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Enhancement of historical printed document images by combining Total Variation regularization and Non-Local Means filtering

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Abstract

This paper proposes a novel method for document enhancement which combines two recent powerful noise-reduction steps. The first step is based on the total variation framework. It flattens background grey-levels and produces an intermediate image where background noise is considerably reduced. This image is used as a mask to produce an image with a cleaner background while keeping character details. The second step is applied to the cleaner image and consists of a filter based on non-local means: character edges are smoothed by searching for similar patch images in pixel neighborhoods. The document images to be enhanced are real historical printed documents from several periods which include several defects in their background and on character edges. These defects result from scanning, paper aging and bleedthrough. The proposed method enhances document images by combining the total variation and the non-local means techniques in order to improve OCR recognition. The method is shown to be more powerful than when these techniques are used alone and than other enhancement methods.

Keywords: Document image enhancement; Image processing; Variational approach; Non-local Means; Historical documents; Character recognition

1 Introduction

A large number of document images are available for consulting, exchange and remote access purposes. These images have been scanned from collections of historical documents in libraries or archives thanks to digitization projects [3, 20, 15]. Accessing the content of document images is fully enhanced when textual transcriptions are attached to them: this allows users to index and search images through textual queries. For establishing such transcriptions, automatic tools such as OCR systems (Optical Character Recognition) are used to convert document images into text lines and words in ASCII format. However OCR systems are very sensitive: when facing noise, they perform poorly for both segmentation and recognition tasks. Historical documents include many defects due to aging and human manipulations. These defects include bleed-through ink, folding marks, ink fading, holes and spots. The grain of the paper can also produce texture in the background. The scanning process can produce uneven illumination in the image, modify character edges and create other types of defects such as streams due to microfilms [8]. Thus, reducing or removing noise in document images is an important issue for improving OCR recognition. The main goal of this paper is to show that two recent powerful image restoration techniques can be combined to drastically improve the recognition performance.

Several approaches have been proposed for enhancing document images. Leung et al. [24] enhance contrast with the POSHE method based on sub-block histogram

equalization: the readability of very low-contrast images is improved. Sattar and Tay [32] deblur noisy document images using fuzzy logic and multi-resolution approaches. Pan et al. [29] correct uneven illumination and remove wood grain and shading on images of text incised on wood tablets by filtering: this allows handwritten strokes to be more easily extracted. Removing shades in document margins produced while scanning thick documents with a region growing method has been studied by Fan et al. [17]. Shades in the background can also be detected by morphological operations and lightened for removal [28]. The water flow model of [21] can extract the different background layers of a document while binarizing it. Restoring character edges by PDE-based (Partial Differential Equations) approaches has been proposed in [14]. This approach regularizes a document image using anisotropic diffusion filtering through an iterative process. Removing bleed-through pixels has been proposed by [27, 38]. These approaches require co-registration of the recto and verso images. Source separation is another framework to address document enhancement [37]. It assumes that each pixel results from the mixture of different sources (background, foreground and, in the case of palimpsests, another writing layer). With such approach, smoothing, noise removal and thresholding are performed jointly. It contrasts with our filtering-based approach which is fast thanks to efficient algorithms and does not assume any structure of the document.

Document image enhancement can be the first step of a binarization task. To handle the variations of foreground and background brightness in historical documents, local binarization methods may be preferred to global ones [33]. In [19], noise reduction by Wiener filtering is performed prior to the local (adaptive) binarization of the document image. In [6] a combination of a global and a local method is used to binarize handwritten characters whose edges are blend with the background. The

local method classifies within a local window those pixels connected to the seed image of a noisy character obtained from the global thresholding. Markov Random Fields (MRFs) approaches [39, 41, 42] are also suitable for document enhancement. Such approaches include in a single model both the data (the spatial local context of a pixel) and a degradation model. In [39], a MRF-based blind deconvolution is used to segment touching characters. In [42], both character repair and binarization are performed through MRF modeling. Wolf in [41] uses a MRF with two hidden label fields to distinguish between recto pixels, verso pixels and those superimposed with the verso due to bleed-through. The labeling is obtained by energy minimization.

Most reported methods require an elaborated process to describe the document structure. For instance MRF approaches which build a statistical model for each layer of the document, have a parameter estimation process. Such methods have the ability to separate the different layers of a document (characters, noise, one or several backgrounds) but at the cost of increased time and computational complexity. In contrast, the method we propose is simpler and fast since it is based on filtering (TV and NLmeans). Compared with other filtering approaches (see Section 4.4), our approach is more efficient and need only to tune a single parameter.

Our approach is based on regularization and filtering and aims at reducing the noise level in the background and on character edges of document images. The background noise comes from ink bleeding from the verso or from defects of the recto. The existence of such noise makes document segmentation and recognition difficult: additional pixels may fill the inter-line and inter-word spaces or create confusing character shapes. Character edges may be not smooth due to scanning. The proposed method combines two restoration steps based respectively on the Total

Variation regularization approach (TV) and Non-local Means (NLmeans) filtering.

Two methods of combining TV and NLmeans are proposed and analysed. Figure 1 shows the flowcharts of the proposed combinations. In Figure 1-a the input image is pre-processed by TV in order to reduce background noise. A mask is constructed from this TV-processed image through binarization and dilation operations. The resulting binary image is applied as a mask on the TV-processed image. This results in a grey level image with low background noise and smoothed edges. The NLmeans filter is then applied to enhance character details. This combination is called the type-A combination. In the second combination scheme, the type-B combination shown in Figure 1-b, the mask is applied to the image pre-processed by NLmeans rather than TV but the mask construction is identical. The decision whether to apply the first or second combination scheme is related to character dimensions and document contrast (see Section 4.3.3). Our approach contrasts with PDE-based approaches since it relies on both regularization and on the use of a mask for a better noise removal between text lines, while PDE relies on an evolution process that requires a stopping time. We compare both approaches in Section 4.5. Our approach is also different from the MRF approach of [41] since we do not attempt to detect noisy pixels but rather regularize the grey level values of both background and text.

The paper is organized as follows. In Section 2, the background noise reduction based on Total Variation is presented, as well as the mask construction. Section 3 presents the foreground noise reduction based on NLmeans. In Section 4.3.1, we describe the parameter setup for the main regularization β parameter. In Section 4, we validate the proposed method on printed documents from various periods showing its robustness to a range of degradations. Our evaluation is based on edge

Figure 1. Flowcharts of the two proposed enhancement methods combining TV regularization and NLmeans filtering. a) type-A combination b) type-B combination. quality and on the recognition rate of an open source OCR, at the character level. Section 5 concludes the paper.

2 Background noise reduction by Total Variation regularization

The first step of our enhancement method is based on the Total Variation (TV) regularization approach. The image is first filtered by TV, then from the filtered image a mask is constructed (see Figure 1). TV is a filtering method which preserves edges and sharp boundaries while reducing noise in the background. This property is desirable since background noise reduction increases the ability of an OCR system to extract textual data at different levels: zones, text lines and characters. The mask construction mainly uses the property of background noise reduction in regions distant from the characters but TV can also be used for enhancing character edges (see Section 2.2).

We introduce the following notation for our enhancement method. It is assumed that an image is defined on a 2D regular grid S. Let us denote by Ω the set of such images. The input image and its restored version are denoted by v and \hat{u} , respectively. The grid S is endowed with a neighborhood system N and we denote by $\mathcal{N}(s)$ the set of sites that are neighbors of site s (relative to \mathcal{N}).

2.1 Total Variation

The TV approach relies on image modeling and a variational point of view. Variational approaches are popular methods for image restoration. Few works use a variational approach in the domain of document analysis and recognition [7]. In [7], a variational approach is used at the character level for the restoration of degraded character contours. This approach needs a reference character for the contour in the degraded region of the character, to converge to the desired position. In contrast, our method aims to apply the TV approach directly to document images as a noise reduction step. Variational and Markovian formulations of the image restoration problem consist of minimizing an energy that is generally a weighted combination of two terms, namely the data fidelity and the regularization (also called prior). Since a discrete framework is considered in this paper, we consider a Markovian point of view as presented in $[13]$. The data fidelity D measures how far the current solution

Figure 2. Total Variation: input and regularized words for increasing values of regularization parameter β . Background noise is flattened as β increases.

u is from the observed image v. It is defined from the nature of the noise that corrupts the image. For instance, a separable quadratic data fidelity term corresponds to the assumption that the noise is additive Gaussian noise. We assume here such noise and thus the data fidelity is defined as

$$
D(u|v) = \frac{1}{2} \sum_{s \in S} (u(s) - v(s))^2 \quad \forall u \in \Omega,
$$
\n
$$
(1)
$$

where u is a candidate image defined on Ω . The value of the image u at site s is denoted by $u(s)$.

The prior should embed the knowledge we have of the nature of the problem, e.g., the statistical properties of the image. Among many regularization terms that have been proposed (see [40], for instance), Total Variation has been a popular one since the seminal works of [9, 31]. The main characteristics of the TV prior is that the solution lives in the space of functions of Bounded Variation that allows for sharp edges and discontinuities. We follow [13] and define TV as the l^1 -norm of a discrete

gradient. More formally we have

$$
TV(u) = \sum_{s} \sum_{t \in N(s)} |u(s) - u(t)| \tag{2}
$$

Recall that $N(s)$ denotes the set of pixels that are neighboring the site s. In this paper, we consider the 4-nearest neighbors.

The restored image \hat{u} which corresponds to the candidate image u which minimizes the energy $E(.|v)$ that is a weighted combination of the two above terms

$$
\hat{u} = \underset{u}{\arg\min} E(u|v) = \underset{u}{\arg\min} [D(u|v) + \beta \cdot TV(u)] \quad , \tag{3}
$$

where the parameter β is non-negative. This coefficient is a parameter that governs the balance between the data fidelity and the regularization; a large value for β will produce an image with few details while a tiny one will yield an image that leaves v almost unchanged. It was shown in [26] that such an approach is prone to a loss of contrast. This prevents us from using a high regularization value since in addition to removing noise, it would both remove small features that can be text, and reduce too much the contrast so that the binarization process would fail to produce the desired result. Figure 2 shows the effect of the regularization parameter β on sample words. The background has been regularized with values of $\beta = 5$ and $\beta = 20$. Larger values of β such as $\beta = 60$, produce more regularization which can also remove smaller desired image features and fill intra-character spaces. If the image contains small characters from low resolution scanning (around 13-14 pixels in height), the value of β should be a smaller value, typically lower than 10.

For highly degraded documents (see Figure 3), TV can considerably reduce the background noise on character contours. However small character components from

Figure 3. Edges from a highly degraded word from set XVIII-b. From top to bottom: without regularization, after regularization by TV. fading characters may vanish.

2.2 Construction and application of the mask

The first step of both type-A and type-B enhancement is the construction of a mask from a TV regularized image to denote pixels that clearly belong to the background. The TV-regularized image is thresholded by the Otsu algorithm to locate the set of pixels which in majority belong to text. Second, the thresholded image is dilated by a squared structuring element of side 9 pixels. This results in a binary mask where regions around characters are set to 0 and the remaining ones to 1.

The mask is superimposed on the initial image to construct the masked image. The masked image consists of saturating at value 255 the image values corresponding to mask value 1, and recovering the initial pixel values corresponding to mask values 0. The mask can be applied to any image and we choose to apply it either to the TV-regularized image which has been created during mask construction or to the NLmeans filtered image (see also Section 3). This corresponds to the type-A and type-B combination methods respectively. The choice of the image to be masked depends on the character size since spaces within small-sized characters processed by TV are more likely to be filled (see Section 4.3). There is no such effect with NLmeans. The choice of the combination type according to the characteristics of the document set is described in Section 4.3.3.

Figure 4 shows the TV regularized image obtained from an input image. For this document, the TV image has been masked and the masked image (Figure 4-d) is different from the TV image (Figure 4-b) since background pixels distant from character pixels have been saturated.

3 Non-Local Means filtering

The NLmeans filtering is used in our combined approach in two ways (see Section 1). The filtering can be applied either to the TV-regularized masked image as an additional filtering step (type-A), or to the input image which is then masked (type-B). The mask construction is described in Section 2.2. NLmeans is a non-local filter which can smooth character parts from neighboring data. NLmeans averages neighboring parts of the central pixel but the averaging weights depend on the similarities between a small patch around the pixel and the neighboring patches within a search window [10]. NLmeans capitalizes on the redundancy present in most images [10]. Document images may contain even more redundancy than other types of images. As previously defined, the input image and its restored version are denoted by v and \hat{u} respectively. The NLmeans filter considers the similarity of a block of neighboring

c) d) b) a)

Figure 4. a) Input image b) TV-regularized image c) Mask d) Enhanced image resulting from the application of the mask on the TV image. Pixel values outside character regions are saturated to 255.

pixels to the block centered on the pixel under evaluation. We denote such a block by Δ . For the sake of clarity we assume it is a square patch whose side is $(2P + 1)$. The similarity measure $w(s, t)$ for the two sites s and t is defined as

$$
w(s,t) = g\left(\sum_{\delta \in \Delta} \left(v(s+\delta) - v(t+\delta)\right)^2\right) \tag{4}
$$

where $g(x) = \frac{1}{1 + (x/2)^2}$.

Once the similarity measures are available they are convexly combined to produce

Figure 5. NLmeans approach: two patches Δ of size $2P + 1$ around t and t' within the size $2K+1$ search window centered on s. The similarity measure between patches is computed from all pairs of points at the same location within patches.

the filtered image. The value of the filtered image at site s is

$$
\hat{u}(s) = \frac{1}{Z(s)} \sum_{t \in \mathcal{N}(s)} w(s, t)v(t) , \qquad (5)
$$

where $Z(s)$ is a normalization constant defined as $Z(s) = \sum_{t \in \mathcal{N}(s)} w(s, t)$ for all sites, and $\mathcal{N}(s)$ the set of sites that are neighbors of s. In the original NLmeans version [10], the similarity is assumed to be computed for every pair of pixels, and thus $N(s) = S \setminus \{s\}$ (all image sites not including s). This is extremely time consuming. Instead, the similar sub images for the pixel are searched for in a region around the considered pixel: the search window. Let us assume that this search window is a square whose side is $2K + 1$. The number of patches within the search window is $(2K+1)(2K+1)-1$. In our implementation, when the patch reaches pixels outside the image, we replicate the image pixels in a mirror-based way. Otherwise, we consider the actual image pixels. The size of this search window affects the pixels that could be found and the level of regularization on the image. A larger searching window possibly allows more similar patches to be found and thus would yield a filter that better preserves the features. This also tends to produce more regularized images since the restored pixel will be a weighted average of more values. This behavior gives a background that is more homogeneous. But since NLmeans never completely discards patches, this tends to smooth too much and we have shown in [25] that fading characters lose more pixels when the search window is too wide. Increasing K also produces a small loss of contrast. Let us emphasize that this loss is more modest than for the Total Variation based filter. Nevertheless, there will be less contrast between background and characters due to the averaging with more data patches. Moreover increasing K yields a higher computational load since complexity is $K^2 \cdot N$ (N is the image size).

The complexity of our implementation is independent of P. However, when increasing the size of patches, it is more unlikely to find similar patches. This is why P is generally kept small. If images include characters of greater size, one could increase the size of K and P . In practice, this is not performed because of the computational load due to the higher value of K. Default parameters for the NLmeans approach, $K = 4$ and $P = 3$, are widely used for a number of applications. We also use the default parameters in our proposed enhancement method. Figure 6 shows the effect of the NLmeans filtering on a sample word and characters of set XXa. We observe that the noisy background has been strongly smoothed since similar patches can be found for background pixels. The fading pixels of the character n have been preserved; they have been less smoothed since less similar patches have been found. We also observe a small improvement on the edges of the binarized character j since similar patches can be found along the long vertical stroke of this character. It can be noted that edges are also regularized by TV but small objects such as fading pixels may vanish with TV.

Figure 6. From top to bottom. An input sample word and enlarged character. The same word and character enhanced by NLmeans. Input word, enlarged and binarized character. Same word and character enhanced by NLmeans. NLmeans filtering reduces background noise and preserves character details.

4 Experiments

Experiments are conducted to evaluate the combination of TV and NLmeans on printed documents of various periods. The effect that this combination has on sample images is illustrated in Section 4.2. Section 4.3 then shows how this combination fares when used for OCR both when TV and NLmeans are used as stand alone algorithms, and when they are combined. Sections 4.4, 4.5 and 4.6 compare our method with other preprocessing methods.

4.1 Data sets

Three sets of real degraded documents are used in these experiments. The sets are built according to the period in which the documents were created: the XVII, XVIII or XX century. Each set currently includes text images from two document collections, so that each set can be separated into set-a and set-b (see Figure 7). Set XVII includes 1,457 characters from the electronic collection of the British library [2]. Set XVII-a comes from a Hamlet theater piece, while set XVII-b is a festival book in French. Set XVIII includes 4,560 characters of French Gazettes, newspapers from the 18th century [4]. Set XVIII-a (Gazette d'Avignon) is less degraded, while set XVIII-b (Gazette de Leyde) includes more degraded characters. Set XX includes 496,836 characters of twentieth century documents. Sample images from a French journal whose publishing period is around 1930 are used to form set XX-a [1] and the whole set News.3G provided by ISRI forms set XX-b [36]. Table 1 shows how the size of x-characters varies according to the sets. The smallest characters are found in set XVIIa.

4.2 Edge analysis on sample documents

An enhanced image resulting from the TV and NLmeans combination is presented in Figure 8-b for a noisy document of the XVIII century. Background noise comes from ink bleeding from the recto and the verso (see Figure 8-a). The TV regularized image has been obtained with $\beta = 20$. Background noise has been reduced by the type-A combination of TV and NLmeans (see Fig. 8-b).

Table 1

Dataset image specifications. Size of x characters and qualitative description of the primary noise effects.

The method can be compared with two well-known restoration methods: the median filter and the Wiener filter which are popular methods for noise reduction (see also Section 4.4). For this experiment, the window size of the median filter is 3x3. Results in Figure 8-b-c-d show that our method reduces the number of extraneous edges compared to the median and Wiener filters and produces more regular edges. This can be seen for instance on the first character u of the third text line (Fig. 8-f). Since the proposed method is mask-based, we also show a result when the mask is constructed using the Wiener filter instead of TV. Results in Fig. 8-e and f show that TV is more efficient than Wiener for removing background noise and regularizing edges, when combined with NLmeans.

Another result in Figure 9-b-c-d-e shows that our method reduces the effect of the stream due to microfilm. This stream is located in the area between the second

> rd of dawning fingeth all ni en they fay, no fpirite darey ghtsare wholefome, then no rie takes, nor Witch hath po ious, and fo hallowed is that So haue I heard, and doe the Sunne in ruffet mantle s ore the deaw of yon hie mo we our watch vp, and by m mpart what wee haue feene

d'armes à feu, & fonnant les clocl mandant dépêcha fix Compagnie parer de deux Ponts peu éloig cord. Près de Lexington, ces Com verent un gros d'habitans, fous l fermoient le chemin. Les Troupes droit à eux; ils fe diffipent en hâte de confusion; mais de derriere u maifons où ils s'étoient retirés, il ques décharges qui n'eurent pas

> même avec famille r ses seraient transfor le matériel des pon aussi dans ces comi pres à être transfor poste de police, ress des fêtes et marchés L'ancienne maison

Les compagnies des Gardes tant Suifles que Françoiles, qui ce iour là eftoient en garde deuant le Louure, commandées par le fieur de Guibriand Capitaine au Regiment des Gardes, fe mirent en haye depuis la barriere de la rue des Poulies iufque à la grande porte du Louure, en lamefme force qu'elles font lors que le Roy entre, excepté que les tambours ne battoient pas lors que fon Alteffe paffa. Les Suiffes de la Garde du Corps

bras de la Compagnie : Il é Oncle, Frere de fa Mere. pour motif de fa fuice le de de reiter son Pere du trifte e

Figure 7. Sample documents. From top to bottom, left to right: XVII-a, XVII-b, XVIII-a, XVIII-b, XX-a, XX-b.

and third lines. However, as mentioned earlier (see Section 2.1) small character components may vanish when regularized by TV as seen in Fig. 9-b. Detecting such fading character areas would be useful in order to adapt locally the β parameter. In summary, we have shown in this Section that:

- the proposed method has the ability to regularize background noise such as microfilm streams and character edges,

- It is thus easier for an OCR to locate characters and recognize their shapes.

f)	ய យ្ញ	று க खु ⋓
e)	parer de deux Ponts pe cord. Pres de Lexington, c verent un gros d'habitans	parer de deux Ponts pe cord. Près de Lexingron , c terent un gros d'habitans
d)	parer de deux Ponts pe cord. Près de Lexington, c verent un gros d'habitans	parer de deux Ponts per cord. Près de Lexingron , c kasant mu Ease q'yeprens'
c)	parer de deux Ponts pe cord. Pres de Lexington, c verent un gros d'habitans	parer de deux Ponts pe cord. Prės de Lexingron , c <i>x</i> caswi ww BLos q proprens
b)	parer de deux Ponts pe cord. Près de Lexington, c verent un gros d'habitans	parer de deux Pours per cord. Pres de Lexingron , c zacant un gros d'habitans
a)	parer de deux Ponts pe cord. Près de Lexington, c verent un gros d'habitans	parer de deux Ponts pe cord. Près de Lexingron , c sassidad'ib song qilabicans

Figure 8. Edges obtained with a) input image b) proposed method (type-A) c) Median filter d) Wiener filter e) combination method with TV replaced by Wiener f) sample character u (on third line) obtained with methods a)-e).

4.3 Evaluation through recognition

The proposed methods are evaluated through recognition performance on printed documents of various periods described in Section 4.1. To evaluate the performance of the proposed approach, we pass the enhanced images through the OCR Tesseract [34]. This OCR was originally developed by HP and obtained good results at the UNLV accuracy test in 1995 [36]. It is now available open source through Google. The set XX-b is one of the sets tested in the UNLV evaluation as set News.3G. The

a)	Oncle, Frere de pour motif de sa de reirer son Père	Oncle , Frere de ⁷ pour morif de fa- IS reiner fon Pere
$_{\rm b)}$	Oncle, Frere de pour motif de fa de re ifer fon Pere	් 9b නන්හි දී, xkna© powr morif de fa 989G un ⁿ acii 91°IC
$\mathbf{c})$	Oncle, Frere de pour motif de fa- de reirer son Pere	$\tilde{}$ ാര് \mathbb{R} പ്രീസി \mathbb{O} pour morif de fa azsk un) voit öv SS
d)	Oncle, Frere de pour motif de sa de reirer son Père	Oncle , Ineré de ^v pour morif de fa azsk nod "mir'an "Bö
e)	Oncle, Frere de pour motif de fa- de reliter sou Pere	Cacle , Hore de pour morif de la asé rémiér fon Père

Figure 9. Edges obtained with a) input image b) proposed method (type-A) c) Median filter d) Wiener filter e) combination method with TV replaced by Wiener.

OCR engine is a means for evaluating the improvements brought by the enhancement method we are proposing.

We consider two tunings for the OCR. One tuning consists of reducing the influence of dictionaries in order to test the improvement brought by the proposed enhancement approaches at the pattern recognition level, character by character. This is done by setting the Tesseract configuration variables *ok_word*, *good_word*, *non_word*, and garbage to one. This setting is suggested by [35] and allows us to run the OCR without dictionary-based corrections. Another tuning consists of using the Tesseract dictionary of the document language (here English or French) since dictionaries are often used to compensate for OCR errors. The improvement brought by both

preprocessing and dictionary-corrections is then observed.

We provide to Tesseract the grey level document images, unprocessed or enhanced. The OCR uses the Otsu thresholding algorithm to binarize the images. However in our combined approach, there are two kinds of background pixels: saturated and not saturated (see Section 2.2). Consequently, we have modified the Otsu algorithm within the OCR system to take into account the specificity of these images which include three modes. The modification consists of removing the saturated mode from the histogram. Similarly, the modification of the Otsu thresholding algorithm is necessary for set XX-b (News.3G) since those images have large white background zones around the clipped news articles whose paper intensities are moderately dark gray. The histograms of these images also have three modes due to the two backgrounds and the foreground. It can be noted that preliminary experiments on set XX-b [25] used a common global threshold for XX-b images, the value (75) being chosen as suggested in [36] for this data set. However for the sake of comparison, all sets are binarized in our experiments according to the same Otsu-based framework.

The main parameter of our proposed approach is the regularization parameter β . We first set the range of its values in Section 4.3.1. In Section 4.3.2, we evaluate separately the two enhancement approaches, TV and NLmeans, on the different datasets. Then we evaluate in Section 4.3.3 their combined performance.

4.3.1 Parameter setup

The most important parameter is the TV β parameter. In the following experiments we set the TV parameter β to increasing values with a step of 2, ranging from $\beta = 2$ to $\beta = 24$ for most sets, and up to $\beta = 30$ for sets XVIII-a and b since high values of β still yield high performance. Results in Fig. 10 show that:

- the β parameter can be set to lower values when the resolution of the characters is low,
- and set to higher values when characters are of higher resolution.

Thus, for sets XVIIa and XXb which include small sized characters, β values should be lower (lower than 12 for set XVIIa and lower than 6 for set XXb). The β values for sets XVIIIa and XVIIIb including characters of higher resolution should be chosen greater than 20. However a too fine tuning of this parameter is not necessary since ranges of values yield comparable performance of the TV regularization.

4.3.2 TV and NLmeans as single enhancement methods

TV and NLmeans can be used as single enhancement approaches and applied directly to document images [25]. We applied these methods in isolation at the ICDAR DIBCO 2009 document image binarization contest [18] and our results were reported top 10 (over 43 participants) according to the four measures used in the contest, and top 6 according to the F-measure only. We use the fast implementation of TV proposed by Chambolle [11]. We also use the fast implementation of NLmeans proposed by Darbon et al. [12].

Our first experiment consists of evaluating each preprocessing algorithm in isolation and compare their respective performance.

Results in Fig. 11 show the performance of TV and NLmeans for each set. Results

Figure 10. Performance of TV regularization as a function of the β parameter. Arrows indicate for each set the range of operating values for β .

are reported for the value of β yielding the best performance in the range of values determined previously in Section 4.3.1. Results show that in all but one set (XXb), TV and NLmeans as single enhancement methods, improve recognition. The improvement is small for less degraded sets such as XVII-b and XX-a, and higher for more degraded sets such as XVII-a, XVIII-a and b. The low performance observed when using TV for set XX-b can be explained by the loss of contrast resulting from

Figure 11. Performance of TV regularization and NLmeans filtering as single enhancement methods (without combination). Dictionary corrections are turned off.

Figure 12. Performance of TV regularization and NLmeans filtering when dictionary corrections are turned on.

the TV regularization. The loss of contrast is lower for NLmeans: this explains the better results obtained with NLmeans for this set. However, the combination of both methods will increase performance (see Section 4.3.3).

In Figure 12, results are given when dictionary corrections are turned on in the OCR. TV regularization is performed with the same β value for each set, obtained when corrections are turned off (see Fig. 11). TV and NLmeans improve recognition for all but one set as previously. Results in Figure 11 and 12 show that the improvement brought by NLmeans or TV is more important when dictionary-based corrections are turned off. While disabling of the dictionary is generally not desirable for practical applications, it shows that isolated recognition is enhanced with the proposed preprocessing methods. In particular for the most degraded sets (XVIII-a and b), the relative improvement brought by the preprocessing is the highest as shown in Figure 12. Even if the number of correctly recognized characters improves a little, the dictionary-based correction yields a much higher number of corrected characters. Similar tests were also performed using the ABBYY OCR system [5]. Results were comparable to those achieved with Tesseract, indicating the results are OCR engine independent.

The Otsu algorithm is the thresholding method provided with the OCR engine. However binarized images can be directly fed to the OCR. Thresholding can also be seen as an enhancement technique since it aims at removing unwanted background pixels and at detecting all foreground ones. To observe the effect of the thresholding on performance, we replace Otsu by the Kittler and Illingworth method [22]. We choose this method since it is also a clustering-based method. Results show that this thresholding globally performs worse on our document sets than Otsu. Performance is still acceptable for sets XVIIb and XVIIIa but for other sets there is a drastical decrease of performance. For set XVIIIb, the binarization of the unprocessed images could not even be exploited by the OCR. This may be due to the fact that image

histograms do not follow the underlying assumption of a two Gaussian mixture. However we still observe a global improvement with TV and NLmeans over no preprocessing when changing the thresholding method.

Figure 13. Performance of TV regularization and NLmeans filtering followed by another thresholding technique [22].

In summary in this Section, it has been shown that:

- TV and NLmeans as single enhancement methods globally improve OCR results,
- TV yields a higher loss of contrast compared to NLmeans,
- Thus, for low-contrast documents NLmeans should be preferred to TV as a single enhancement method.

4.3.3 Combination of TV and NLmeans

The two enhancement steps, TV and NLmeans, are now combined as described in Sections 1. There are two types of combination:

- the first type (type-A) applies the mask to the TV-regularized image,
- the second type (type-B) applies it to the NLmeans filtered image.

Results are provided for the two types of combination in Fig. 14. The value of β yielding the best performance is chosen for each set and each type of combination. We observe that the type-A combination is more effective for sets XVII-b, XVIIIa, XVIII-b and XX-a. The type-B combination is more effective for set XVII-a which includes the smallest sized characters. On set XX-b, since TV and NLmeans perform similarily as single enhancement techniques, both types of combination perform similarily.

The improvement brought by the type-A combination is very high for sets XVIII-a and b: the increase reaches 20% in absolute value for set XVIII-b. This is due to the efficiency of the background noise reduction step on these highly degraded sets. Additional results are provided in Fig. 20.

The choice between the type-A and type-B combination depends on how TV performs as a single enhancement method. If the TV regularization brings improvement, the type-A combination should be chosen. When TV regularizes too much, this degrades performance and the type-B combination should be chosen. It can be noted that for the type-B combination, the final enhanced image is not regularized by TV but TV is however very useful for removing the background noise. All combination types construct the same mask obtained by thresholding the TV regularized image. Noise pixels which have their grey levels flattened by TV are thus not included in the mask. When the type of the combination is correctly chosen, the combination globally brings improvement over each enhancement method in isolation. Actually,

the combination always yields an improvement except for the set XX-a for which TV alone performs slightly better. More precisely, the type-A combination has a 70.8 % recognition rate (see Fig. 14) while the best TV ($\beta = 16$) result reaches a 71 % rate (see Fig. 11) .

Figure 14. Combination of TV and NLmeans. Performance of the combined methods (type A and B) through character recognition accuracy (in $\%$).

It can be noted that the optimal β value for TV regularization as a single enhancement method may be different than the one used for the type-B combination. During mask construction, a high β value will remove small objects, which is desirable in the background, and this property is fully exploited in the type-B combination. Thus, we found that the $\beta = 20$ value is the most effective for sets XVIIa and XXb and for the type-B combination. Practically, setting the value of β for the combination may be performed on a training set when a collection of documents with similar characteristics (character size, contrast) is available. The peak of the graph representing the OCR accuracy as a function of β will indicate the best β value. Alternatively, the β value can be set to a default value. We found that $\beta = 20$ was an effective default value (see Section 4.6) and we provide additional results for this setting in Fig.18.

In summary, in this Section it has been shown that:

- there are two ways for combining TV and NLmeans, namely the type-A and type-B combinations,
- type-B combination should be preferred for low-contrast documents,
- the β parameter used for constructing the mask can be set to a default value $\beta = 20.$

4.4 Comparison with standard enhancement methods

We have compared in Section 4.2 the edges obtained by the proposed approach with those obtained by other enhancement methods such as the Median and the Wiener filters. In the following experiment, we compare all enhancement approaches through the character recognition rate. Figure 15 compares the accuracy at the character level without dictionary-based corrections for all data sets. The combined methods are of type-A for sets XVII-b, XVIII-a, XVIII-b and XX-a, and of type-B for sets XVII-a and XX-b. The combined approach always performs better than the other enhancement methods. Median filtering is a suitable approach for document restoration with low background noise (such as set XVIIb), but when background noise is high, it cannot remove all remaining edges as shown in Figure 8 and those edges interfere with the recognition.

Figure 15. Comparison of enhancement methods through character recognition accuracy (in %). Dictionary corrections are turned off.

We also conduct a combination experiment by replacing the TV- filtered image by the Wiener-filtered image. As previously we use the same combination type for each set: the mask is either applied to the Wiener-filtered image or to the NLmeansfiltered image. In both cases the mask is constructed using the Wiener filter. Results in Fig. 15 show that the Wiener filter globally performs better in combination than in isolation. The mask construction and image regularization with Wiener filtering is also effective when combined with the NLmeans filtering. However TV performs better.

4.5 Comparison with a PDE-based enhancement method

PDE-based approaches, originally developed for describing physical laws, rely on a diffusion process. As mentioned in Section 1, they can also be used for restoring images, including document images [14]. A popular PDE approach is the Perona-Malik anisotropic diffusion approach [30]. This approach relies on an iteration process which smoothes homogeneous regions while preserving edge discontinuities. Three main parameters govern the diffusion process. In the Kovesi's implementation [23], they are: the number of iterations, the integration constant δt and the gradient modulus threshold κ which appears in the conduction coefficient function.

We conduct experiments on our datasets varying the number of iterations. Choosing a correct number of iterations can be critical since characters may vanish if the diffusion is not stopped early enough. We avoid this by slowly increasing the number of iterations until a maximum is reached for the recognition rate. Thus, 14 iterations are generally necessary, except for sets XVIIIa and b which need more iterations. We set the remaining parameters to default values: $\delta t = 1/7$ and $\kappa = 30$. The diffusion coefficient is equal to $exp(-(\nabla I/\kappa)^2)$. Results in Fig. 16 show that there are sets (XVIIb and XXa) for which performance is stable within a range of iterations. For the other sets, performance shows more variations.

As a pre-processing method, PDE-diffusion improves performance except for set XXb. The images in set XXb include characters of different sizes and the constrast is low. The diffusion process results in a number of images where characters of the text body are merged, even for a small number of iterations.

Figure 16. Recogition accuracy as a function of the number of iterations when preprocessing images with the Perona-Malik PDE-based approach.

Comparing from Figs. 14 and 16 the PDE-approach with our combined approach, PDE performs slightly better for sets XVIIa and XVIIIb, and performs worse for the other sets (XVIIb, XVIIIa, XXa, XXb). For sets XVIIa and XVIIIb, the absolute difference in accuracy is 0.5 $\%$ and 0.7 $\%$ respectively, when choosing the optimum number of PDE iterations for each set. We have observed that the PDE diffusion yields thinner characters while our approach results in thicker characters. Thick characters have lost less detail but when characters are small, intra-character spaces may be filled. However our approach better removes the background noise which results in an easier line and word segmentation for the OCR. This is shown in Fig. 17 where the last words of the first text line and the first words at the beginning of the second line were correctly found by the OCR with our approach, but not with the PDE approach.

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Figure 17. a) input image from set XVIIIa. b) type-A combination c) OCR result for the type-A combined image (dictionary corrections turned off) d) PDE processed image with six iterations e) OCR result for the PDE-enhanced image.

4.6 Comparison with a mask-based binarization method

We have compared in the last sections the proposed enhancement method with several filters. All methods were followed by the same Otsu-based binarization performed by the OCR. We now compare the binarization obtained with the proposed enhancement method followed by Otsu thresholding with the binarization method presented in [19]. This method has been chosen since it is also mask-based and dedicated to degraded documents. We implemented the following steps: enhancement (Wiener filtering), estimation of the foreground and background images and final

thresholding. The estimation of the foreground image is performed through Sauvola adaptive binarization and it is used as a mask applied to the input image. Pixels belonging to the foreground region are interpolated in order to construct the background image.

We propose two ways of comparison. We first consider the proposed combination method as described in Section 4.3.3 using the best β parameter for each set. Then we set the value of parameter β to 20, which is the best β value when a single value has to be selected for all document sets. Setting β to a single value also corresponds to the case where the user does not know or does not want to set the β parameter and sets it to the default value. Moreover, since we compare the Gatos binarization method using its default parameter values, a fairer comparison with the proposed method is obtained when using a default β value. Results are shown in Figure 18 for all sets. The default parameters of [19] are used in these experiments except for set XVIIa where the weighting parameter q is set to 0.2 in order to avoid resulting blank images. Using the implementation of the Gatos binarization method provided thanks to the Gamera project [16] gave us similar results. Compared to this latter method, we observe better results for our method, both using the default $\beta = 20$ value and when β is tuned for each set.

For the sake of comparison, performance for all methods presented here are provided in Fig. 19 through box-and-whisker plots. Each plot shows the median value of the recognition rate for each method as well as the spread of variation (25th and 75th percentiles) of this rate through document sets. There are no outliers for our rates, hence the whiskers extend to the most extreme rates. The improvement of the proposed combination method can be observed through its high median value. TV

Gatos Binarization method [18]

Proposed method (beta=20)+Otsu Proposed method (best beta)+Otsu

and NLmeans as single enhancement technique also have high median values. The smallest spread of variation is observed for the Perona-Malik enhancement method. However the spread of enhancement methods based on TV and NLmeans (combined or not) is globally smaller than for the other methods.

5 Conclusion

We have proposed a new enhancement method based on the combination of two powerful preprocessing methods, namely the Total Variation regularization and the NLmeans filtering which have the ability to reduce background noise and improve character detail, respectively. We have proposed two types of combinations, depending on the size of characters in a document set. Both types use TV regularization

Figure 19. Performance of enhancement methods through box-and-whisker plots.

for eliminating noise in the background through the construction of a mask. We have compared our approach to other noise reduction methods, namely the Median and the Wiener filters, and the Perona-Malik diffusion filter. It has been shown that our approach performs better than these filters for most degraded documents on an OCR recognition task. An advantage of the proposed method is that it includes only one main parameter. Only the TV β parameter has to be set within a range of values according to character size and noise level. We have shown that when ones does not know or want to tune this parameter, a convenient default value is $\beta = 20$. However, automatically tuning the β parameter is a major perspective beyond the scope of this study. Another perspective is to locally adapt parameter β instead of globally. This would be useful for instance for processing fading character areas which need a lower β . Finally, evaluating our approach on other types of document noise such as speckle and blur as well as studying the impact of several local and global binarization techniques are also included in our future work.

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Un Courier extraordinaire de Madrid a apporté à la Cour de France à Marly la Nouvelle
du ravitaillement de Gibraltar par la Flotte Angloife, annoncée dans la Gazette de Madrid du 24. Avril: Mais en revanche ce même Courier a appris, que le Convoi de Marfeille, au fujet duquel l'on étoit inquiet, est en fûrêté dans le Port d'Alicante.

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24. Avril: Mais en revenche ce même Courier a appris, que le Convoi de Marseille, au dans le Port d'Alicante.

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attribution de qualités, au plus offrant et dernier encherisseur, du fonds de commerce dont la désignation suit:

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Tobacco chiefs still refuse

Figure 20. Enhancement results. Left: input image, right: enhanced image using a combination of TV and NLmeans.

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