielectric (i.e., the dielectric adjacent to the conductor). While image charge effects on the first dielectric does modify the maximum barrier height of the first dielectric, the band offset of another dielectric with respect to the conductor may be large enough that the maximum barrier height of the gate *stack* is controlled by the barrier height of the non-adjacent dielectric. An example of the second dielectric being the maximum barrier

height is illustrated using a  $HfO<sub>2</sub>$  (with a high frequency dielectric constant of 4, [104])  $SiO<sub>2</sub>$  bilayer shown in [Figure 7.2.](#page-114-0) The  $SiO<sub>2</sub>$  layer in [Figure 7.2](#page-114-0) controls the barrier height for thermionic emission due to the larger conduction band offset of  $SiO<sub>2</sub>$  with TiN compared to the conduction band offset of  $HfO<sub>2</sub>$  to TiN. Because the  $SiO<sub>2</sub>$  has the largest band offset of any of the dielectrics in the gate stack, its band offset with the metal Fermi energy level is the maximum barrier height for an electron injected from the gate metal. However, the  $SiO<sub>2</sub>$  layer is not adjacent to the gate metal and hence cannot not described by [\(7.3\)](#page-111-2). Therefore, Schottky emission, expressed by [\(7.5\)](#page-112-0), does not model electron gate thermionic emission in [Figure 7.2.](#page-114-0) This is one example of the limited use of [\(7.5\)](#page-112-0) when considering multilayer dielectrics and illustrates the attention that is required when using (7.5) to analyze a multilayer dielectric gate stack.



<span id="page-114-0"></span>Figure 7.2: Energy band diagram of a TiN/3nm HfO $\frac{1}{2}$  (1nm SiO $\frac{1}{2}$ Si nMOSFET biased at -2V. Image charges are used in the calculation of the dielectric conduction band. The barrier height for thermionic emission of electrons from the metal gate is dictated by the barrier height of the second dielectric  $(SiO<sub>2</sub>)$  not the first dielectric adjacent to the metal gate (HfO<sub>2</sub>). Created using [40].

Another example in which Schottky emission does not describe thermionic emission in multilayer dielectrics is illustrated by examining  $x_{max}$  in [\(7.2\)](#page-111-3). For Schottky emission in a multilayer dielectric stack, [\(7.5\)](#page-112-0) is only valid if  $x_{max}$  as described by [\(7.2\)](#page-111-3) resides within the layer adjacent to the conductor from which thermionic emission is considered.<sup>[14](#page-115-0)</sup> Equation [\(7.2\)](#page-111-3) indicates that as the electric field approaches zero  $x_{max}$ approaches infinity. One can envision that at a low enough electric field an *xmax* that is greater than the thickness of the dielectric adjacent to the conductor could result. This situation is highlighted by considering thermionic emission at positive gate biases for the 3 or 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  dielectric gate stacks measured in this study. [Figure 7.3](#page-116-0) shows the energy band diagram for a 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  dielectric stack for substrate electron injection. The dielectric barriers are calculated three different ways in [Figure 7.3:](#page-116-0) 1) without image charge effects (dashed lines), 2) with image charge effects only due to the semiconductor mimicking the barrier lowering described by Schottky emission (thin lines labeled "Schottky image" in [Figure 7.3\)](#page-116-0), and 3) with image charge effects due to both the conductor-dielectric interfaces and dielectric-dielectric interfaces (thick lines labeled "image charge" in [Figure 7.3\)](#page-116-0). A slight difference in the maximum barrier height is observed between the "Schottky image" and the "image charge" due to the  $SiO<sub>2</sub>$ dielectric –  $HfO<sub>2</sub>$  dielectric interaction. For the maximum barrier height calculated using the "Schottky image", [\(7.3\)](#page-111-2), to approximate the maximum barrier height calculated considering the dielectric-dielectric interface ("image charge"), *xmax* must be slightly less than the dielectric thickness. [Figure 7.4](#page-117-0) plots the location of *xmax* as a function of electric

<span id="page-115-0"></span><sup>&</sup>lt;sup>14</sup> The argument of the importance of the location of  $x_{max}$  also applies to thin single layer dielectrics. In multilayer dielectrics however, layers can be very thin without risk of large leakage currents due to direct tunneling if additional layers are present. Indeed, this situation is more common.

field for the  $SiO<sub>2</sub>$  IL in this study. For electric fields below  $\sim$ 1.25MV/cm, the calculated peak of the barrier height resides at or beyond the  $SiO<sub>2</sub> IL$ , which is 1.1nm thick and [\(7.3\)](#page-111-2) fails to describe the maximum barrier height. Conventional Schottky analysis should therefore be performed at electric fields above ~1.25MV/cm for the devices in this study.



<span id="page-116-0"></span>Figure 7.3: Energy band diagram of a 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  nMOSFET. The dielectric barriers are shown calculated (dashed line) with image charge effects, (solid thin lines) image charge due only to the semiconductor, and (solid thick lines) image charge due to the semiconductor, dielectric interfaces, and metal gate. The majority of the barrier lowering occurs in the  $SiO<sub>2</sub>$  IL while no appreciable barrier lowering occurs in the HfO<sub>2</sub> layer. Created using [40].



<span id="page-117-0"></span>Figure 7.4: Plot of the distance where the maximum barrier height occurs,  $x_{max}$ , as a function of electric field in the  $SiO<sub>2</sub>$  interfacial layer for the high frequency dielectric constant of SiO<sub>2</sub>,  $\varepsilon$ <sub>*r*</sub> = 2.38. The plot indicates that electric fields above ~1.25MV/cm can be analyzed using  $(7.5)$  for the SiO<sub>2</sub> IL 1.1nm thick.

In contrast to the examples given above where Schottky emission did not describe thermionic emission, for the  $HfO_2/SiO_2$  dielectric stack in this study, Schottky conduction as expressed by  $(7.5)$  does describe thermionic emission from the substrate over the  $SiO<sub>2</sub>$ IL. However, according to [Figure 7.4,](#page-117-0) this is only true when the electric fields in the  $SiO<sub>2</sub>$ layer are above ~1.25MV/cm. The reasons that Schottky emission from the substrate over the  $SiO<sub>2</sub>$  can be safely examined are two-fold. First, carrier separation analysis, section [5.2,](#page-79-0) reveals that the gate leakage current corresponds to substrate injection for positive gate biases (electron injection) and negative gate biases (hole injection). The maximum barrier height in the HfO<sub>2</sub>/SiO<sub>2</sub> bilayer is dictated by the SiO<sub>2</sub> layer as is shown in Figure [7.2](#page-114-0) and described in the associated discussion. Since carrier transport originates from the substrate and the adjacent dielectric  $(SiO<sub>2</sub> layer)$  dictates the maximum barrier height for both electrons and holes, Schottky emission correctly describes thermionic emission over

the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  bilayer barrier. Second, as was described using [Figure 7.4,](#page-117-0) for analysis performed for a  $SiO_2$  electric field above  $\sim$ 1.25MV/cm, the location where the maximum barrier occurs resides in the  $SiO<sub>2</sub>$  layer, which is necessary for Schottky emission to apply. Schottky analysis can therefore be applied to the  $HfO_2/SiO_2$  stacks used in this study to determine if Schottky emission describes the temperature dependence of the gate leakage current.

Schottky analysis is performed in much the same way as P-F conduction analysis was performed in Section [6.1](#page-91-0) since  $(7.5)$  is an Arrhenius-like equation. The activation energy of the Arrhenius equation, which corresponds to the reduced barrier height given by [\(7.3\)](#page-111-2), is derived from the slope at various  $E_{ox, SiO2}^{1/2}$  points taken from the inverse temperature linearized form of [\(7.5\)](#page-112-0):

<span id="page-118-0"></span>
$$
\ln\left(\frac{J_{SE}}{T^2}\right) = -\frac{q(\phi_B - \sqrt{qE_{ox}/4\pi\varepsilon_0\varepsilon_r})}{k_b} \frac{1}{T} + \ln(A^*). \tag{7.6}
$$

The barrier height at flatband, which should correspond to the  $SiO<sub>2</sub>/Si$ conduction/valance band offset, is then determined by linear extrapolation of the activation energy versus  $E_{ox,SiO2}^{1/2}$  [ $E_{ox}$  in [\(7.6\)](#page-118-0)] to the point at which  $E_{ox,SiO2}^{1/2}$  is equal to zero. The electric field in the  $SiO<sub>2</sub>$  layer was extracted using the energy band simulation tool described in Chapter 4. Performing Schottky analysis of the temperature dependent gate leakage data in this study however, reveals an extracted barrier height of  $\sim 0.4 \text{eV}$ , which is considerably smaller than the  $SiO<sub>2</sub>/Si$  conduction band offset of 3.1eV for positive gate biases. Schottky analysis for nMOSFETs biased at negative voltages is physically non-sensical as the extracted activation energy is negative. Schottky analysis for 5nm HfO<sub>2</sub> pMOSFETs at negative gate biases results in a barrier height of  $\sim 0.2 \text{eV}$ ,

which is significantly smaller than the  $SiO<sub>2</sub>/Si$  valance band offset of 4.68eV. Since the extracted barrier height does not match the band offset, thermionic emission of carriers over the  $SiO<sub>2</sub>$  IL is not occurring.

This perhaps is not a surprising result given that the highest temperature for which devices were measured was 400K and the conduction and valance band offset of the  $SiO<sub>2</sub>/Si$  interface is very large. Consideration should be given to emission through the  $SiO<sub>2</sub>$  (via tunneling, assumed in this argument to be a non-limiting mechanism) into the  $HfO<sub>2</sub>$  conduction band since  $HfO<sub>2</sub>$  has a band offset of 1.4eV, a much lower value than the  $SiO<sub>2</sub>/Si$  conduction band offset of 3.1eV. Inspection of the reduced barrier height of the HfO<sub>2</sub> conduction band with respect to the Femi energy level of the Si in a 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> nMOSFET at  $V_{Gate} = 2V$  reveals a barrier of only 0.48eV. The reduced barrier height of  $0.48$ eV is small enough that if tunneling through the  $SiO<sub>2</sub>$  layer can be considered as non-limiting, then thermionic emission into the  $HfO<sub>2</sub>$  conduction band may explain the temperature dependence of the gate leakage current.

[Figure 7.3](#page-116-0) shows the energy band diagram of thermionic stimulation of carriers above the HfO<sub>2</sub> conduction band where tunneling can take place through the thin  $SiO<sub>2</sub>$ layer. As observed in [Figure 7.3,](#page-116-0) the maximum barrier height of the  $HfO<sub>2</sub>$  is not affected significantly by image charge effects. The maximum barrier height of the  $HfO<sub>2</sub>$  in relation to the Si band edge at the  $SiO<sub>2</sub>/Si$  interface (neglecting image charge effects) is instead reduced by the potential drop in the in  $SiO_2$  layer  $V_{ox,SiO2}$ , or:

<span id="page-119-0"></span>
$$
V_{\alpha,\text{SiO}_2} = E_{\alpha,\text{SiO}_2} t_{\alpha,\text{SiO}_2} \tag{7.7}
$$

where  $E_{\alpha x, SiO2}$  is the electric field in the SiO<sub>2</sub> layer (without image charge effects) and  $t_{ox,SiO2}$  is the thickness of the SiO<sub>2</sub> layer. The HfO<sub>2</sub> barrier height is lowered by  $V_{ox,SiO2}$  and following Schottky in modifying Richardson's thermionic emission equation, the thermionic assisted tunneling (TAT) current is written as:

<span id="page-120-0"></span>
$$
J_{TAT} = A * T^2 \exp\left(\frac{-q(\phi_B - E_{ox, SiO_2} t_{ox, SiO_2})}{k_b T}\right).
$$
 (7.8)

Determining if [\(7.8\)](#page-120-0) describes the temperature dependence of the gate leakage current is performed by extracting  $\phi_B$  using the relationship described in [\(7.8\)](#page-120-0) and comparing it to the HfO<sub>2</sub>/Si conduction and valance band offsets, which are  $\sim$ 1.4eV and  $\sim$ 3.18eV, respectively.[15](#page-120-2)

Extracting  $\phi_B$  using [\(7.8\)](#page-120-0) is done using the same method that was used for Schottky emission and P-F conduction in Chapter 6, which is to linearize [\(7.8\)](#page-120-0) versus the inverse of temperature as follows:

<span id="page-120-1"></span>
$$
\ln\left(\frac{J_{TAT}}{T^2}\right) = -\frac{q(\phi_B - E_{ox, SiO_2}t_{ox, SiO_2})}{k_b} \frac{1}{T} + \ln(A^*).
$$
 (7.9)

Equation [\(7.9\)](#page-120-1) reveals that data described by [\(7.8\)](#page-120-0) plotted as  $\ln(J_{Gate}/T^2)$  versus  $1/T$ should result in a straight line whose slope is proportional to the activation energy,  $(\phi_B - E_{ox,SiO2}t_{ox,SiO2})$ . Plotting the activation energy versus  $E_{ox,SiO2}$  should result in a *y*intercept of  $\phi_B$  and a slope of  $t_{ox,SiO2}$ . In the following sections, this method of extracting  $\phi_B$  is applied to the temperature dependence of the gate leakage current for both positive and negative gate biases to determine if [\(7.8\)](#page-120-0) describes the data. The method of extracting  $\phi_B$  for TAT, [\(7.8\)](#page-120-0), is very similar to the method for extracting  $\phi_B$  for Schottky emission, [\(7.5\)](#page-112-0), except  $E_{ox,SiO2}$  is used in TAT instead of  $E_{ox,SiO2}^{1/2}$ , which is used for Schottky. Due to these similarities, much of the commentary and discussion of the data in relation to

<span id="page-120-2"></span> $15$  Another method to determine if [\(7.8\)](#page-120-0) describes the temperature dependence of the data is by examining if the slope of the activation energy versus  $E_{\alpha x, SiO2}$  plot results in the  $SiO_2$  thickness of 1.1nm.

TAT can also be applied to Schottky emission. Where appropriate, discussion of the data in relation to Schottky emission is included as a supplemental discussion to the brief discussion of Schottky emission above.

# **7.2: Analysis of Thermionic Assisted Electron Tunneling Current**

To examine the validity of the TAT model, a representative TAT characteristic plot,  $\ln(J_{\text{Gate}}/T^2)$  versus  $E_{\text{ox,SiO2}}$ , for positive gate biases is shown in [Figure 7.5.](#page-122-0) Notice that the characteristic TAT plot shown in [Figure 7.5](#page-122-0) is similar to a characteristic Schottky plot except for the *x*-axis, which plotted as  $E_{ox,SiO2}$  (TAT) instead of  $E_{ox,SiO2}^{1/2}$  (Schottky). The data in [Figure 7.5](#page-122-0) is observed to have a slight curvature (as shown by comparison to the linear reference line) over the large electric field range shown  $\left(\sim 2MV/cm\right)$  to  $\sim 7MV/cm$ ), which limits the validity of TAT as an explanation to the temperature dependence of the gate leakage current. In order for the data to be considered linear, as predicted by [\(7.9\)](#page-120-1), only a relatively small electric field range can be used.



<span id="page-122-0"></span>Figure 7.5: A characteristic thermionic stimulated tunneling current plot,  $\ln(J_{\text{Gate}}/T^2)$ versus  $E_{ox,SiO2}$ , for a 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> nMOSFET. A linear reference line has been added for comparison.

Additionally, [Figure 7.5](#page-122-0) shows that for the majority of the temperatures examined,  $\ln(J_{Gate}/T^2)$  decreases as the temperature increases as indicated by the arrow. A clearer representation of this trend is shown in [Figure 7.6](#page-123-0) where  $\ln(J_{Gate}/T^2)$  is plotted versus  $1/T$  for select  $E_{ox,SiO2}$  values. For temperatures below  $\sim$ 240K,  $\ln(J_{Gate}/T^2)$  increases as the temperature decreases and results in a negative activation energy, which is physically implausible for thermionic emission. Only for temperatures above ~240K does the data have negative slope, which results in a positive activation energy. Due to the negative activation energy for temperature below ~240K, TAT and Schottky emission fail to explain the temperature dependence of the gate leakage current in this temperature range.



<span id="page-123-0"></span>Figure 7.6: Characteristic thermionic stimulated tunneling current plot,  $\ln(J_{\text{Gate}}/T^2)$  versus  $1/T$  of a 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> nMOSFET for select SiO<sub>2</sub> electric fields. For temperatures below  $\sim$  240K, the increasing  $\ln(J_{\text{Gate}}/T^2)$  values for decreasing temperatures results in a negative activation energy, which is physically non-sensical for thermionic emission.

The data for  $T > -240K$  is nonlinear, which results in an activation energy that is dependent on the temperature ranges chosen to perform the extraction, indicating that the behavior of the data is not Arrhenius. Similar observations of a temperature rangedependent activation energy were made during P-F analysis (Section [6.3\)](#page-95-0) and the Arrhenius analysis (Section [5.3\)](#page-83-0). Extracting the activation energy using temperatures 360K to 400K results in [Figure 7.7.](#page-124-0) The activation energy is nonlinear with respect to  $E_{\alpha x,SiO2}$  and results in a barrier height extrapolation that depends on the electric field range over which the linear fit is performed. A significant difference in the range of activation energies is also observed between devices composed of 3nm and 5nm HfO2. Since both of the stack types have the same  $SiO<sub>2</sub>$  IL thickness, the activation energy at a given  $E_{\alpha x, SiO2}$  (or  $E_{\alpha x, SiO2}^{1/2}$  for Schottky emission) should be the same according to (7.9) and

(7.6). Hence, TAT (or Schottky emission) does not explain the temperature dependence of the gate leakage current. A linear extrapolation of the activation energy [\(Figure 7.7\)](#page-124-0) to  $E_{\alpha x,SiQ2} = 0$  results in a  $\phi_B$  ranging from ~0.15eV to ~0.4eV, which is significantly lower than the HfO<sub>2</sub>/Si conduction band offset of  $\sim$ 1.4eV. This disparity is another indication that TAT does not explain the temperature dependence of the gate leakage current for the positive gate bias regime.



<span id="page-124-0"></span>Figure 7.7: Activation energy (or reduced barrier height) versus  $SiO<sub>2</sub>$  electric field for n/pMOSFETs composed of 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  and 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$ . The barrier height at flatband is derived using linear extrapolation to zero electric field (dashed vertical line). Various barrier heights from ~0.15eV to ~0.4eV can be extracted depending on the device, stack type, and electric field ranged used.

# **7.3: Analysis of Thermionic Assisted Hole Tunneling Current**

The validity of the TAT model is analyzed using the gate leakage current at negative gate biases, which corresponds to substrate hole injection. A characteristic ln(*JGate*/*T*<sup>2</sup> ) versus *Eox,SiO2* plot is shown in [Figure 7.8.](#page-125-0) The negative sign on *Eox,SiO2* indicates the polarity of the electric field. A slight curvature in the data is observed in the

data as shown by comparison to the linear reference line. According to [\(7.9\)](#page-120-1), the data should be linear. As temperature increases,  $\ln(J_{\text{Gate}}/T^2)$  decreases for most of the temperature range. Plots of  $\ln(J_{\text{Gate}}/T^2)$  versus  $1/T$  are shown in [Figure 7.9](#page-127-0) and Figure [7.10](#page-128-0) for several  $HfO<sub>2</sub>$  gate stacks.



<span id="page-125-0"></span>Figure 7.8: A characteristic thermionic stimulated tunneling current plot,  $\ln(J_{\text{Gate}}/T^2)$ versus  $E_{ox,SiO2}$ , for a 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> pMOSFET. A linear reference line has been added for comparison.

[Figure 7.9](#page-127-0) is a characteristic thermionic Arrhenius plot for a 3nm  $HfO<sub>2</sub>$ 

nMOSFET. Similar behavior were also observed for data from 3nm HfO<sub>2</sub> pMOSFETs and  $5$ nm HfO<sub>2</sub> nMOSFETs and are not shown for brevity. [Figure 7.10](#page-128-0) is a representative plot of 5nm  $HfO<sub>2</sub>$  pMOSFETs. Except for 5nm  $HfO<sub>2</sub>$  pMOSFETs [\(Figure 7.10\)](#page-128-0), the slope for the inverse temperature plots (e.g., [Figure 7.9\)](#page-127-0) is positive, which results in a negative activation energy. The negative activation energy indicates that the TAT/Schottky model does not fit the data.

For 5nm HfO2 pMOSFETs [\(Figure 7.10\)](#page-128-0), a negative slope is shown in the 1/*T* plot for temperatures above ~360K. Activation energies extracted from these slopes are very small however; less than  $\sim 0.1$ eV. In addition, for  $E_{ox,SiO2} = -3MV/cm$  to  $-4.5MV/cm$  the activation energy increases rather than decreases as the electric field increases (data not shown). Equation [\(7.9\)](#page-120-1) predicts that the activation energy,  $(\phi_B - E_{ox,SiO2}t_{ox,SiO2})$ , should decrease as  $E_{ox, SiO2}$  increases.<sup>[16](#page-126-0)</sup> The incorrect change in the activation energy with electric field indicates that the gate leakage current of the  $5<sub>nm</sub>$  HfO<sub>2</sub> pMOSFETs is not explained by TAT/Schottky conduction. A linear fit to the point at which the activation energy decreases as the electric field increases  $(E_{ox,SiO2} = -2MV/cm)$  to  $-3MV/cm$ ) results in an extracted  $\phi_B = \sim 70$ meV, which is significantly smaller than the HfO<sub>2</sub>/SiO<sub>2</sub> valance band offset of ~3.18eV. The large discrepancy between the valance band offset and the extracted  $\phi_B$  indicates that TAT does not model the data.

<span id="page-126-0"></span><sup>&</sup>lt;sup>16</sup> Note in ([7.5\)](#page-112-0), [\(7.7\)](#page-119-0), [\(7.8\)](#page-120-0) and [\(7.9\)](#page-120-1) and other similar equations that the electric field term refers to the magnitude of the electric field which is a positive value. The minus sign in a negative electric field value refers to its polarity. The activation energy should decrease for larger magnitude values regardless of its polarity.



<span id="page-127-0"></span>Figure 7.9: Characteristic thermionic stimulated tunneling current plot,  $\ln(J_{\text{Gate}}/T^2)$ versus  $1/T$  of a 3nm  $HfO_2/1.1$ nm SiO<sub>2</sub> nMOSFET for select SiO<sub>2</sub> electric fields. For temperatures below ~400K, the increasing  $\ln(J_{\text{Gate}}/T^2)$  values for decreasing temperatures results in a negative activation energy, which is physically invalid for thermionic emission.



<span id="page-128-0"></span>Figure 7.10: Characteristic thermionic stimulated tunneling current plot,  $\ln(J_{\text{Gate}}/T^2)$ versus  $1/T$  of a 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> MOSFET for select SiO<sub>2</sub> electric fields. For temperatures below ~360K, the increasing  $\ln(J_{\text{Gate}}/T^2)$  values for decreasing temperatures results in a negative activation energy, which is physically implausible for thermionic emission.

In summary, models using thermionic emission over the  $SiO<sub>2</sub>$  layer (Schottky emission) or into the HfO<sub>2</sub> conduction/valance band, via tunneling through the  $SiO<sub>2</sub>$ (TAT), does not explain the temperature dependence of the gate leakage current for positive or negative gate biases. The data fail to follow the Schottky and TAT models based on the following observations:

- 1. Nonlinear (i.e., non-Arrhenius) behavior of the characteristic plot of  $\ln(J_{Gate}/T^2)$  versus  $E_{ox,SiO2}$ , which is predicted by TAT, [\(7.9\)](#page-120-1). Nonlinear behavior of the characteristic plots for Schottky emission  $[\ln(J_{\text{Gate}}/T^2)$  versus  $E_{ox,SiO2}^{1/2}$ ] were also observed (not shown).
- 2. Negative activation energies were obtained for temperatures less than ~300K (activation energies should be positive).

3. Extracted barrier heights ( $\phi_B$ ) that significantly differ from the reported band offsets with Si.

To summarize the findings in Chapters 6 and 7, two of the most commonly reported temperature dependent conduction mechanisms for  $HfO<sub>2</sub>$ , P-F and thermionic emission, fail to explain the strong temperature dependence of the gate leakage current for the devices used in this study. It is important to note that both P-F and thermionic emission studies reported in the literature in regards to  $HfO<sub>2</sub> MOS$  devices used temperatures greater than what was used in this study. While for greater temperature ranges, P-F and thermionic emission may explain the temperature dependence of the gate leakage current, they do not explain the temperature dependence for temperatures ranging from 6K to 400K in these devices leaving other possible mechanisms to be explored.

### CHAPTER 8: HOPPING CONDUCTION ANALYSIS

In the analysis of the temperature dependence of the gate leakage current in 3nm  $HfO_2/1.1$ nm Si $O_2$  and 5nm  $HfO_2/1.1$ nm Si $O_2$  n/pMOSFETs, the data has been compared with several models. Two of the most popular models for the temperature dependence of the gate leakage current in  $HfO<sub>2</sub> MOS$  devices, P-F (Chapter 6) and Schottky (Chapter 7), fail to explain the temperature dependence of the gate leakage current of the devices in this study over the temperature range 6K to 400K. Notable problems with P-F model were 1) a range of defect levels extracted between 3nm and 5nm HfO<sub>2</sub> samples yielding a thickness dependence for which the P-F model does not incorporate, 2) the extracted defect energy level is highly sensitive to the chosen temperature range, and 3) the inability of the P-F model to explain the transport mechanism trend for gate voltages less than  $\sim$ 1V (i.e., device operation voltage range) in 3nm HfO<sub>2</sub> samples. Schottky conduction also fails to explain the strong temperature dependence of devices studied for the temperature range of 6K to 400K. Notable problems with Schottky emission were 1) Schottky emission is thickness independent while a thickness dependence for the extracted barrier heights was found between 3nm and 5nm  $HfO<sub>2</sub>$  devices, 2) the extracted barrier heights differed significantly from the band offsets of  $SiO<sub>2</sub>$  or HfO<sub>2</sub> with Si, and 3) negative activation energies were found for temperature less than ~300K, leaving a wide temperature range where the trend of the gate leakage current with temperature cannot be explained. Analysis of one-dimensional quantum mechanical transmission coefficient calculations for electron substrate injection (positive gate biases), described in

Appendix C, show nearly the same transmission coefficient for the equivalent distance of Fowler-Nordheim tunneling into the HfO<sub>2</sub> conduction band for the 3nm and 5nm HfO<sub>2</sub> gate stacks. The gate leakage current of 3nm and 5nm  $HfO<sub>2</sub>$  devices at equivalent tunneling distances show orders of magnitude difference, indicating that quantum mechanical tunneling from the Si to  $HfO<sub>2</sub>$  conduction band is not responsible for the temperature dependence of the gate leakage current.

In short summary, the following is concluded about the conduction path of the carriers as they move from the Si substrate to the TiN gate given the analysis shown thus far.

- 1. Carriers are not emitted from a single defect level in  $HfO<sub>2</sub>$  to the  $HfO<sub>2</sub>$ conduction band (for electron substrate injection) or the valance band (for hole substrate injection), (P-F analysis).
- 2. The dominate transport mechanism is not due to carriers going over the barrier (Schottky analysis).
- 3. The dominate transport mechanism is not due to quantum mechanical tunneling from the Si to  $HfO<sub>2</sub>$  conduction band (transmission coefficient analysis, Appendix C).

Due to points 2 and 3, defect mediated transport is suggested as the dominate transport mechanism over the temperature range investigated, 6K to 400K. Point 1 may suggest many defect levels exist in the  $HfO<sub>2</sub>$  layer, which would be consistent with the polycrystalline/amorphous nature of the  $HfO<sub>2</sub>$ . The thickness dependence of the gate leakage current could be due to a longer percolation path in  $5<sub>nm</sub>$  HfO<sub>2</sub> devices compared to the  $3$ nm HfO<sub>2</sub> devices for defect mediated transport. The literature also suggests a strong

defect presence in  $HfO<sub>2</sub>$  based dielectric stacks (e.g., [105, 106]). Oxygen vacancies in the  $HfO<sub>2</sub>$  have been suggested as the origin of traps as well as impurity metals and polaronic traps (e.g., [28, 29, 107]).

In the semiconductor device community, trap assisted tunneling via electrically active deep level point defects have been used to describe leakage currents in thin MOS dielectrics (e.g., [108, 109]). However, another approach to defect mediated transport is known as hopping conduction (see Section [2.2\)](#page-25-0). Hopping transport has been used extensively in disordered systems to explain the temperature dependence of the conductivity (e.g., [45, 110-113]). This chapter explores the application of hopping conduction models to the temperature dependence of the gate leakage current of HfO2/SiO2 bilayer dielectric stacks.

# **8.1: Analysis of Hopping Conduction**

Hopping conduction was described in Section [2.2](#page-25-0) and for three-dimensional variable range hopping predicts a  $T^{1/4}$  dependence in the conductivity for a constant density of states with respect to energy around the Fermi level. For the two-dimensional case applicable to the thin dielectrics investigated in this study, a  $T^{1/3}$  dependence in the conductivity is predicted and the density of states around the Fermi level,  $N(E_F)$  is given by [see  $(2.5)$ ] [114]:

$$
N(E_F) = C_2^3 \frac{\alpha^2}{k_b t(T_0)}
$$
\n(8.1)

where  $C_2$  is a constant (derived to be approximately 2). The pre-exponential constant  $\sigma_{\text{hon}}$ in [\(2.4\)](#page-27-0) has also been derived in the literature and depends on various material parameters (e.g., defect density, velocity of sound in the medium, deformation potential) [115, 116]. Traditional analysis of variable hopping conduction is performed by linearizing [\(2.4\)](#page-27-0) as:

<span id="page-133-0"></span>
$$
\ln(\sigma) = -T_0 T^{-\frac{1}{d+1}} + \ln(\sigma_{hop}), \qquad (8.2)
$$

which indicates that a plot of  $\ln(\sigma)$  versus  $T^{1/d+1}$  for data that exhibit variable range hopping should result in a straight line. The conductivity through the gate stack of the devices in this study are not linear when plotted as suggested by [\(8.2\)](#page-133-0) with *d* equal to three or two, indicating that variable range hopping conduction cannot describe the temperature dependence of the conductivity by itself.

Arrhenius analysis performed in Section [5.3](#page-83-0) indicates a weak temperature sensitive regime (6K-50K), a strong temperature regime (near 400K), and a very wide temperature transition regime between the two. An Arrhenius plot of the gate leakage current density at various gate voltages above  $V_{th}$  in the transport limited regime  $(0.85V)$ to 2V) is shown in [Figure 8.1,](#page-135-0) illustrating the three general temperature regimes identified above. [Figure 8.1](#page-135-0) shows the wide temperature transition regime (labeled "Region 1") and the strong temperature sensitive regime (labeled "Region 2"). The inset in [Figure 8.1](#page-135-0) shows the weak temperature sensitive regime (labeled "Region 3").

Following the three general temperature regimes observed in the Arrhenius plot (Regions 1-3), a model for the conductivity through the  $HfO<sub>2</sub>$  (which assumes the presence of the  $SiO<sub>2</sub>$  IL in the HfO<sub>2</sub>/SiO<sub>2</sub> bilayer is a non-limiting function of the conductivity of the HfO<sub>2</sub> layer or the HfO<sub>2</sub>/SiO<sub>2</sub> stack for that matter) for the full temperature regime measured (6K-400K) is proposed:

<span id="page-134-0"></span>
$$
\sigma_{HfO_2} = \sigma_{hop} e^{-\left(\frac{T_0}{T}\right)^{1/3}} + \sigma_{Arr} e^{-\frac{E_1}{k_b \cdot T}} + \sigma_0
$$
\n(8.3)

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The first conductivity term represents two-dimensional variable range hopping to describe Region 1, the second conductivity term represents an Arrhenius mechanism with activation energy  $E_1$  to model Region 2, and the last conductivity term represents temperature independent conduction mechanisms (e.g. direct/FN tunneling, temperature independent hopping due to high electric fields) to model Region 3. The addition of the three conduction mechanisms as shown in [\(8.3\)](#page-134-0) implies parallel conduction, where it is assumed that the conduction path of one mechanism does not significantly affect the conduction path of another, or at least if it does, does so when the affected mechanism is not the dominate conduction mechanism. The parallel conduction mechanism approach has been used in the literature in conjunction with describing temperature dependent conductivity that exhibit multiple mechanisms (e.g., [43, 45, 117]).



<span id="page-135-0"></span>Figure 8.1: Representative Arrhenius plot of the gate leakage current density for gate voltages ranging from  $0.85V$  to 2V of a 5nm HfO<sub>2</sub> nMOSFET. A wide nonlinear region is shown from 50K to 400K. The inset shows a very weak temperature region for *T* < 50K.

Equation [\(8.3\)](#page-134-0) cannot be linearized with respect to temperature, hence nonlinear curve fitting is used to determine if (9.3) describes the temperature dependence of the gate leakage current from the perspective of conductivity through the  $HfO<sub>2</sub>$ , which is assumed to be the material limiting current flow. The conductivity through the  $HfO<sub>2</sub>$  layer at various gate voltages is calculated using  $\sigma_{HfO2} = J_{Gate}/E_{ox,HfO2}$ . Nonlinear curve fitting is performed by adjusting the fitting parameters until the error between the model and data reach a local minimum. The method used in this study to calculate the error between the model and data is Chi-Squared, which is:

<span id="page-135-1"></span>
$$
\chi^{2} = \sum w_{i} (y_{i} - f(x_{i}))^{2}, \qquad (8.4)
$$

where  $y_i$  and  $x_i$  is the *i*-th data point,  $f(x_i)$  is the model evaluated at  $x_i$ , and  $w_i$  is the weighting. Without weighting, the reduction of Chi-Squared is biased toward larger

values of *yi*, where the difference between the model and data has a larger impact on Chi-Squared. A weighting function of  $w_i = 1/y_i^2$  creates a relative distance error where all points are equally weighted regardless of their value. The weighting function  $w_i = 1/y_i$  is used for performing the nonlinear curve fits in this study as a compromise between the actual error and relative error between the model and data [118].

In order for nonlinear curve fitting to be effective, the initial estimation of the parameters (i.e., guess or initialization parameters) must be similar enough to the best fit parameters that when the nonlinear curve tool performs its error minimization techniques the local global minimum (the best fit) results rather than a local non-global minimum. The initial guess parameters were determined by performing two nonlinear fits to two different temperature ranges of the data. The low temperature regime  $(T < 200)$  was fit to:

<span id="page-136-0"></span>
$$
\sigma_{HfO_2,low-temp} = \sigma_{hop} e^{-\left(\frac{T_0}{T}\right)^{1/3}} + \sigma_0 \tag{8.5}
$$

and the high temperature regime  $(T > 200)$  was fit to:

<span id="page-136-1"></span>
$$
\sigma_{HfO_2, high-temp} = \sigma_{Arr} e^{-\frac{E_1}{k_b \cdot T}} + \sigma_0.
$$
\n(8.6)

where  $\sigma_0$  was initialized to the minimum conductivity of the temperature range (6K). The fitting results of [\(8.5\)](#page-136-0) and [\(8.6\)](#page-136-1) were then used as the initialization parameters for performing the nonlinear curve fit using [\(8.4\)](#page-135-1).

#### **8.2: Electron Substrate Injection Results and Discussion**

Fitting the HfO<sub>2</sub> conductivity data using  $(8.3)$  and device level shared fit parameters<sup>[17](#page-137-0)</sup>  $T_0$  and  $E_1$  results in an adjusted R-squared value greater than 0.999. Using ([8.3](#page-134-0)) to model the data. An example of the correlation between the experimental data singular  $T_0$  and  $E_1$  parameters to describe the temperature dependence of the conductivity across multiple gate voltages with high accuracy highlights the effectiveness in using (symbols) and the fitted model (lines) is shown in [Figure 8.2](#page-139-0) (3nm  $HfO<sub>2</sub>$ ) and [Figure 8.3](#page-140-0) (5nm  $HfO<sub>2</sub>$ ). As observed in [Figure 8.2](#page-139-0) and [Figure 8.3,](#page-140-0) the model in [\(8.3\)](#page-134-0) describes the temperature dependence of the gate leakage current for the entire temperature range studied (6K to 400K). For pMOSFETs where the device is in accumulation, fitting was performed for temperatures above 40K where carrier-limited transport is not occurring. The model describes the large non-linear region  $(\sim 50K)$  to  $\sim 400K$ ) on the Arrhenius plot that was discussed in Section [5.3.](#page-83-0)

For the 3nm HfO<sub>2</sub> samples, the  $T_0$  parameter was extracted providing a value  $\sim$ 3x10<sup>5</sup>K.<sup>[18](#page-137-1)</sup> Assuming a decay length ( $\alpha$ <sup>-1</sup>) of 1nm<sup>[19](#page-137-2)</sup> results in a density of states around the Fermi level in the HfO<sub>2</sub>,  $N(E_F)$ , of  $\sim 1 \times 10^{20}$  (cm<sup>-3</sup>eV<sup>-1</sup>) using (2). The extracted defect density is similar to those reported by Xiong *et al*. for HfO<sub>2</sub> also manufactured by SEMATECH, which ranged from  $\sim 10^{19}$  to  $\sim 10^{21}$  cm<sup>-3</sup>eV<sup>-1</sup> [121]. The average spacing

<span id="page-137-0"></span><sup>&</sup>lt;sup>17</sup> "Shared fit parameters" refers to the same parameter value used to fit across multiple data sets. In the context of this study, singular  $T_0$  and  $E_1$  values are used to fit data over multiple conductivities extracted at various gate voltages. Single values for  $T_0$  and  $E_1$  are only enforced on the conductivities of the device being fitted and not across multiple devices. Hence "device level" (the level at which the parameters are shared) is used to describe the fitting procedure used.

<span id="page-137-1"></span><sup>&</sup>lt;sup>18</sup> As a reference, the characteristic temperature parameter,  $T_0$ , for many materials can be quite large. For example, TiO<sub>2</sub> – 2x10<sup>7</sup>K [119], Cu-vermiculite intercalation – ~1x10<sup>5</sup> to ~1x10<sup>6</sup> [46], Ge – ~1x10<sup>8</sup>K [120], and  $\overline{Si}$  – ~1x10<sup>8</sup>K [120].

<span id="page-137-2"></span><sup>&</sup>lt;sup>19</sup> As a reference, the defect decay length in Ge is  $\sim$ 1nm [114]. As will be shown later the assumed value here of 1nm is close to an extracted value using electric field dependent hopping, ~0.83nm.

between defects is then  $N^{1/3} \approx 2$ nm, if one considers defects spread over 1eV. Calculating the average spacing between defects assuming an energy spread of 1eV is not unreasonable as a large distribution in energy can exist for defects in  $HfO<sub>2</sub>$  indicated by theoretical calculations of oxygen vacancies [98]. For the 5nm  $HfO<sub>2</sub>$  samples,  $T<sub>0</sub>$  was extracted to ~8x10<sup>5</sup>K resulting in  $N(E_F)$  of ~2x10<sup>19</sup> (cm<sup>-3</sup>eV<sup>-1</sup>) and an average defect spacing of 3.7nm considering defects spread over 1eV. A significant difference in the defect density is observed between the 3nm and 5nm  $HfO<sub>2</sub>$  samples. This may be due to a large concentration of defects in the  $SiO<sub>2</sub>$  at the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  interface, which are averaged lower in the 5nm  $HfO<sub>2</sub>$  compared to the 3nm  $HfO<sub>2</sub>$  samples due to its greater thickness; the variable range hopping model used assumes a constant defect density about the Fermi level [46, 115]. A significant concentration of defects in the  $SiO<sub>2</sub>$  layer was suggested in Section [5.1.2.](#page-74-0)



<span id="page-139-0"></span>Figure 8.2: Arrhenius plot of experimental conductivity data (symbols) for gate voltages ranging from 0.75V to 2V of a 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> nMOSFET. Fit of variable range hopping and Arrhenius model described by [\(8.3\)](#page-134-0) is also shown (lines). Model describes the nonlinear region (50K to 400K) very well in addition to the entire temperature region studied (*T* < 50K), not shown. Only gate voltages in 0.25V increments are shown for clarity.



<span id="page-140-0"></span>Figure 8.3: Arrhenius plot of experimental conductivity data (symbols) for gate voltages ranging from 1V to 2V for a 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> nMOSFET. Fit of variable range hopping and Arrhenius model described by [\(8.3\)](#page-134-0) is also shown (lines). Model describes the nonlinear region (50K to 400K) very well in addition to the entire temperature region studied (inset). Only gate voltages in 0.25V increments are shown for clarity.

Fitting results for the Arrhenius expression provides an activation energy of  $\sim$ 0.19eV for the 3nm HfO<sub>2</sub> samples and  $\sim$ 0.42eV for the 5nm HfO<sub>2</sub> samples. If  $E_1$  is allowed to vary for each gate voltage, the activation energy does not decrease as the gate voltage increases as predicted by the Poole-Frenkel conduction mechanism. There are many transport mechanisms that are represented by Arrhenius expressions. Below is a list of various kinetic processes that are described by an Arrhenius expression [45].

1. Thermal stimulation of from carriers from the defect energy level to the conduction band. The activation energy is the energy difference between the Fermi energy level and the conduction band.

- 2. Thermal stimulation of carriers from one defect state to another defect state where the activation energy is the difference between the two defect energy levels.
- 3. Hopping conduction within a finite energy band (energy bandwidth limited) where the activation energy corresponds to order of half the width of the energy band of defect states. The hopping energy may include a lattice deformation energy associated with the presence of the charged carrier (i.e., defect mediated polaron hopping).
- 4. Nearest neighbor hopping conduction where the activation energy is on the order of the energy band width of the defect states.

The activation energy can also be the sum of multiple processes, such as a hopping energy term and a polaron energy term [45]. As was discussed in the introduction, due to the high dielectric constant of  $\text{HfO}_2$ , polaron motion may have an effect on the transport mechanism.

Theoretical predictions of activation energies in monoclinic  $HfO<sub>2</sub>$  near the extracted activation energies reported here are: electron self-trapped polaron energy (0.32eV below conduction band) [29], electron polaron hopping transport energy (0.05eV) [29], thermal activation energy of an electron from the oxygen vacancy  $V^2$ charge trap state (0.56eV) [28], and the energy difference of the oxygen vacancy  $V^{-1}$  and  $V^2$  charge states (0.2eV) [28].

For the 3nm HfO<sub>2</sub> samples, the extracted activation energy of  $\sim 0.19 \text{eV}$  is close to the energy difference between the oxygen vacancy  $V^{-1}$  and  $V^{-2}$  charge states (0.2eV). The similar energy levels suggest electron transport at large temperatures occurs by electron

hopping between these two charge states. For the  $5$ nm  $HfO<sub>2</sub>$  samples, the extracted activation energy of ~0.42eV is similar to the electron self-trapped polaron energy (0.32eV) and the energy difference between the oxygen vacancy  $V^2$  charge trap state and the  $HfO<sub>2</sub>$  conduction band (0.56eV). Additional studies are needed to determine the relationship between the Arrhenius activation energy and  $HfO<sub>2</sub>$  thickness and what mechanisms they model.

## **8.3: Hole Substrate Injection Results and Discussion**

The HfO<sub>2</sub> conductivity data for the entire temperature range at negative gate voltages can also be described by  $(8.3)$  using device level shared fit parameters  $T_0$  and  $E_1$ . Fitting the model to the data results in an adjusted *R*-squared value greater than 0.999. [Figure 8.4](#page-143-0) (3nm HfO<sub>2</sub>) and [Figure 8.5](#page-145-0) (5nm HfO<sub>2</sub>) are examples of the correlation between the experimental data (symbols) and the fitted model (lines). As observed in pMOSFETs, [Figure 8.5,](#page-145-0) the model in [\(8.3\)](#page-134-0) describes the temperature dependence of the gate leakage current for the entire temperature range studied (6K to 400K). For nMOSFETs [\(Figure 8.4\)](#page-143-0), where at negative gate biases the device is in accumulation, fits were only performed for temperatures above 40K so that the gate leakage current modeled is dominated by transport-limited conduction (see Section [5.3\)](#page-83-0). For both n- and pMOSFETs, the model describes the large nonlinear region (~50K to ~400K) on the Arrhenius plot that was discussed in Section [5.3.](#page-83-0)

The extracted characteristic temperature,  $T_0$ , for 3nm HfO<sub>2</sub> samples is ~1.7x10<sup>4</sup>K, which, assuming a localized defect decay length of  $1 \text{nm} (\alpha^{-1})$  as was done for positive gate biases, results in a defect density about the Fermi level of  $\sim 1.5 \times 10^{21}$ cm<sup>-3</sup>eV<sup>-1</sup>. For the

5nm HfO<sub>2</sub> samples,  $T_0$  is ~4.3x10<sup>4</sup>K, which, again assuming  $\alpha^{-1}$ =1nm, results in a defect density about the Fermi level of  $\sim 3.9 \times 10^{20}$ cm<sup>-3</sup>eV<sup>-1</sup>. The extracted defect density for hole variable range hopping transport is about an order of magnitude above the defect density extracted for electrons in the previous section. The large defect densities for electrons and holes suggests that there is room for significant improvement in  $HfO<sub>2</sub>$  layer, which would reduce the temperature dependence of the gate leakage current.



<span id="page-143-0"></span>Figure 8.4: Arrhenius plot of experimental conductivity data (symbols) for gate voltages ranging from -0.75V to -2V of a 3nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> nMOSFET. Fit of variable range hopping and Arrhenius model described by [\(8.3\)](#page-134-0) is also shown (lines). The model describes the nonlinear region (50K to 400K) very well. Temperatures below 40K were not used during the fit due to carrier rate limited conduction in accumulation (see Section [5.3\)](#page-83-0).Only gate voltages in 0.25V increments are shown for clarity.

The extracted activation energy for the Arrhenius term in  $(8.3)$  is  $\sim 0.19$ eV for the 3nm HfO<sub>2</sub> samples and  $\sim 0.32$ eV for the 5nm HfO<sub>2</sub> samples. Theorized activation energies for holes include: polaron self-trap energy (0.57 and 0.14eV) [29], polaron hopping transport energy (0.08, 0.16, 0.19, and 0.56eV) [29], and the energy difference of the oxygen  $V^+$  and  $V^0$  states (0.01eV) [28]. The injection location of the carriers (near
the Si Fermi level) into the HfO<sub>2</sub> layer is near the middle of the HfO<sub>2</sub> band gap signifying that the Arrhenius expression does not correspond to carrier thermal transitions from defects near the middle of the HfO<sub>2</sub> band gap,  $[V^+ - E_C (3.39 \text{eV})$  and  $V^0 - E_C (3.19 \text{eV})$ oxygen vacancy charge states] to the  $HfO<sub>2</sub>$  band edge as the energy difference between the defect levels and  $HfO<sub>2</sub>$  valance band is too large compared to the extracted activation energy. The Arrhenius expression also is not likely to correspond to polaron hopping of holes in the  $HfO<sub>2</sub>$  valance band, as the energy difference between the Si Fermi energy level and self-trapped hole in the  $HfO<sub>2</sub>$  valance band is ~2.7 eV, which is significantly larger than the extracted activation energy. The Arrhenius expression might represent nearest neighbor hopping conduction or energy bandwidth limited conduction where the activation energy is proportional to the width of the defect energy band. Possible defects for which nearest neighbor hopping conduction could occur is the  $V^+$  and  $V^0$  oxygen vacancy charge states. For disordered layers or high defect densities, the distribution of energy levels for defects would be more broadly distributed than the mono-energetic levels calculated using monoclinic HfO<sub>2</sub>. Additional studies are necessary to further determine the mechanism that the Arrhenius term represents.



Figure 8.5: Arrhenius plot of experimental conductivity data (symbols) for negative gate voltages ranging from -1.25V to -2V for a 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> pMOSFET. Fit of variable range hopping and Arrhenius model described by [\(8.3\)](#page-134-0) is also shown (lines). The model describes the nonlinear region (50K to 400K) very well as well as the entire temperature region studied (inset). Only gate voltages in 0.25V increments are shown for clarity.

#### **8.4: Electric Field Dependent Variable Range Hopping**

<span id="page-145-0"></span>While the parameters  $T_0$  and  $E_1$  were held constant over the various gate voltages investigated, parameters  $\sigma_{hop}$ ,  $\sigma_{Arr}$ , and  $\sigma_0$  were allowed to vary with gate voltage. Figure [8.6](#page-146-0) gives an example of how  $\sigma_{hop}$ ,  $\sigma_{Arr}$ , and  $\sigma_0$  vary with  $V_{Gate}$ . As observed in [Figure 8.6,](#page-146-0) the parameters  $\sigma_{hop}$  and  $\sigma_{Arr}$  span several orders of magnitude as  $V_{Gate}$  increases to 2V showing a strong *VGate* dependence. However, the variable range hopping model, [\(2.4\)](#page-27-0), was derived for low electric fields and does not predict a  $V_{Gate}$  dependence [122].



<span id="page-146-0"></span>Figure 8.6: Example of the large change in the  $\sigma_{hop}$ ,  $\sigma_{Arr}$ , and  $\sigma_0$  fitting parameters with respect to  $V_{Gate}$ . While  $\sigma_0$  is expected to change with  $V_{Gate}$ ,  $\sigma_{hop}$  and  $\sigma_{Arr}$  are not expected to have such a strong dependence on *VGate*.

As was discussed in Section [2.2,](#page-25-0) at high electric fields hopping can occur without thermal assistance. Analogous to variable range hopping in three-dimensions, which has a temperature dependence of  $T^{1/4}$  for a constant density of state, electric field dependent variable range hopping has a dependence of  $E_{ox}$ <sup>-1/4</sup> as shown in [\(2.9\)](#page-30-0). For twodimensional variable range hopping the electric field dependence becomes  $E_{ox}$ <sup>-1/3</sup> similar to temperature dependent variable range hopping in two dimensions. The conductivity through the HfO<sub>2</sub> versus  $E_{ox}$ <sup>-1/3</sup> at positive gate biases is shown in [Figure 8.7](#page-147-0) for 6K, where temperature dependent hopping is minimized. The data in [Figure 8.7](#page-147-0) is linear over almost the entire electric field range above the threshold voltage where conduction pathlimited transport occurs. A linear fit to the data (red line in [Figure 8.7\)](#page-147-0) demonstrates the linearity of the data when the log of the conductivity is plotted versus  $E_{ox,HfO2}$ <sup>-1/3</sup> and

indicates that non-thermally activated hopping due to the presence of high electric fields has an important role in the temperature dependence of the gate leakage current.



<span id="page-147-0"></span>Figure 8.7: Two-dimensional electric field dependent hopping plot of 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  nMOSFET. The conductivity through the HfO<sub>2</sub> at 6K indicates that electric field dependent hopping participates in the gate leakage current. An adjusted R-Squared value greater than 0.99 exists between the data and the linear fit.

Models have been developed for hopping conduction in high electric fields [123,

124]. A model for two-dimensional variable hopping conductivity in an electric field can

<span id="page-147-1"></span>be written as [124]:

$$
\sigma = Ae^{-\left(\frac{2T_0}{T(P+Q)}\right)^{1/3}}
$$
\n(8.7)

where

$$
P = \frac{1 + f/2}{(1 + f)^2}, \qquad Q = \frac{3f}{2} + 1, \qquad f = \frac{E_{ox, HfO_2}q}{2\alpha k_b T},
$$

*q* is the charge of an electron, and *A* is a constant weakly dependent on the electric field and temperature [122]. The density of states at the Fermi energy level is given by [\(8.1\)](#page-132-0). The most probable hop distance is given by [124]:

$$
R_{hop} = \frac{1}{3\alpha} \left(\frac{T_0}{T}\right)^{1/3} \tag{8.8}
$$

<span id="page-148-1"></span>To verify if this model explains the gate voltage dependence of the variable range hopping, the three conductivity terms of [\(8.3\)](#page-134-0) are plotted in [Figure 8.8](#page-148-0) to determine where each term dominates.



<span id="page-148-0"></span>Figure 8.8: Temperature dependence of the conductivity through the  $HfO<sub>2</sub>$  for various gate voltages. Experimental data is shown by symbols while the model is shown in lines. The three terms of the model are also plotted separately demonstrating where each component dominates. Only gate voltages in 0.25V increments shown for clarity.

From [Figure 8.8,](#page-148-0) the temperature independent conductivity term  $(\sigma_0)$  dominates

for *T* < 120K. In [Figure 8.8,](#page-148-0) the Arrhenius conductivity term appears to dominate at temperatures near and above 400K, which is the highest temperature measured. Higher temperature measurements are required to determine if the Arrhenius conductivity term

correctly models the high temperature region  $(T > 380K)$ . The variable range hopping conductivity term dominates for temperatures around 240K.

To determine if high electric field variable range hopping models describe the variable range hopping dominated temperature range, [\(8.7\)](#page-147-1) was used to fit the data over a temperature range of 200K-260K as a function of temperature and electric field. It is expected that as temperature increases, the density of states about the Fermi energy level in the  $HfO<sub>2</sub>$  and the decay length of the localized wave function of the defects do not change with temperature. Therefore, the fitting parameters of  $A$ ,  $\alpha$ , and  $T_0$  should be the same for each temperature investigated. [Figure 8.9](#page-150-0) shows an example of the best fit obtained for shared parameters (i.e.,  $A$ ,  $\alpha$ , and  $T_0$ ) for each temperature while the inset illustrates the best fits for non-shared parameters (i.e., parameters allowed to vary for each temperature). As observed in [Figure 8.9](#page-150-0) (not the inset), [\(8.7\)](#page-147-1) does not describe the complete electric field range investigated (corresponding to  $V_{Gate} = 0.85V$  to 2V). The electric field dependent variable range hopping expression correctly models the high field regime but fails to describe the relatively low electric field regime.



<span id="page-150-0"></span>Figure 8.9: Example of conductivity through the  $HfO<sub>2</sub>$  as a function of electric field in the  $HfO<sub>2</sub> 200K-260K$ . Best fit simulations using [\(8.7\)](#page-147-1) are shown by lines while experimental results are shown by symbols. Only every fifth experimental data point is shown for clarity. The main plot shows best fit results if shared parameters are considered over the temperature range shown while the inset shows bet fit results for parameters not shared across temperatures.

Extracted parameters for the 3nm HfO<sub>2</sub> samples results in  $T_0 = -5x10^6$ K and  $\alpha =$  $\sim$ 1.2x10<sup>7</sup>cm<sup>-1</sup> (recall 1x10<sup>7</sup>cm<sup>-1</sup> was assumed earlier), which using [\(8.1\)](#page-132-0) and [\(8.8\)](#page-148-1) corresponds to a defect density of  $\sim 7 \times 10^{18}$ cm<sup>-3</sup>eV<sup>-1</sup> and hopping distance of  $\sim 7$ nm. The extracted hopping distance is larger than the physical distance of the dielectric stack (4.1nm in total). Average variable range hopping distances up to six times larger than the thickness of the material in two-dimensional hopping has also been observed in amorphous Si and germanium (Ge) [45]. Although in the presence of an electric field hopping is more likely to occur in the direction of the electric field, hopping is not restricted to be directionally normal to the gate stack plane. Hence, hops greater than the thickness of the dielectric are therefore expected, leading to average variable range hopping distances greater than the thickness of the material. The ratio of the hopping

distance with respect to the material thickness further suggests two-dimensional hopping is present. A rough estimate between two-dimensional and three-dimensional hopping occurs when the material thickness is three to four times larger than the hopping distance [45].

Extracted parameters for the 5nm HfO<sub>2</sub> samples results in a  $T_0 = \sim 1 \times 10^7$ K and  $\alpha =$ ~2.2x10<sup>7</sup>cm<sup>-1</sup>, which results after using [\(8.1\)](#page-132-0) and [\(8.8\)](#page-148-1) in  $N(E_F) = \sim 9 \times 10^{18} \text{cm}^{-3} \text{eV}^{-1}$  and  $R_{hop} = -5$ nm. Notice that the extracted hopping distance is nearly the same as the HfO<sub>2</sub> thickness and just shy of the dielectric stack thickness (6.1nm). This indicates a one or two hop transport through the dielectric stack. Using [\(8.7\)](#page-147-1) to model the gate leakage resulted in a larger  $T_0$  and smaller defect density compared to using  $(8.3)$  for both the 3nm and 5nm  $HfO<sub>2</sub>$  stacks.

From [Figure 8.9,](#page-150-0) the best fit achieved for shared parameters between temperatures results in poor fits for the lower  $E_{ox, HfO<sub>2</sub>}$  values, which indicates the electric field dependent variable hopping model for the 5nm and 3nm samples is limited. The inset in [Figure 8.9](#page-150-0) shows excellent fits over the entire strong inversion regime investigated but was achieved by considering independent  $T_0$ ,  $\alpha$ , and  $A$  terms for each temperature, implying different defect density and defect localization lengths based on temperature, which is unlikely. So while  $(8.7)$  can correctly model a particular temperature, it fails when considering multiple temperatures. Fits performed of  $\sigma_{HfO2}$  versus *T* show that adding Arrhenius or  $\sigma_0$  conduction terms to [\(8.7\)](#page-147-1) provides little benefit in improving fits when holding  $\alpha$  constant over various temperature and  $E_{ox,HfO2}$  ranges.

In this chapter, application of two-dimensional variable range hopping models were applied to  $\text{MOS }\text{HfO}_2/\text{SiO}_2$  bilayer gate stacks to determine if they could explain

the temperature dependence of the gate leakage current over a wide temperature range  $(6K - 400K)$ . Using a three-conductivity term model that consists of 1) a temperature independent term, 2) variable range hopping term, and 3) Arrhenius term described by [\(8.3\)](#page-134-0), the temperature dependence of the gate leakage current can be well described from 6K-400K with an adjusted R-squared value greater than 0.999. For variable range hopping models to completely describe the temperature dependence of the gate leakage current, some issues need to be addressed.

- 1. The physical meaning of the Arrhenius expression in [\(8.3\)](#page-134-0) which results in an activation energy of  $\sim 0.19$ eV for 3nm HfO<sub>2</sub> samples and  $\sim 0.42$ eV for the 5nm  $HfO<sub>2</sub>$  samples. While at large gate biases the activation energy may correspond to thermal emission from defects near the Fermi energy level in the  $HfO<sub>2</sub>$  layer to the conduction band at high gate biases, for low positive gate biases and for negative gate biases it is presently unclear what the activation energy of the Arrhenius term might represent.
- 2. The gate voltage dependence of the fitting parameters  $\sigma_{hop}$  and  $\sigma_{Arr}$  span orders of magnitude for a gate bias range of  $\sim$ 1V to 2V. A link between the fitting parameters and the gate voltage is missing.
- 3. Using a hopping conduction model for high electric fields in an attempt to explain the variation of the pre-exponential factor with gate voltage falls short of describing the gate leakage current over many temperatures yielding defect densities and decay lengths that vary with temperature.

Despite these limitations, the model successfully describes the temperature dependence of the gate leakage current over a very broad temperature range for both positive and negative gate biases.

#### CHAPTER 9: SUMMARY AND FUTURE WORK

As new dielectrics, including multilayer dielectrics, continue to be introduced into semiconductor devices, an increased understanding of the materials performance and limitations is necessary. With respect to reliability and power consumption, understanding the charge carrier transport through the dielectric is of particular interest. Of immediate concern to the semiconductor community is the material of  $HfO<sub>2</sub>$ , which is quickly being integrated into the production line. In this study, the gate leakage current of  $TiN/HfO<sub>2</sub>/SiO<sub>2</sub>/Si$  n/pMOSFETs devices were measured over a temperature range of 6K to 400K using finely spaced temperature steps. The large temperature range over which the devices were measured give an accurate description of the gate leakage current with respect to temperature for which analysis can be performed to determine the carrier transport mechanism. In the next two sections, a brief summary of the important observations and analysis are presented followed by some suggestions for future work.

### **9.1: Summary**

Multilayer dielectrics increase the complexity of carrier transport through the dielectric stack requiring new tools to aid in their understanding. An energy band simulation tool was developed to assist in visualizing complex MOS systems and perform analysis. The simulation tool allows an arbitrary number of dielectrics to be placed in the MOS gate stack and calculates the energy band, electric field, charge distribution, and potential diagrams. Additional analyses include flatband voltage, threshold voltage,

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capacitance, tunneling distance, trap charge effects, transmission coefficient, and image charge effects. Versions of the program are available to the public free of charge [94] providing a simulation tool that is a valuable resource to the semiconductor community.

General observations of the temperature dependence of the gate leakage current in  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate stacks included:

- 1. The temperature dependence of the 3 and 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  bilayer stacks is significantly greater than the  $2nm$  SiO<sub>2</sub> control stack (Section [5.1\)](#page-66-0).
- 2. Carrier transport is dominated by a carrier limited regime in the depletion/weak inversion regime and a transport path-limited regime in the strong inversion and accumulation regimes (Section [5.1.1\)](#page-66-1).
- 3. Carrier separation analysis of the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate stacks indicates that at positive gate biases the gate leakage current is due to substrate electrons moving to the metal electrode and at negative gate biases substrate holes moving to the metal electrode (Section [5.2\)](#page-79-0).
- 4. Arrhenius plots of the gate leakage current indicate multiple transport mechanisms are present. A weak temperature dependent regime is identified (*T* < 50K) that is nearly temperature insensitive and requires measurements at temperatures lower than 50K. Studies only performed to liquid nitrogen temperatures (77K) indicate an activation energy in the meV range for the weak temperature dependent regime (Section [5.3\)](#page-83-0).
- 5. For devices biased in accumulation, the gate leakage current decreases (especially noticeable in 3nm HfO<sub>2</sub> pMOSFETs) for  $T < 50K$  while devices biased in inversion do not. Capacitance-voltage measurements indicate the

reduction of the gate leakage current is due to freeze-out of majority carriers creating a carrier-limited transport regime (Section [5.3\)](#page-83-0).

- 6. For the strong temperature dependent regime, the Arrhenius slope never saturates (becomes linear) as the temperature increases over the temperature regime investigated. The extracted activation energy is therefore very dependent over the temperature regime from which it is extracted (Section [5.3\)](#page-83-0).
- 7. The activation energy in the strong temperature dependent regime is dependent on the gate voltage (Section [5.3\)](#page-83-0).

Common mechanisms used to explain the temperature dependence of the gate leakage current are P-F conduction and Schottky emission. The gate voltage dependence (i.e., an electric field dependence) of observation 7 listed above also suggests that P-F conduction or Schottky emission might apply to the temperature dependence of the gate leakage current in the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  stacks studied. P-F analysis and Schottky analysis, however, do not describe the temperature dependence of the gate leakage current for the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  bilayer stack studied here. Notable problems with the P-F conduction (Chapter 6) as applied to the bilayer stack are:

- 1. For the positive gate bias regimes, the P-F plot is nonlinear over a large electric field range for positive gate biases [\(Figure 6.2\)](#page-96-0).
- 2. The Arrhenius P-F plots are nonlinear [\(Figure 6.3](#page-98-0) and [Figure 6.7\)](#page-105-0) for which many different trap barrier heights can be extracted depending on the temperature range examined. The standard P-F model was developed for mono-energetic defect levels for which a linear Arrhenius P-F plot is

expected. The standard P-F model is therefore only able to describe a small temperature range.

- 3. Nonlinear  $\phi_r$ 's with respect to  $E_{ox,HfO2}^{1/2}$  were obtained for which different  $\phi_{PF}$ 's can be extracted depending on the choice of electric field range used to perform the linear extrapolation [\(Figure 6.5\)](#page-101-0). The small electric field range (which can then be approximated as linear) is evidence that the P-F conduction mechanism provides an inappropriate explanation to the gate leakage dependence.
- 4. Thicker 5nm  $HfO<sub>2</sub>$  samples resulted in larger extracted trap barrier heights than thin 3nm  $HfO<sub>2</sub>$  samples, resulting in a thickness dependence. The standard P-F model does not predict thickness dependence in the leakage current.
- 5. For 3nm HfO2 MOSFETs, P-F transport could not explain the transport mechanism trend for gate voltages less than 1V. As the device voltage operating point is in this regime, ~1V and less, the dominate leakage current mechanism is not explained by the standard P-F analysis.
- 6. For the negative gate bias regime, the extracted trap energy level is nonsensical, yielding a shallow defect energy which requires a large thermal emission of holes from the Si to populate the energy level. This would result in a defect filling-limited transport mechanism and not thermal emission from the defect (P-F) as the limiting mechanism.
- 7. For 5nm HfO<sub>2</sub> devices at large negative biases  $(|E_{ox,HfO2}|^{1/2}| > |-1000|$  (V/cm)<sup>1/2</sup>) and for 3nm HfO<sub>2</sub> devices at small negative biases ( $E_{ox,HfO2}$  < 700 (V/cm)<sup>1/2</sup>),

*ϕ<sup>r</sup> increases* as the magnitude of the electric field increases. According to the P-F model, *ϕ<sup>r</sup>* should *decrease* as the magnitude of the electric field increases not *increase*.

In addition to examining Schottky emission, an expression for thermionic stimulated tunneling (TAT) current was developed for bilayers where the interfacial layer is sufficiently thin that thermionic stimulation is the limiting conduction mechanism. Notable problems with Schottky and TAT emission as an explanation to the temperature dependence of the gate leakage current in this study are (Chapter 7):

- 1. Nonlinear (i.e., non-Arrhenius) behavior of the characteristic plot of  $\ln(J_{Gate}/T^2)$  versus  $E_{ox,SiO2}$ , which is predicted by TAT, [\(7.9\)](#page-120-0). Nonlinear behavior of the characteristic plots for Schottky emission  $[\ln(J_{\text{Gate}}/T^2)$  versus *Eox,SiO2* 1/2].
- 2. Negative activation energies for temperatures less than ~300K (should be positive).
- 3. Extracted barrier heights  $(\phi_B)$  that significantly differ from the reported band offsets with Si.

The last transport mechanism that was investigated as an explanation to the temperature dependence of the gate leakage current was hopping conduction (defect mediated transport). Hopping conduction has long been a popular mechanism to explain the temperature dependence of the conductivity in disordered systems within the physics community. Variable range hopping conduction could not describe the transport mechanism over the entire temperature regime. Using a three-term expression, [\(8.3\)](#page-134-0), composed of a temperature independent term, variable range hopping term, and an

Arrhenius term, the conductivity through both the 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  and 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  gate stacks can be described through the entire temperature regime investigated with a reduced *R*-squared value greater than 0.999. Below are some important observations from the fit parameters.

- 1. For 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> n/pMOSFETs at positive gate biases (substrate electron injection), a defect density of  $\sim 10^{20}$  cm<sup>-3</sup>eV<sup>-1</sup> about the Fermi energy level was extracted from  $T_0 \approx 3 \times 10^5 \text{K}$  and  $\alpha = 10^7 \text{ cm}^{-1}$ .
- 2. For 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> n/pMOSFETs at positive gate biases (substrate electron injection), a defect density of  $\sim 2x10^{19}$  cm<sup>-3</sup>eV<sup>-1</sup> about the Fermi energy level was extracted from  $T_0 \approx 8 \times 10^5 \text{K}$  and  $\alpha = 10^7 \text{ cm}^{-1}$ .
- 3. Activation energies of  $\sim 0.19$ eV for the 3nm HfO<sub>2</sub> samples and  $\sim 0.42$ eV for the  $5<sub>nm</sub>$  HfO<sub>2</sub> samples were extracted from the Arrhenius term for positive gate biases.
- 4. For negative gate biases (hole substrate injection) of  $3$ nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> n/pMOSFETs, a defect density of  $\sim 1.5 \times 10^{21}$  cm<sup>-3</sup>eV<sup>-1</sup> about the Fermi energy level was extracted.
- 5. For negative gate biases (hole substrate injection) of 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$ n/pMOSFETs, a defect density of  $\sim$ 3.9x10<sup>20</sup> cm<sup>-3</sup>eV<sup>-1</sup> about the Fermi energy level was extracted.
- 6. Activation energies of ~0.19eV for the 3nm  $HfO<sub>2</sub>$  samples and ~0.32eV for the 5nm  $HfO<sub>2</sub>$  samples were extracted using the conductivity at negative gate biases (substrate hole injection).

The defect densities extracted correspond well to other values reported in the literature for  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate stacks [121]. It is unclear what transport mechanism the activation energies of the Arrhenius term might represent as many different thermally activated mechanisms are expressed by an Arrhenius equation. Additional work is required to identify which Arrhenius mechanism is responsible for the behavior observed. The pre-exponential terms of the variable range hopping term and Arrhenius term have a very strong gate voltage dependence. A link between the pre-exponential terms and the gate voltage needs to be established. Application of high electric field variable range hopping models performed well when modeling a single temperature but failed when considering multiple temperatures. Despite the short comings of the hopping models in describing transport through the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  gate stack, they do describe the temperature dependence of the gate leakage stack very well. The excellent fit of the temperature dependence of the gate leakage current can be used to empirically model the phenomenon and promotes continued study of the application of hopping models to the temperature dependence of the gate leakage current in novel dielectric stacks.

A significant implication for substrate electron injection is suggested by examining the results of the average hopping distance extracted during hopping analysis (Section [8.4\)](#page-145-0) and the bulge observed and discussed in relation to [Figure 5.9](#page-74-0) (Section [5.1.2\)](#page-74-1). For the 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> devices, the extracted average hopping distance ( $\sim$ 7nm) is greater than the stack thickness (4.1nm), while for the 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> devices it is not. For the 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  devices an average hopping distance of ~5nm was extracted compared to a physical thickness of 6.1nm. In relation to [Figure 5.9,](#page-74-0) a bulge in the temperature dependence of the gate leakage current is observed in the 3nm

 $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> devices and not in the 5nm  $HfO<sub>2</sub>/1.1$ nm SiO<sub>2</sub> devices. The existence of a bulge in the 3nm  $HfO<sub>2</sub>$  and large hopping distance suggest that the transport mechanism in 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> devices is dominated by the SiO<sub>2</sub> layer, while for the 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  devices the transport mechanism is dominated by the  $HfO<sub>2</sub>$  layer. This observation is consistent with a study performed by Bersuker *et al*.'s [125] on TiN/3 or 4nm  $HfO_2/1.1$ nm Si $O_2/Si$  gate stacks (which are very similar to the TiN/3nm  $HfO_2/1.1$ nm  $SiO<sub>2</sub>/Si$  gate stacks used in this study), where defects above the Si conduction band edge in the  $SiO<sub>2</sub>$  IL were found responsible for increases in the stress induced leakage current. In describing a possible qualitative mechanism for the bulge observed in the temperature dependent leakage data of 3nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub> MOSFETs$ , the same layer ( $SiO<sub>2</sub>$ ) and energy location of the defects (above the Si conduction band edge) was suggested (see discussion below [Figure 5.9\)](#page-74-0). This correlation further suggests, that for substrate electron injection in 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> MOSFETs, carrier transport is dominated by the SiO<sub>2</sub> layer and for 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub> MOSFETs$ , carrier transport is dominated by the  $HfO<sub>2</sub>$  layer.

This study of carrier transport in  $HfO<sub>2</sub>/SiO<sub>2</sub> MOS$  dielectric stacks has many important applications to current and future MOS dielectric stacks for the following reasons.

- 1. In this study, a bilayer dielectric stack is investigated. Novel dielectrics in MOS devices usually require the presence of more than one dielectric.
- 2. The presence of multiple dielectrics requires special attention to understand possible carrier transport mechanisms and how to model them. The approach

to analyzing the conduction mechanism(s) in the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  bilayer dielectric stacks in this study can be used as a template for other dielectric stacks.

- 3. Software capable of calculating the energy band structure and extracting important parameters developed for this study can be used on dielectric stacks composed of an arbitrary number of dielectrics.
- 4. Analysis techniques used in this study can also be applied to other novel dielectrics in MOS devices.

In addition to contributing to the understanding the carrier transport through the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  dielectric stack, this dissertation can be used as a model to analyze dielectric stacks of more than one dielectric and demonstrates the advantages of using characterization techniques over a wide temperature range.

## **9.2: Future Work**

The work in this study provides a solid foundation for continued investigation into the temperature dependence of novel dielectrics and, in particular, the  $HfO<sub>2</sub>/SiO<sub>2</sub>$  bilayer gate stack. Some particular directions for future work that this study inspires are:

1. Investigating the existence of a link between pre-exponential terms, *σhop* and *σArr*, and the gate voltage. High electric field variable range hopping models, which relate hopping conductivity to gate voltage, exist and were primarily developed for *three*-dimensional electric field dependent variable range hopping. Further development of *two*-dimensional electric field dependent variable range hopping models may explain the temperature dependence of the gate leakage current.

- 2. A significant difference between the temperature dependence of  $3$ nm HfO<sub>2</sub> and 5nm HfO<sub>2</sub> gate stacks were observed. Hopping models suggest a thickness independence in the conductivity. Hence, the  $SiO<sub>2</sub>$  interfacial layer and  $HfO<sub>2</sub>/SiO<sub>2</sub>$  interface play an important part in the gate leakage current of thin  $HfO<sub>2</sub>$  samples. Examining the thickness dependence of the temperature dependence of the gate leakage current may further determine the role the  $SiO<sub>2</sub>$  layer and HfO<sub>2</sub>/SiO<sub>2</sub> interface plays on the temperature dependence of the gate leakage current. Thicker  $HfO<sub>2</sub>$  samples may follow hopping models more accurately allowing for better determination of defect densities in the HfO2 layer and could therefore be used for process optimization.
- 3. The success of applying DC hopping models to the temperature dependence of the gate leakage current suggest further studies be performed measuring and modeling the AC conductivity of the temperature dependence of the gate leakage current as further confirmation of hopping conduction.
- 4. The success of modeling the gate leakage current at both positive and negative gate biases using hopping conduction suggests multi-phonon trap assisted tunneling (MPTAT) [126, 127], which is also a defect mediated process that is strongly temperature dependent, may describe the temperature dependence of the gate leakage current. Description of the temperature dependence using MPTAT of the gate leakage current at positive gate biases for 3nm and 5nm  $HfO<sub>2</sub>$  nMOSFET used in this study have already been shown to capture important trends in the temperature dependence of the gate leakage current [128].
- 5. Arrhenius plots of the gate leakage current indicate non-Arrhenius behavior over the temperature regime examined. Modeling the temperature dependence of the gate leakage current using [\(8.3\)](#page-134-0), however, showed that the Arrhenius equation coupled with variable range hopping equation fits the data very well. As the Arrhenius term dominates at high temperature [\(Figure 8.8\)](#page-148-0), measuring the gate leakage current to higher temperatures  $(T > 400K)$  would help confirm the existence of the Arrhenius mechanism and may provide additional information on which Arrhenius transport mechanism is occurring.
- 6. In the application of image charge to multilayer dielectrics, a model for a thin layer dielectric sandwiched between two other materials of infinite thickness was used. In multilayer dielectric MOS devices, however, neighboring dielectrics can be quite thin yielding additional interfaces, which were not considered when deriving [\(4.15\)](#page-52-0). The presence of additional interfaces near the thin dielectric layer will modify the potential slightly in the thin dielectric layer. Due to the inverse decay of the image charge potential with respect to distance, effects of additional interfaces were considered negligible. Further work is necessary to determine how much of an effect additional interfaces will have on the potential of a thin dielectric. Finite element physics solvers such as COMSOL<sup>®</sup> are suggested as an aid in this study.

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APPENDIX A

# **A.1 Introduction to Polarons**

#### **A.1 Introduction to Polarons**

The presence of a charged carrier will distort its surroundings to some extent [45] leading to electron-phonon interactions. If the distortion is large, the rigid-band approximation fails and coupling between the lattice (phonons) and the electron must be considered [129]. An example of such an interaction is in polar ionic crystals. An electron in such a material will act to polarize the immediate surrounding lattice. To reduce the energy of the electron-lattice interaction, a quantized deformation of the lattice occurs resulting in phonons or a phonon cloud around the charged carrier; together they from a quantized quasi-particle called a polaron. As the electron moves, it will carry the phonon cloud with it and in some instances act like a free particle with a higher effective mass [129].

Polarons are divided into two categories: large polarons or Fröhlich polarons and small polarons or Holstein polarons [130, 131]. In large polarons, the radius of the polaron (the extent of the charge carrier phonon interaction) extends over many atoms. For small polarons, the phonon-charged carrier interaction is limited to the immediate surrounding atoms. Small polarons can sometimes be called "self-trapped" electrons or holes if the charge carrier "digs" a potential well that it cannot escape due to the rearrangement of the surrounding atoms. Extrinsic traps, such as oxygen vacancies in  $HfO<sub>2</sub>$ , can mediate polaron transport in a material. The extrinsic trap can confine the carrier for sufficiently long periods of time increasing the probability of lattice relaxation and thus enhancing the electron-phonon interaction  $[132]$ . In HfO<sub>2</sub> a relaxation energy of ~0.5 to 0.7eV is theorized for the negative charge state [28].

Although small polarons have sparked immense interest in the physics community since the idea was first proposed by Landau [133] and later formalized by Holstein in 1959 [131], polaron conduction has not been extensively applied to carrier transport in MOSFET gate stack with perhaps the exception of irradiated  $SiO<sub>2</sub>$  [134-136]. With the introduction of high-*k* dielectrics into the gate stack, a renewed interest in the investigation of polarons is being observed. Currently the investigation of polaron conduction in high-*k* MOSFET stacks is limited to a few groups and a handful of studies [28, 29, 36, 37, 98, 137, 138]. Most of the work performed has been theoretical with very few experimental studies.

Since phonons are directly coupled to temperature, variable temperature studies are ideally suited to aid in the investigation of polaron conduction in high-*k* dielectrics. Of the experimental work performed in polaronic transport, only one study has been reported, to the author's knowledge, in which multiple temperatures were examined and the author took part in that study [138].

APPENDIX B

# **B.1 SILVACO Input Parameters Without Quantum Mechanical Correction**

#### **B.1 SILVACO Input Parameters Without Quantum Mechanical Correction**

```
go atlas
mesh 
x.m l=0 spac=1
x.m l=1 spac=1
y.m l=-0.02 spac=0.00005
y.m l=0 spac=0.00005
y.m l=0.1 spac=0.0001
y.m l=0.5 spac=0.02
region num=1 silicon y.min=0
region num=2 oxide y.max=0 y.min=-0.0011
region num=3 nitride y.max=-0.0011 y.min=-0.0061
electrode substrate
electrode name=gate x.min=0 x.max=1 y.max=-0.0061 y.min=-0.02
doping uniform conc=1e18 p.type
save outf=TiNHfO2SiO2Si.str
go atlas
mesh inf=TiNHfO2SiO2Si.str
MATERIAL material=oxide eg300=8.9 affinity=0.95 permit=6.13
MATERIAL material=nitride eg300=5.7 affinity=2.65 permit=20 
MATERIAL material=silicon affinity=4.05
contact name=gate workfunction=4.45
models cvt srh
method carriers=0
output con.band val.band
solve init
solve vgate=0 vstep=-0.1 vfinal=-2 name=gate
save outf=TiNHfO2SiO2SiNeg2V.str
tonyplot TiNHfO2SiO2SiNeg2V.str
solve vgate=-2.01
log outf=TiNHfO2SiO2SiNeg2toPos2.log master
PROBE NAME=SurfPot X=0.1 Y=0.0 POTENTIAL
PROBE NAME=BulkPot X=0.1 Y=0.3 POTENTIAL
PROBE NAME=EoxSiO2 X=0.1 Y=-0.0005 FIELD DIR=90
PROBE NAME=EoxHfO2 X=0.1 Y=-0.004 FIELD DIR=90
solve vstep=0.01 vfinal=2.0 name=gate
save outf=TiNHfO2SiO2SiPos2V.str
### plot results
tonyplot TiNHfO2SiO2SiPos2V.str
tonyplot TiNHfO2SiO2SiNeg2toPos2.log
```
quit
**B.2 SILVACO Input Parameters With Quantum Mechanical Correction**

## **B.2 SILVACO Input Parameters With Quantum Mechanical Correction**

```
go atlas
```

```
mesh 
x.m l=0 spac=1
x.m l=1 spac=1
y.m l=-0.02 spac=0.00005
y.m l=0 spac=0.00005
y.m l=0.1 spac=0.0001
y.m l=0.5 spac=0.02
region num=1 silicon y.min=0
region num=2 oxide y.max=0 y.min=-0.0011
region num=3 nitride y.max=-0.0011 y.min=-0.0061
electrode substrate
electrode name=gate x.min=0 x.max=1 y.max=-0.0061 y.min=-0.02
doping uniform conc=1e18 p.type
save outf=qm_TiNHfO2SiO2Si.str
go atlas
mesh inf=qm_TiNHfO2SiO2Si.str
MATERIAL material=oxide eg300=8.9 affinity=0.95 permit=6.13
MATERIAL material=nitride eg300=5.7 affinity=2.65 permit=20 
MATERIAL material=silicon affinity=4.05
contact name=gate workfunction=4.45
models fermi schro new.eig ox.poisson qy.min=-0.0015 qy.max=0.5 qx.min=0 
       qx.max=1 ox.schro fixed.fermi
method carriers=0
output con.band val.band t.quantum eigens=4
solve init
solve vgate=0 vstep=-0.1 vfinal=-2 name=gate
save outf=qm_TiNHfO2SiO2SiNeq2V.str
tonyplot qm_TiNHfO2SiO2SiNeg2V.str
solve vgate=-2.01
log outf=qm_TiNHfO2SiO2SiNeg2toPos2.log master
PROBE NAME=SurfPot X=0.1 Y=0.0 POTENTIAL
PROBE NAME=BulkPot X=0.1 Y=0.3 POTENTIAL
PROBE NAME=EoxSiO2 X=0.1 Y=-0.0005 FIELD DIR=90
PROBE NAME=EoxHfO2 X=0.1 Y=-0.004 FIELD DIR=90
solve vstep=0.01 vfinal=2.0 name=gate
save outf=qm_TiNHfO2SiO2SiPos2V.str
### plot results
tonyplot qm_TiNHfO2SiO2SiNeg2toPos2.log
tonyplot qm_TiNHfO2SiO2SiPos2V.str
quit
```
## APPENDIX C

## **C.1 Transmission Coefficient Analysis**

## **C.1 Transmission Coefficient Analysis**

In a study performed by Ling-Feng Mao on poly-Si/HfSiO /Si, the temperature dependence of the gate leakage current (100K-300K) was modeled using quantum mechanical tunneling (no defect mediated tunneling was considered) [9]. The temperature range used in Mao's study is similar to the temperature range in this study (6K-400K) and while performed on a different gate stack begs the question "can quantum mechanical tunneling explain the temperature dependence of the gate leakage current?" If the answer is no, it suggests defect mediated transport is responsible for the gate leakage current and the temperature dependence (recall that carrier emission over the barrier was shown not to be responsible for the gate leakage current in Chapter 7).

As was discussed in Section [2.1,](#page-23-0) to first order, tunneling is temperature independent but many secondary parameters depend on temperature, such as effective mass, carrier energy and population levels, band offsets, etc. The quantum model developed in Section [4.1.6](#page-55-0) only calculates the transmission coefficient through the dielectric barriers; it does not calculate the carrier energy levels or population density quantum mechanically.<sup>[20](#page-183-0)</sup> However, comparing the transmission coefficient between the 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> and 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> gate stacks can provide insight into whether quantum mechanical tunneling is responsible for the temperature dependence of the gate leakage current.

Consider [Figure C.1](#page-185-0) where the energy band diagram for a 3nm  $HfO<sub>2</sub>$  (thick lines)/1.1nm  $SiO<sub>2</sub>$  nMOSFET and 5nm HfO<sub>2</sub> (thin lines)/1.1nm nMOSFET are shown.

<span id="page-183-0"></span> $20$  The energy band simulation tool uses classical mechanics and Boltzmann's statistics as an approximation to Fermi-Dirac statistics to calculate the carrier density in the semiconductor.

For both the 3nm and 5nm  $HfO<sub>2</sub>$  devices, the stack is biased such that the electric field in the HfO<sub>2</sub> layer is 2MV/cm. Due to the same electric field bias and that the  $SiO<sub>2</sub>$  IL and Si substrate is the same for both layers, the band bending in the  $SiO<sub>2</sub>$  and  $Si$  substrate is the same as shown in [Figure C.1.](#page-185-0) To first order, the quantized energy states in the Si inversion layer and population density are the same for the  $3$ nm and  $5$ nm HfO<sub>2</sub> devices at this bias condition. Also notice that the tunneling distance for electrons from the substrate through both the  $SiO<sub>2</sub>$  (direct tunneling) and HfO<sub>2</sub> (Fowler-Nordheim tunneling) at or above the Si Fermi energy level is the same for the 3nm and  $5nm$  HfO<sub>2</sub> devices. Given these similarities, one should expect that, *if* the gate leakage current is due to quantum mechanical tunneling, *then* the gate leakage current for 3nm HfO<sub>2</sub> nMOSFETs biased at 1.8V ( $E_{ox,HfO2}$  = 1.98MV/cm) should equal the gate leakage current of 5nm HfO<sub>2</sub> nMOSFETs biased at 2.2V (*Eox,HfO2* = 1.98MV/cm). Here the aforementioned premise is considered.



<span id="page-185-0"></span>Figure C.1: Energy band diagram for 3nm  $HfO<sub>2</sub>$  (thick lines) and 5nm  $HfO<sub>2</sub>$  (thin lines) nMOSFETs with a 1.1nm  $SiO<sub>2</sub>$  IL biased at an electric field of 2MV/cm in the HfO<sub>2</sub> layer. The tunneling distance for both stacks is identical.

Consider the gate leakage current of 3nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  and 5nm  $HfO<sub>2</sub>/1.1$ nm  $SiO<sub>2</sub>$  at the four  $E<sub>ox,HfO2</sub>$  biases shown in [Figure C.2.](#page-186-0) A difference in the gate leakage current between the 3nm and 5nm  $HfO<sub>2</sub>$  devices that is close to two orders of magnitude is observed in [Figure C.2](#page-186-0) for equivalent  $E_{ox, HfO2}$  biases. The forbidden region of the barrier (labeled in [Figure C.1\)](#page-185-0) for equivalent  $E_{ox,HfO2}$  larger than 2MV/cm in the 3nm and  $5$ nm HfO<sub>2</sub> stacks is the same. While the forbidden region of the barrier is the same for the 3nm and 5nm nMOSFETs, shown in [Figure C.1,](#page-185-0) outside the forbidden region the barrier is not the same on the TiN/HfO<sub>2</sub> side. For the 3nm HfO<sub>2</sub> case, the electron exits into the TiN layer and for the 5nm  $HfO<sub>2</sub>$  case the electron exits into the  $HfO<sub>2</sub>$  conduction band. Even if higher electric fields are considered, the potential barrier outside the forbidden region is not identical. The transmission coefficient is strongly dependent on the thickness and height of the forbidden region of the barrier and to a lesser extent the shape

of the barrier outside the forbidden region. Does the shape of the barrier outside the forbidden region modify the transmission coefficient enough to account for a near two order magnitude difference in the gate leakage current? To quantify the effect this will have on the transmission coefficient, the energy band simulation tool is used to calculate the transmission coefficient for the 3nm and 5nm  $HfO<sub>2</sub>$  devices for comparison.



<span id="page-186-0"></span>Figure C.2: Comparison of the gate leakage current of  $3$ nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> to 5nm  $HfO<sub>2</sub>/1.1$ nm Si $O<sub>2</sub>$  at equivalent  $E<sub>ox,HfO2</sub>$  biases where the tunneling barrier over the tunneling distance is the same.

In order to calculate the transmission coefficient for the 3nm and 5nm  $HfO<sub>2</sub>$ devices, an effective mass for  $HfO<sub>2</sub>$  is required. However, a wide variety of effective masses of electrons in  $HfO<sub>2</sub>$  have been reported in the literature and range in value from  $\sim 0.1 m_0$  to  $\sim 0.5 m_0$  [7, 34, 61, 139-141], where  $m_0$  is the mass of an electron in free space. Here a comparison of the transmission coefficient using an effective mass of  $0.44m<sub>0</sub>$ [139] and  $0.11m_0$  [141] for HfO<sub>2</sub> layer is considered with an effect mass of  $0.5m_0$  [142,

143] for the  $SiO<sub>2</sub>$  IL. The transmission coefficients for 3nm and 5nm HfO<sub>2</sub> devices at four bias conditions are shown in [Figure C.3.](#page-187-0) $^{21}$  $^{21}$  $^{21}$  The transmission coefficient is shown for a transmission coefficient ([Figure C.3](#page-187-0)) over this energy range. The energy location of the range of electron energies (*E*) from the Si conduction band edge ( $E_c$ ) at the SiO<sub>2</sub>/Si interface to 1eV above *Ec*. Resonance peaks (i.e., local maxima) are observed in the transmission coefficient resonance peaks changes as  $E_{ox,HfO2}$  changes. The energy location of the transmission coefficient resonance peaks also depends on the  $HfO<sub>2</sub>$  thickness. While there are general similarities in the position and magnitude of the transmission coefficients between 3nm and 5nm [\(Figure C.3\)](#page-187-0), the differences are substantial enough such that a direct comparison would be unrealistic.



<span id="page-187-0"></span>Figure C.3: Transmission coefficients as a function of energy above the Si conduction band for 3nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> (black lines) and 5nm HfO<sub>2</sub>/1.1nm SiO<sub>2</sub> (red lines) barriers at four  $E_{ox,HfO2}$  bias points using HfO<sub>2</sub> effective masses of (a) 0.11 $m_0$  and (b)  $0.44$ *m*<sub>0</sub>.

A resonance peak is observed at lower energy levels in the  $5<sub>nm</sub>$  HfO<sub>2</sub> device

compared to the 3nm HfO<sub>2</sub> device. The resonance peak at lower energy in the 5nm HfO<sub>2</sub>

<span id="page-187-1"></span> $21$  The effective mass of the electron in the Si substrate and TiN gate are not considered in the transmission coefficient calculation. The transmission coefficient calculation only considers the ratio of the incidence and transmitted waves through the dielectrics, which is independent of the gate and substrate effective masses.

device, which results in a larger transmission coefficient, suggests that the 5nm  $HfO<sub>2</sub>$ should have a larger tunneling current compared to the  $3$ nm  $HfO<sub>2</sub>$  devices. Tunneling current does not solely depend on the transmission coefficient however, but also on the number of carriers available to tunnel (carrier concentration). The carrier concentration varies significantly with energy and requires solving the Poisson-Schrödinger equations to accurately determine the carrier concentration versus energy. Due to this complexity, the average of the transmission coefficients of  $3$ nm and  $5$ nm  $HfO<sub>2</sub>$  stacks are compared as a simple means to evaluate whether enough disparity between the transmission coefficients exist to account for the approximately two orders of magnitude difference in the measured leakage current.

<span id="page-188-0"></span>The chosen method of comparing the average difference in the transmission coefficient is given as:

$$
\% \Delta_{Avg} \overline{T}_{5nm} = \frac{1}{E_0} \int_{E_C}^{E_C + E_0} \frac{T_{5nm}(E) - \frac{T_{5nm}(E) + T_{3nm}(E)}{2}}{\frac{T_{5nm}(E) + T_{3nm}(E)}{2}} \times 100 dE
$$
  

$$
= \frac{100}{E_0} \int_{E_C}^{E_C + E_0} \left( \frac{2T_{5nm}(E)}{T_{5nm}(E) + T_{3nm}(E)} + 1 \right) dE
$$
 (C.1)

<span id="page-188-1"></span>and

$$
\% \Delta_{Avg} \overline{T}_{3nm} = \frac{1}{E_0} \int_{E_C}^{E_C + E_0} \frac{T_{3nm}(E) - \frac{T_{5nm}(E) + T_{3nm}(E)}{2}}{\frac{T_{5nm}(E) + T_{3nm}(E)}{2}} \times 100 dE
$$
  
= 
$$
\frac{100}{E_0} \int_{E_C}^{E_C + E_0} \left( \frac{2T_{3nm}(E)}{T_{5nm}(E) + T_{3nm}(E)} - 1 \right) dE
$$
 (C.2)

where  $E_0$  is the energy interval above the conduction band over which to compare and average the transmission coefficients. In the formulation above for comparing the transmission coefficient,  $(C.1)$  and  $(C.2)$ , the difference in the transmission coefficient of one stack and the average transmission coefficient of both  $HfO<sub>2</sub>$  stacks is taken and then referenced to the average transmission coefficient of both stacks and turned into a percent by multiplying by 100. By integrating over an energy interval of  $E_0$  above the conduction band and dividing by  $E_0$ , the average difference in the transmission coefficients is computed. Two important advantages exist by using this method of comparison.

- 1. By comparing the difference in the transmission coefficient of one stack to the average transmission coefficient of both stacks [e.g. *T5nm*-(*T3nm*+*T5nm*)/2] and referencing that difference to the average transmission coefficient of both stacks [i.e., dividing by  $(T_{3nm}+T_{5nm})/2$ ], a symmetrical comparison is made (i.e.,  $\sqrt[6]{\Delta_{Avg}} \overline{T}_{3nm}$  and  $\sqrt[6]{\Delta_{Avg}} \overline{T}_{5nm}$  are equal but opposite values). By comparing the transmission coefficient to the average voids the possibility where both stacks indicate they have a higher transmission coefficient than the other.
- 2. By referencing the difference in the transmission coefficients [e.g.,  $T_{5nm}$ - $(T_{3nm}$ + $T_{5nm}$  $/2$ ] to the average transmission coefficient [i.e.,  $(T_{3nm}+T_{5nm})/2$ ] before performing the integral, the difference in the transmission coefficients are weighted evenly. At large energy levels, the transmission coefficients are larger, creating larger differences between the transmission coefficient of one stack and the average transmission coefficient of both stacks. Without normalizing this value to the average transmission

coefficient of both stacks, the comparison would be skewed toward higher energy levels.

Using an energy interval,  $E_0$ , of 1eV a comparison of % $\Delta_{Avg} \overline{T}_{3nm}$  and % $\Delta_{Avg} \overline{T}_{5nm}$ for the four  $E_{ox,HfO2}$  values shown in [Figure C.3](#page-187-0) is given in [Table C.1. Table C.1](#page-190-0) indicates that the transmission coefficient of the 5nm  $HfO<sub>2</sub>$  stack is slightly larger on average than the 3nm HfO<sub>2</sub> stack, regardless of the HfO<sub>2</sub> effective mass considered  $(0.11m_0)$  or 0.44*m*<sub>0</sub>). Allowing for variation between the modeled energy band structure and the actual energy band structure is not enough to close the gap between the nearly two decade difference between the gate leakage current between the 3nm and 5nm  $HfO<sub>2</sub>$  gate stacks. The discrepancy between the theoretical transmission coefficient and the experimental gate leakage current indicates that quantum mechanical tunneling (nondefect mediated) cannot explain the gate leakage current or its temperature dependence for the  $HfO<sub>2</sub>$  gate stacks in this study.

$E_{ox,HfO2}$ (MV/cm)	$3$ nm HfO <sub>2</sub>			$5$ nm HfO <sub>2</sub>		
	$V_{Gate}$ (V)	$\% \Delta_{Avg} \overline{T}_{3nm}$ $m^* = 0.11 m_0$	$\% \Delta_{total} T_{3nm}$ $m^* = 0.44 m_0$	$V_{Gate}$ (V)	$\% \Delta_{Avg} T_{5nm}$ $m^* = 0.11 m_0$	$\% \Delta_{Avg} T_{5nm}$ $m^* = 0.44 m_0$
1.98	1.8	$-6.52$	$-14.49$	2.2	6.52	14.49
2.13	1.9	$-10.52$	$-12.97$	2.33	10.52	12.97
2.28	റ	$-9.64$	$-9.62$	2.46	9.64	9.62
2.42	2.1	$-5.28$	$-0.84$	2.58	5.28	0.84
	Average $(\% )$	-7.99	$-9.48$	Average $(\% )$	7.99	9.48

<span id="page-190-0"></span>**Table C.1: Comparison of Average Transmission Coeffecients**